CORBAUX
ON
POPULATION.

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To Mr. Oliver Byrne,

from his very humble Sol
Francis Corbaux

ON THE

NATURAL AND MATHEMATICAL LAWS

CONCERNING

POPULATION, VITALITY, AND MORTALITY;—

THE MODIFICATIONS WHICH THE LAW OF MORTALITY RECEIVES, WHEN REFERRED TO DIFFERENT CLASSES OF PEOPLE; —

AND GENERALLY THE MOVEMENTS OF POPULATION, IN ITS PROGRESS OF RENEWAL;

WITH

TABLES OF MORTALITY,

APPLICABLE TO FIVE CLASSES OF EACH SEX;

AND

OTHER TABLES,

EXPRESSING THE RELATIONS BETWEEN CAPITAL AND INCOME,

UNDER THE OPERATION OF COMPOUND-INTEREST:

BY

FRANCIS CORBAUX,

AUTHOR OF "*An Inquiry into the National Debt, and into the Means and the Prospect of its Redemption, with a Plan for redeeming that Debt, upon the principle of Terminable Annuities,*" etc. etc,

Rectè facti, fecisse merces est.
(SENEC. Epist. 81.)

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ERRATUM.

Page 134. — Chapter XXIII, — read Chapter XXII.

PREFACE.

The present subject was but incidentally treated in the "Doctrine of compound-interest;" of which, after distributing copies to friends and to subcribers, I preserved only the set of Tables that terminate this volume and are perpetually applicable, as they exhibit under various points of view the relations between Capital and unrestricted Income.

Innumerable transactions, in reference to contingent property depending on the chances of human life, take place on an assumption that such contingencies are correctly appreciated; yet it is certain that the representations hitherto set forth of the Law of Mortality, and implicitly admitted as grounds of computation, generally fail of the requisite accuracy, besides their being inadequate to the demands of contra-distinguishable cases. The defective character of those Mortality-tables is rendered apparent, from occasional

attempts at their improvement; but which attempts, uncontrolled by any definite principle, have left the matter scarcely less enveloped in obscurity than it was a century ago. Indeed the introduction of some additional tables, professing — though constructed in defiance of Nature's laws — to advance our information as regards the gradual waste of life, create greater embarrassment, consequent on such accession of discordant and contradictory results. The object is, now, to provide a remedy for those deficiencies.

Many fundamental questions, — relating to the average term of life, — to the comparative rates of mortality at specific years of age, — and generally to all movements of the population in its progress of renewal, — are however so complicated, from their subordination to local or transient circumstances, that the researches in this branch of science encounter endless impediments. Its having devolved on myself, to fathom those questions and strive against their incessantly recurring difficulties, should be imputed to the absorbing avocations of men more eminently gifted; which prevented their anticipating me. Perhaps some may have abstained, on considering the extent of sacrifice required for the completion of so arduous an enterprize. Let no one therefore suppose that

it has been unwarily ventured upon. Great is the diffidence with which I proceeded; diligent to remove all causes of error, ardently desirous of promoting available knowledge, and regardless of every personal inconvenience; yet trusting to devoted perseverance, for results that should ensure attention and entitle me to temperate judgment.

Those results principally unfold TEN *Sets of Tables*, referable to the discriminated sexes of FIVE *classes*; into four of which any considerable population may in different proportions be divided, and another class collectively representing the whole. Each set describes its appropriate modification of the *Law of Mortality*, whence follow all corresponding deductions; but personal limitations compel, as yet, the omission to publish such useful, interesting and numerous deductions, from each modified law in particular. A complete system of them extends even to the tabulated values of contingent sums, severally describable, as Annuities, Reversions, etc., and depending either on individual lives of each understood class and sex, on the joint-continuance of lives in plurality, or on the eventually last-surviving life; according to the respective ages, single or combined, of such considered lives, and to distinct rates of

Interest in the investment of Capital; independently of solving many important questions, not of a pecuniary description.

Other questions, hitherto unsettled, concerning the relative quantities of births Male and Female, the quantities of periodic Marriages compared with the amount of any Population, as also the average of births generally attributable to each marriage, are carefully investigated from incontestable data; and it is shewn, that all observed variations of such results proceed from ascertainable causes, amongst which the population's special distribution, into relative quantities of each sex and existing within certain intervals of age; a distribution materially influenced by such population being either stationary, or else in progress of increase or of decrease. Further a method is given, from which the average of births in expectation, by each marriage contracted at any specific age of the female, may be determined with sufficient approximation for practical purposes.

Embracing every part of a subject until now treated on loose grounds, and proceeding on principles confirmed by digested experience, my endeavours have constantly tended to establish an harmonious

connexion between each part and the whole; as also between the successive results developed in each series referring to any specific modification of the Law of Mortality, and between all corresponding results under its varied modifications.

The best view of collective objects is that which connects them. Statistics, the vogue in this age, though new only by name, constitute a science of facts presented under their natural relation, and vesting them with the character of evidence; but failing certain conditions, scarcely surmised by the *fact-collectors* who abound, it sinks into a science of deception. To omit none of the elements a complicated question may be composed of; — to discern, in the appreciation of facts, those properly comparable; — to ascertain them in quantity sufficient for attaching the due measure of probability to any conclusions from them, and for admitting those facts to found a general rule; — to exclude such as, from the mode of their collection, should be justly suspected of error, — are conditions the fulfilment of which is not the business of every meddler. They involve immense difficulties, which to overcome requires the union of sagacious penetration with many previous acquirements. Since the Baconian philosophy was introduced,

the inductory process, so fruitful in discoveries and important results, has been too much neglected; and misconceptions have prevailed, respecting what is meant by *Experience*. The experimental and inductory methods claim mutual assistance, without which the path of knowledge shall inevitably become obstructed; and it has been my study to render them equally available.

An apology however is called for, consequently to my having sometimes used dogmatical language, necessitated by the introduction of much unprecedented matter, and to occasional semblances of obscurity easily penetrable by those for whom chiefly I have written; resting my claim to public favour on other merits (if any) than that of style, which here should be of minor consideration.

The substance of this volume was embodied in a Memorial submitted to the Academy of Sciences, at Paris; *four* commissioners from which are appointed for its investigation. That deference was due in a quarter whence the materials have been in great measure supplied, and I confess gratitude for the very liberal spirit with which I have been met in that sanctuary of knowledge. It was intended to postpone the present

publication until a judgment there intervencd, subsequently to the Commissioners' report; but as the latter being brought up suffers unavoidable delay, it becomes proper to answer, without further loss of time, the expectation of scientific friends to whom my work has been long announced. It shall nevertheless be imperative on me to communicate, on some early opportunity, the results of that official investigation, when terminated.

Aware of this production's liability to improvement, I shall thankfully avail myself of any communication the enlightened amongst my cotemporaries might think proper to favour me with, to that effect, and even in the shape of criticism.

My last protracted sojourn on the continent having compelled me to confide this edition to a foreign press, I trust nevertheless that the minute attention bestowed on correcting the proofs, and a repeated collation of the tables, as also of all other numerical expressions herein comprized, will have completely assured the absence of disgracious errors.

After sparing neither my substance nor protracted labours, towards enlarged utility, I contemplate ulti-

mately to found an INSTITUTION for prospectively providing, at the time of Marriage, Endowments to each child that may issue therefrom, in whatever number; equitably proportioning all contributions, according to the wife's age on the respective contracts being entered into. A few particulars regarding that Concern, — which, as my property, I shall devolve to the public on suitable terms, — are stated in one of the following chapters.

FRANCIS CORBAUX.

Paris, 31st August 1833.

ON THE

NATURAL AND MATHEMATICAL LAWS

CONCERNING

POPULATION, VITALITY, AND MORTALITY.

CHAPTER I.

Of a primary LAW OF MORTALITY, *and its modifications.*

1. Amongst the points of resemblance, between our own and other species of the animal kind, is a similar tendency to ultimate resolution of the component parts of organisation, into their elements. The comparative periods at which this phenomenon is to occur, with reference to each species in particular, must first depend on differences in character and complication of that organization, as also in quality of the substances it has incorporated; whence greater or less capability of resisting the many causes of destruction by which the individual may be assailed. They will further depend on the degree of activity possessed by the organic fluids, and lastly on various influences of the surrounding medium. Those united circumstances most likely determine a certain standard of powers, adequate to support the vital principle throughout some limited period originally intended; assuming all external conditions of existence best appropriate to — and congenial with — each species respectively. Such limitation is then the

more probable, as, regarding a great number that include our own species, the process of respiration, through which that vital principle retains its action, indicates combustion, however slow.

2. Confining to the human species this view of the matter; if we admit in the utmost degree favourable, towards preserving the well-constituted individual, all secondary circumstances,—not only the external, but even those depending on the exercise of free agency, — the duration of life, as primarily assigned, shall certainly exceed its utmost term apparent on modern record; and although to ascertain such extreme period may transcend the efforts of calculation, it may without inconvenience be assumed at an arbitrary maximum, to which any law of mortality ought to bear reference.

3. This primary law of nature, however, is incessantly disturbed from the influence of secondary causes. It consists with the infirm disposition of man, that his inclinations and passions, excellent as they may be in some tendencies, should in their effects often prove injurious to himself and to his fellow-creatures; hence the assigned term of life is liable to abridgment at each of its stages, from innumerable causes combined according to time, place, circumstance, and resulting in a great measure from social arrangements. The variable proportions of untimely deaths, at different years of age, depend on greater or less inequality in the distribution of social advantages and disadvantages; on the circumstances of climate, soil and produce; on the mode of living, the characteristic temperament, the general habits, the confirmed abuses; and besides many other causes, merely accidental, a great deal on the government and neighbourhood, from which proceed the alternations of war and peace. The latter causes, indeed, are not very dissimilar with the circumstances affecting the brute

creation; amongst which, the domesticated species, and others peculiarly exposed to hostile enterprize, become subject to rates of mortality far different from the original intention.

4. The two sexes, differing in organization, in their allotted functions, and in the degree of activity of their faculties, shall further be liable to a corresponding difference as to the absolute term of life, as also to still greater and fluctuating differences in their respective rates of mortality at equal phases of existence; though the one and the other sex existed under all other circumstances as nearly alike as could be supposed.

5. Considering the variable degrees of intensity with which each of those combined causes is susceptible of operating, it must be easily conceived that the law of mortality admits innumerable modifications, more or less important to discriminate in its application to practical purposes.

6. Yet, in the present state of civilization, there is throughout Europe, and even beyond its limits, such assimilation of habits, customs and inclinations, with so nearly corresponding a distribution of occupations and other principal circumstances, that the rates of mortality, referable to each year of age respectively, do not appear very dissimilar in regard to the aggregate populations of extensive countries. Material differences, nevertheless, are remarkable in those rates applied to subdivisions of each population; consequently to great dissimilarity in the general conditions attendant on the existence of various classes of individuals. Amongst the inferior class, unwholesome or excessive labour, accompanied with partial deprivation of the necessaries for sustaining life and health, occurs in populous towns, rather than in agricultural parts of the country; as also, in a greater measure, the influence of degrading vices

on the chances of mortality; and all those are paramount causes of its elevated rates, whilst any disadvantage arising from difference of soil or of climate, especially the latter, operates but in less degree to the same effect. Therefore the tables deduced from direct observation in all countries, on the mortality of large towns, exhibit human life in its worse aspect; and they singularly contrast with analogous results of observation limited to the select classes, whose lot is to exist under a series of conditions eminently favourable to the protraction of life.

7. Those conditions, without regard to differences of individual constitution, chiefly consist in the certain and adequate supply of wholesome food, as also of other means on which the preservation of health may depend; in the exemption from injurious or intolerable labour, and in a reduced measure of detrimental habits. Admitting any specific class, to which such and a few other favourable conditions shall best apply; it is every where to be found, with reference to an equal quantity of periodic births, that the proportions according to which the lives drop at successive years of age are incomparably less, in that class, than in its counterpart, or class subject to notable disadvantages in social order.

8. The modifications to which any general law of mortality is liable are thence so diversified, under the view of special applicability, that the joint-continuance of two select lives of similar age and sex may obtain, during a long series of years, a probability superior to that of any single life of the same sex and age, but belonging to another class; though both classes were equally susceptible of being stipulated with, for the purpose of valuing contingent sums made to depend on such lives. Notwithstanding this matter of fact, it has long been of daily occurence to stipulate, concerning lives that belonged to a class in

more or less degree select, consequently to the application of a law of mortality so described as even to preclude any population from maintaining its level : those transactions being an unwarrantable deviation from the most common notions of justice, on whatever side might lie the advantage.

9. Neither, in England, Dr. Price's law deduced from the Northampton observations, nor in France the one computed by Duvillard from data chiefly collected in populous towns, could have approached a fair expression of the standard of vitality in those respective countries at large and at the time being; though both have been, during a long while, admitted for indiscriminate application. The same is remarkable of Dr. Halley's law, deduced from observations at Breslaw (in Germany), and exhibiting results of great similarity with the first two combined. If it be considered that marriages average a fraction less than *four* births each, at the same time that *sixteen* births admit, according to those laws of mortality, no more than *seven* survivors at *twenty-six* completed years of age, taken also on an average as the age for marrying by both sexes; and even supposing every individual, without exception, then to marry, however impossible this generally is; it follows that each succeeding generation should, consequently to such laws, have suffered a diminution of one-eighth part of the population, wich on the contrary has progressively increased. Making allowance for inaccurracies whatsoever in these round statements, they sufficiently attest that experiments confined to populous towns, where the inferior class of people exist under circumstances peculiarly unfavourable, are incapable of supplying correct data towards ascertaining the real standard of vitality in any country.

10. Independently of such modifications as the law of mortality may receive from local circumstances, or from

distinctions of classes and of sexes, there are further modifications which from many other causes are likely to arise in process of time. The conditions of existence, as affecting any mass of population, may in numerous respects improve or degenerate; and without adverting in particular to causes depending on government, neighbourhood, manners or customs, it will be sufficient to remark that the influence exercised by prevailing diseases, on the rates of mortality, is perpetually fluctuating. Some diseases, of pestilential or contagious character, retain, during a longer or shorter period after their first invasion, a considerable intensity of morbid influence, which subsequently declines; whilst other diseases, more or less destructive, become in turn predominant. The present age is not unlikely to mark some notable change in this respect, and perhaps no longer on the side of amelioration. It is obvious, however, that Permanence is not an attribute of the Law of mortality.

CHAPTER II.

Of preceding attempts at ascertaining the Law of mortality; — the conditions required for such ascertainment; — and the sources of error to be guarded against.

11. It could not answer any useful purpose, neither consist with the motives of this publication, to dilate on a critical history of many attemps at ascertaining the law understood to regulate the waste of human life. The talented men to whom the world stands indebted for those laborious researches are mostly our cotemporaries, entitled to respect, which can suffer no diminution from their having sometimes lapsed into error, or rather inadvertence; when the subject for investigation was so intricate, as, at least, to require being met by an unmixed avocation. Sufficient will it be, for all purposes of comparison, hereafter to collect in the shape of synoptic tables the results to which those authors severally arrived. In a single instance of exception, the latitude is however taken of a more detailed inquiry into the bases lately sanctioned by an Act of parliament, for computing the values of life-annuities thereafter to be charged on the British exchequer.

12. Before the matter under consideration had acquired its present and daily growing importance, materials collected from the observation of facts, at various times and places, were already wrought upon, towards discovering the law of mortality amongst mankind in a civilized state.

But to obtain such results as, without inducing injurious errors, might be applied to pecuniary agreements, (being a special object of the investigations,) various modifications of the data, consequently to notable differences in the conditions of existence between distinguishable classes in a whole population, should have been taken into the account; whilst a reference of those data to the discriminated sexes was not less an indispensable requisite, inasmuch as existing under dissimilar conditions, throughout their active life, neither the one nor the other could accommodate with any imaginable law common to both. Those materials afterwards acquired greater extent, and it was attempted to distinguish between the male and the female. Yet comparing all analogous results, referred to the one and to the other sex, they mostly fail to harmonize in some essential point, and frequently are discrepant in different parts under mutual dependance, when those results are considered in any specific modification of the law of mortality; whether it so happen, from too narrow limitation of the facts observed upon in each instance, — from mistaking altered proportions in the distribution of an increasing population, for those that exclusively belong to a stationary one, which is always a fundamental supposition in those computations, — or from any other cause. On further remarking the contradictions with each other, which almost all the hitherto concluded tables of mortality exhibit, it becomes obvious that not one of them,—though it were constructed with mathematical precision, upon data carefully and completely collected during a sufficient period, within any local circumscription, — could be susceptible of generalized application.

13. Data collected on a limited scale, from the registries of births and of deaths, are in all respects inadequate. On an extensive scale they are at best disproportionate in some of their details; and singly considered, in their crude state,

those collections of either description could never be available as decisive experiments. Previously to being admitted, they first require confirmation from — or corroboration with — other corresponding data; and secondly, to undergo methodical adjustment on settled principles. Until then, such results are merely susceptible of notation, as possessing an uncertain quantum of probability; to be taken into consideration, after a comparison with analogous results of observation, and when a moral value shall with judicious discrimination have been assigned to each in particular. From further motives that shall be adduced, other data less liable to error, such as lists of tontine-nominees, of life-annuitants, or of insured-lives, are equally precluded from admittance without preliminary correction; the unavoidable defect, of all which data, consists in a paucity of their distributed quantities, namely, of the living and the dying at each year of age; quantities usually admitted as chance may have produced them, or at least under such corrections, only, as could make but a distant approach to regularity in each series and their progressive differences. Let us take a more extended view of this part of the matter.

14. Towards warrantably using the unmitigated results of observation on the mortality of any considerable town, as we will suppose for the sake of exemplification; there would *first* be required, both at the commencement and termination of the period observed upon, a correct census of the population distributed according to successive years of age, which should be ascertained without error proceeding from careless indifference or from any other cause; *secondly*, that the registry of deaths were exempt from misrepresentation of ages, whilst it is of common occurrence to substitute round numbers, or else the multiples of 5, for ages differing only from these by a year or two; *thirdly*, that the observations were extended to the fate

of all infants committed to the charge of nurses in the surrounding country; *fourthly*, that a correct account were kept of all individuals who, being born in the place, may have removed in their pursuits whatsoever, and of their ages at the time of such removal; *fifthly*, that a similar account embraced the whole of travellers, settlers, artisans, labourers and others, according to their respective ages at their incomings and outgoings, during the entire period of the undertaken observations; *sixth* and lastly, that such period were sufficiently extended, for rectifying, through a fair average of the events in different years, and regarding the rates of mortality, all casual disproportions which never fail to arise, whether from the influence of seasons of abundance contrasted with those of scarcity, or from prevailing diseases and other temporary calamities, to which the individuals within certain limits of age may become liable, preferably to any other. Those various data should also have reference to ascertained quantities of annual births, during the same period of observation; in order to establish the general character of such local population, whether as stationary, or as progressively increasing or decreasing, and in what ratio of either. From the difficulty of procuring accurate information on so many points, and on a large scale,—difficulty increased by the additional requisite of discriminating the sexes in each instance, — the inference is, that the necessary data for concluding, by the means and under the circumstances just described, any Law of Mortality entitled to unhesitating confidence, are nearly of impossible attainment. Those difficulties, certainly, could not quite escape the penetration of men qualified for engaging in researches of this kind; but the full bearing of inevitable inaccuracies, with which the obtained results were tainted, must have been unperceived or underrated in most cases, especially when the population continued progressive during the period observed upon; and data altogether incorrect and incomplete were consequently con-

sidered admissible, with less solicitude concerning previous rectification than ought to have been entertained.

15. Metropolitan localities, whatever facilities they may otherwise afford for collecting statistical information of various kind, are less capable than any other of supplying the correct elements for a law of mortality. Consequently to their multifarious prerogatives, inducing a perpetual ingress and egress of persons resorting there for temporary purposes, those localities exhibit confused masses of population with only ephemeral identity; whence all natural proportions, between the living and the dying at corresponding years of age, are falsely represented.

16. All countries of Europe are not in an equal degree favourable to supplying efficient data. In France, in Prussia, in Sweden, in Denmark, and in some other dominions of less extent, the legal obligation, strictly enforced, of immediately inscribing in authentic registers the births and deaths that occur,—with all possible reference to identity in the latter case,—affords valuable means of solving the principal questions for which those data are intended. In England, we are lamentably deficient in this respect, from the carelessness with which such matters are legislated upon, and from the unjustifiable neglects tolerated by established custom in the records of life and of death; hence the numerous fallacies and contradictions with which our periodic returns of population are replete, as also the clumsy averages, which in despair, and from mercantile habit, we are satisfied in admitting. Much praise indeed is due to gentlemen of local influence, for their persevering efforts, occasionally to supply useful information concerning the movements of population in certain towns and districts; but their observations are necessarily confined within limits too circumscribed for answering general

purposes, to which the single exertions of individual zeal must always prove insufficient.

17. The most available data, towards obtaining a correct representation of the law of mortality, referable however to an exclusive class, would unquestionably result from observations amongst the annuitants, or else amongst lives having been the subject of an insurance; admitting that such observations embraced adequate quantities of either, and also a period of sufficient extent for tracing the greater number of individuals to the extremity of their lives. But we are still unprepared for completely fulfilling those conditions. Life-annuitants, of the several governments, have not been in requisite number for admitting, conformably with their respective ages at the time of entrance, a subdivision from which the proportions of periodic survivors could be exhibited as approaching to regularity in their series; and the insured are under a similar predicament, though in less measure than the lives precedingly described. If even all the insurance-offices consented to publish the results of their experience, (any inconvenience of doing which is scarcely conceivable as applying to old established concerns,) it could avail only as affording a series of probabilities liable to more or less correction; whilst the short experience amongst recent concerns of that description possessed very little value. Again many conventional restrictions, attaching to life-insurance, permit the law of mortality to be traced from that source but with an exception of the first ten years; as also such law, inferred from observations upon the annuitants, must exclude a greater or less number of those first years of life, consequently to a paucity of nominees at those early ages.

18. Supposing adequate quantities of observable lives, either of the one or of the other description, the results

will still be vitiated from a circumstance probably not attended to; and the inconvenience of which, if perceived by those who engaged into computations from such data, appears at least to have been underrated. This circumstance requires explanation; bearing in mind that those classes, both the life-annuitants and the assurable-lives, possess in greater or less degree the character of selection, to which therefore must be exclusively referable any law of mortality concluded from the experience they afford.

19. Regarding insured lives in particular: — A list of individuals at various years of age is indefinitely recruited, whilst the lives it represents are successively dropping, in whatsoever proportions; and the admitted on that list are, in all instances, ascertained at the time being to exist under circumstances qualifying them as select lives of their specific ages; being accordingly susceptible of lower rates of mortality, than those appertaining to individuals of corresponding ages amongst the indiscriminate population. Whether the list increase or decrease in number, by process of time, is immaterial to consider; but it is an important remark, that most of those lives will, subsequently to entrance, and from various causes, abdicate in greater or less degree such primary character of selection, as was the condition of their admittance; so far indeed, that at later periods, it should in all probability have been denied to a considerable proportion of those earlier entered individuals. Let us now suppose, after protracted experience of such a state of things, — thus operating referably to the rates of mortality exhibited at each year of age, — that a table computed from the whole were understood to represent the natural law of mortality concerning such a class of select lives; that law shall obviously be tainted with error, throughout its details. The error will be greatest as regards the earlier ages, and less with reference to the more advanced; because the gradual degeneration

will have proceeded during a longer time, in the former, than in the latter case; and because lives of recent selection will, at every stage, have been assimilated with degenerated ones; thus confounding, at each distinct year of age, the lower with the higher rates of their respective mortality. Not only those rates, or the Specific intensities of life referred to each year of age, must consequently be found in excess, decreasing however from the earliest to the latest; but what is commonly called "*Expectation*", being the average duration of life, — measurable amongst all individuals at any minimum of age, and taken together with those above such age, — must then be misrepresented in corresponding and similarly decreasing excess.

20. For effectually obviating this inconvenience, by which the results of experience extended to annuitants are also more or less affected; and in order to obtain a correct representation of the gradual waste of life, with reference to those classes, it would be requisite to trace the progress of mortality amongst the collective number of individuals entered as select at each year of age, at all times discriminated from others who entered at earlier ages. Failing which distinction, there remains the only alternative of an arbitrary rectification and adjustment of the series of life's intenseness, otherwise the rates of mortality at successive years; a process which, sagaciously conducted, may yield results sufficiently approaching the truth for practical purposes. The above remarks particularly apply to the tables constructed from the experience of the "*Equitable*", assurance-office; but on which tables it is not the present intention to exercise any further criticism. *

21. Resuming the consideration of indiscriminate popu-

* I find, on recurring to Mr Milne's work, whilst this is under press, that he made a similar remark respecting Deparcieux's tables.

lations, whether of a whole country, any town, or particular district; let us now suppose the population to have remained stationary, or very nearly so, for a series of preceding years, continued with the period of observation; and let us assume correct returns of the deaths occurring at each year of age during that period; which requires, for greater accuracy of the results, to be more extended proportionably with the limitation of such population observed upon. The elements for constructing a Law of Mortality, referable to any particular locality, will then be complete; without need to ascertain the periodic quantity of births, which under those conditions becomes inferable from the returned deaths only. It is immediately consequent on a stationary population, or periodic equalization of the births and deaths, that the quantity of individuals attaining any stated age is constantly represented by the total of deaths occurring at ages more advanced; whence arises an ascertainment also of the quantities of the living at each year of age, the sum of all which represents a certain quantity of aggregate population, referable however to a plurality of years equal to the term of observation. It again follows, from those various quantities bearing a mutual relation, that, dividing the latter quantity by the number of years which the period of observation may have embraced, the quotient shall exhibit an actual quantity of permanent population; that the distribution of this, into actual quantities of the living at each completed year of age, will be announced by the quotients of their respective quantities, divided by the same number of years; and that the rate of mortality, affecting each year of age in particular, will result from dividing the relative quantity of individuals who entered upon that year of existence, by the relative quantity of deaths during the next periodic interval. Those rates will from a series conveniently expressing the intensities of life, referably to each age and to the period of one year next ensuing; a correct determination of which series

is the precise object of the "*Law of Mortality*," it in fact and more properly speaking constitutes.

22. Should any experienced state of things accord with this preceding description, the following method usually employed for constructing such a law, or rather a series leading to its ascertainment, will be applicable.

23. After having ascertained the respective quantities of individuals who failed to complete their first, second, third, or other more advanced years of existence, all referred in due proportions to such annual periodicity; the successive subtraction of those quantities from the annual births, or radix corresponding with the completed year *zero*, and represented by the total of annual deaths at all ages, shall exhibit a series of survivors at the commencement of each year. This series does not precisely constitute the law of mortality, for which it is commonly mistaken; but it properly represents the periodic Decrement of life throughout its assumed extent, this identity of expression being consequent on the stationary character of the population. Yet the total of those quantities of individuals, entering upon each year of age, represents not accurately the amount of actual population, because some part of those who enter on any one year will fail to complete it; and a second process must therefore be gone through, for rectifying that inaccuracy. The quantity of lives taken at the age *zero*, and all of which have not completed their first year, may be considered as having averaged a *half-year's* existence; the quantity of those who completed a first, but not a second year, may be averaged at 1 1/2 years each; also the quantity of lives completing a second year, though not a third, may be averaged at 2 1/2; and thus proceeding, for every subsequent year of age, the sum of those successive products shall represent the aggregate population. This process may

however be abridged, by summing up the quantities of individuals who annually entered on each year of age, and subtracting from the whole one-half of the annual births.

24. But when the population has been, during any protracted period, in progress either of increase or of decrease, the quantity of annual births can no longer be inferable from the recorded deaths; nor can the quantity of the living at any assignable age be assimilated, as in the above-stated case, with the total of deaths thereafter occurring; because the permanent proportions, justly assumed in that case, are in the present more or less disturbed, especially as regards the distribution of any amount of population, into relative quantities of individuals at various stages of existence. All analogous results will then be obtainable through other methods; which, together with those of inferring from the decrement of life various further series, are reserved for discussion hereafter.

25. One of those further series, conveying an appropriate expression of the Law of Mortality, will represent the Specific intensities of life at successive years of age, and measured with reference to the interval between each of those years and the next ensuing. That important series constitutes the *Law* itself, inasmuch as its analysis ought to exhibit, with mathematical accuracy, even the elements of increase or of decrease in those successive expressions of intensity, always regularly progressing. Such law of mortality can only result from a methodical rectification of the former series; which, and though produced from direct experience, inevitably involves numerous irregularities, arising from the capricious operation of chance. It is remarkable, that of twenty-five (or more) different series hitherto set forth as expressing the Decrement of life, the one computed by Duvillard, and referred to the population of France, should have

afforded a solitary instance of its rectification upon any definite principle.

26. Notwithstanding that the natural law, supposed to regulate at each stage of human existence the proportion of individuals destined to attain any other specific age, may at first seem to elude detection, the absence of positive information in that respect is thus capable of being in great measure obviated by a course of well-directed experiments. Observations prosecuted through the single exertions of individual zeal could scarcely embrace, for a considerable length of time, all requisite details concerning the entire population of any extensive dominion; hence the tables concluded from observations usually limited to certain localities, where only those details could be obtained with tolerable accuracy, or to classes of people collectively existing under definite conditions, have always proved erroneous, when assumed to represent the gradual waste of life in the respective countries at large.

CHAPTER III.

Of the Life-intensity's presumed increase, during a late period.

27. Whether or not any sensible increase in the average term of life has taken place since the latter part of the expired century, with regard to some principal nations of Europe, is an important question arisen within the last few years; and there appears sufficient ground for admitting the affirmative, yet with much doubt concerning the extent of such increase. This affirmation, in its generality, involves an assumption that the conditions of existence amongst whole masses of population have received material improvement; which, as a main fact, is not sufficiently proved by the results of computation, upon data often uncertain, and more frequently misapplied. Neither is such proof afforded by the better ascertained fact of a progressive population, during the interval of time alluded to; for this may partly be ascribable to a quite different cause. It is obvious, however, that the question should have reference to distinct classes, who may not have equally participated in the supposed improvement. This is most likely, also, to have taken place in different proportions, referably to the discriminated sexes and to specific intervals of age; but the means of investigation being inadequate, to trace the question through those various distinctions, we must for the present be content to consider it in a general point of view.

28. According to fourteen years of the latest experience in France, where correct returns are regularly supplied; if its average population, during that interval, be divided by an

average quantity of its annual births, as also distinctly by an average quantity of the annual deaths in that country, and a geometric proportional be taken between the two quotients, the result will be found 35·74; expressing, by a number of years, the absolute intensity of life, or its average duration.* This quantity is to be compared with analogous results, specially referable to the same country; *first* with 28·76, resulting from Duvillard's statements, referred indeed to its indiscriminate population, but more properly to be considered as proceeding from an experience limited to the towns**; *secondly* with 32·26, resulting from a modification of those statements, consequent on the having abstracted all assumed influence of the small-pox upon the rates of mortality; and *thirdly* with 34·90, resulting from Deparcieux's researches, confined to lives of a select description; observing, as regards the latter, that the data relative to the first three years of life have, — for the purpose of completing the elements required for a law of mortality, — been hypothetically supplied, according to Kersseboom's experience amongst the Dutch annuitants. It is likely that 31·83 years, proceeding from an amalgamation of the first and third of those results, may approach a correct expression of the average term of life throughout France, towards the periods referred to; whence the increase in that country, within a lapse of 70 or 80 years, has apparently extended to 3·91, or a fraction short of *four* years. A great part of Duvillard's researches having been directed to ascertain the amount of influence exercised by the small-pox on the general mortality, which influence he has shewn to have abated 3 1/2 years

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* It will hereafter be shewn, that such proportional yields a correct expression of that intensity, or of what has been usually denominated the *Expectation of life*, referred to the birth; whenever the quotients diverge, consequently to an increasing or to a decreasing population.

** The writer has availed himself of an opportunity, to ascertain that the fact stands as here represented.

from the average duration of life there, and at the period referred to; it becomes worthy of remark, that an addition of the latter quantity, to the above 31·83 years, nearly reproduces the expression of life's absolute intensity in France, referred to an average of the last fourteen years of recorded experience; hence an increased vitality apparently equalizing with the influence of the abovenamed disease, at a former period. It will however be observable hereafter,— according to statements in chapter X, — that the intensity, after increasing to full 36 years, with reference to a period embracing the five years 1821-1825, has suffered some notable diminution for the succeeding five years, or averaged period 1826-1830.

29. Exclusively considering the *forty* counties of England: we have, as analogous results, according to M. Rickman's statements in a recent publication professed to be a digest of the population-returns ordered by Parliament, 41·6 years average duration of life, being a quantity equally apparent from the first and from the second decennal returns; as also 44·7 years, likewise apparent from both the third and fourth, which last returns are carried to the year 1830. Were those results admissible as correct, we should have to compare them in the first place with 25·18, deduced from the Northampton observations, embracing the 46 years that terminate with 1780; and secondly with the results of various other experiments, either referred to select parts of the country noted for peculiar healthiness, or to specific classes, such as assurable lives, possessing a quality superior to that of the population at large; amongst all which, M. Milne's statements, relative to the town of Carlisle between the years 1769 and 1787, yield 38·72, the highest comparable quantity. Allowing for numerous omissions, doubtless involved in those decennal returns, and in all probability more extensive as regards the last two; besides further allowing for any inferiority of the Northampton population in parti-

cular, when compared with that of the whole country; there still must remain between the contrasted results, under all requisite corrections, such a difference as could scarcely be attributable to any other cause than some real improvement in the standard of English lives.

30. It would however be absurd to admit, in the average duration of life, an increase of 19 1/2 years, rendered apparent from comparing the results of the Northampton experience with those of the last decennal returns; at the same time, the wretched system under which the records of births and of deaths are kept in this country leaves the greatest difficulty in reconciling the very considerable difference here observed. That of 3·07 years, just now assumed to exist between the compared results for France generally and for the aggregate of its towns, is doubtless exceeded by the actual difference of life's intensity throughout England, and that which relates in particular to the manufacturing town of Northampton; but assuming as a probable maximum, on the score of the latter particularity, a further extension of *three* years, we obtain 31·25, — not without much probability of approximating the truth, — to express the intensity in England, with reference to a period nearly corresponding with that of the anterior french observations; the respective intensities then differing no more than in the fraction 0·66 of a year, to the disadvantage of our own country. We continue at fault, however, in the attempt to account for a remaining difference, not less than *thirteen* years, between the latter expression of life's intensity and the one brought out by the official returns of more recent date; which there seems no alternative from concluding to involve manifold errors.

31. If an amalgamation could be admitted, of the two extreme results, deduced from the Northampton and from the Carlisle observations, in the same manner as it has been

assumed in regard to Duvillard's and Deparcieux's tables of mortality, we should again find the mean duration of life about 32 years; but this mode is objectionable, inasmuch as the periods, to which the two former sets of observations refer, do not possess the requisite coincidence. Nevertheless, as the apparent results would, under such an admission, very nearly assimilate the expressions of life's intensity in England and in France, both referred to periods more or less remote from the present, an indication is thereby afforded, that the assumptions indulged in the preceding paragraphs are unlikely to be much at variance with the truth.

32. But the amalgamation alluded to is ineligible on other grounds. Without injustice to the talented author of the Carlisle tables, there is a probability of their yielding expressions of intensity more elevated than they should obtain; considering their reference to an indiscriminate population, observed at a period even anterior to the introduction of vaccination, which only took place at Carlisle in the year 1800. Unless it were an established fact, that the lives at Carlisle generally possessed great superiority over those of the kingdom at large, — such a superiority as at least to assimilate them with the select class of Assurable lives, from which all individuals unfavourably circumstanced are positively excluded, — there remains no other alternative than to suppose that many important modifications, hereafter shewn to attend an increasing population, have been overlooked. And it will be seen at the same time, that, in such case, an approximate expression of life's absolute intensity shall result from dividing the population, averaged during the period observed upon, distinctly by the averaged annual births, as also by the averaged annual deaths of that period, and from admitting a geometric proportional between the two quotients; which coincide only when the population is stationary.

33. Perhaps we may come nearer the truth by comparing the Northampton results, under their aforesaid correction, with those further announced by M. Rickman, of a specific experiment extended to 18 years terminating with 1830, on the mortality of the single county of Essex, lately much improved in healthiness. In that instance, we find the comparable quantity of 34·47 years, average duration of life; exhibiting some approach to the results of authentic data relative to all France and referable to the same period. Then, admitting 31·25 years to express that duration at a former period, the improvement in this country would have extended to 3·22 years, whilst the corresponding improvement in France to 3·91.

34. Not only it should be borne in mind that those compared results, referable to England, rest on a very loose foundation; but also an allowance is to be made for M. R's probable inaccuracies. However disinclined to cavil at the valuable statements for which we are indebted to him, and highly appreciating his meritorious researches, a few remarks on those statements are indispensably called for; supposing that any distinctions he may have taken are not here misunderstood.

35. In consequence of abstractedly considering the quantities of deaths, as alone capable of supplying the elements for a Law of mortality, although an increase of population continued in progress during the observed period of eighteen years, those Essex tables, inferred from such exclusive data, must bring out in *excess* the expression of life's Specific intensity* referred to each year of age, except the very advanced; in the same manner as probably has

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* Quotient of the living by the dying at a similar age : see chapter XVI.

occured respecting the tables for Carlisle. Moreover, the proximity of Essex, to the metropolis, occasions a periodic and considerable emigration from that county; of individuals mostly female, in search of service or in other pursuits, at stages of life when the rates of mortality are notably inferior to that of the aggregate population; whence, all identity disappearing, the natural proportions between the living and the dying, within certain limits of age, must be greatly disturbed. It may further be, that from not having adverted to this circumstance, in the attempt at discriminating the sexes, M. R's tables, distinctly referred to the one and to the other, exhibit the Absolute intensity of female life in an insignificant degree only superior to that of the male. Indeed this inadvertence becomes obvious, upon analyzing the tables of mortality which the author has introduced; wherein it is made to appear that the rates of mortality, from the ages of 10 to 43 years, were much lower for the male than for the female sex; a result at variance with the best established facts, and proving that a considerable proportion of the female population, within that interval of age, must have removed from the scene of observation, though belonging to the original account.

36. Some recent returns under the authority of parliament, and stating, with regard to the populations of certain towns in England, the proportions of survivors at the respective ages of *five* and of *twenty* years, out of any equal quantity of births, do not generally exhibit human life in a much more favourable aspect than the Northampton observations already alluded to. Neither do they, on the whole, appear to corroborate the assumption of an improved vitality; but they confirm what has been said in the foregoing pages, concerning the remarkable disadvantages to which the populations of towns generally, and of manufacturing towns in a still higher degree, are obnoxious.

37. Thus deficient in data of sufficient accuracy and certitude, for establishing any measured difference between the Absolute intensity of life in England, at two periods remote from each other; there remains only a moral probability attached to the alleged increase of that intensity, and arising from the discrepancies of various results equally liable to correction. Such probability would receive considerable support from the distinct and better authenticated fact, of an increase not less than *fifty per centum*, in the British population, within the last thirty years (a proportion of increase very superior to that which has taken place in France during the same interval of time); were it not that such increase may partly be ascribed to an independent cause, namely the average proportion of periodic births, respecting which our public records are contradictory with palpable facts, as they also are in many other points of desirable information. Admitting, in round numbers, that proportion of increased population; it is reducible per annum, and during those thirty years, in the inferior ratio of 1·0136; whilst a similar result should be obtained through the single circumstance of about *one-twentieth* part's increase in the understood quantity of periodic births, otherwise by 3·85 resulting from each marriage, instead of 3·67 only*; and that to some circumstance of this description the observed increase of british population may in great part be owing, is at least within the scope of probability.

38. A greater or less increase of the measured vitality in England, within the last half-century, appears however to be upon the whole unquestionable; though announced with so much exaggeration, in late publications, that their authors seem rather possessed of inclination for the mar-

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* The more probable average : See chapter XXIII.

vellous, than acquainted with principles proper to guide through the intricacies of such a subject as the present, and which they merely glanced over.

39. It is presumable that other nations of Europe have, in various degrees, partaken of the cause of this increased vitality. The principal causes, regarding France particularly, consist in the ameliorated circumstances under which the mass of its population exists, and which are self-evident; in improved habits of life, and better management of health, especially during infancy; as also in the benefits of vaccination, most extensively introduced there, and which, notwithstanding well-founded doubts of its efficacy as an absolute preservative against the small-pox, does very materially mitigate the dangerous character of that contagious disease. The last two causes will have not less contributed their beneficial influence in favour of this country; but there is not an equal certainty of the previous cause having operated on our general population, the progressive quantity of which affords not a complete testimony of improvement in their circumstances. The systematic concentration of property; the monopoly of all social advantages; the unequal pressure of a public debt, even not justly that of *persons*, and still less of the unborn; the conversion of salutary institutions into instruments of oppression; an ostentatious charity substituted for equal justice, with an extensive code of abuses and arbitrary proceedings governing with influence superior to that of the positive laws, cannot fail in daily adding to the accumulated miseries of a contemned and trodden-down population.

CHAPTER IV.

Of what is now required for practical purposes, in respect to ascertaining the Law of Mortality.

40. The foregoing will have sufficiently proved, that local experience is inadequate to the supply of data, for a Law of Mortality susceptible of generalized application and permanent use. The synoptic tables, hereafter, will confirm that such results of abstract observation, though proceeding from laborious researches often conducted with great sagacity, forfeit all claim to confidence, from their discrepant and contradictory character; besides its being universally acknowledged, that the indiscriminate application of those tables, to social concerns, has never ceased to generate miscalculations more or less injurious in their consequences. Considering again the varied modes in which the law of mortality is applicable to human transactions, even of an opposite nature, whence suitable modifications of that law are called for, according to differences of sex and of the classes severally dealt with; together with the perplexing hesitations attendant on the necessity, in each particular instance, of preferably appropriating, at all risks, any one of those tables introduced at various periods, under a diversity of circumstances, and mostly founded on assumptions differing from the real state of things; it becomes urgent to adopt for the future, and on definite principles, such a mode of settling all questions concerning the applicability of specific tables, as may best secure against grievous and incessantly impending mistakes.

41. Failing more eligible means, probably hopeless, the only resource appears to consist in supplying a set of co-ordinate tables, immediately referable to the discriminated sexes, and to such definite classes of each as may for greatest convenience be contradistinguished in any population; a primary condition being, that those modifications of the law of mortality should, under every point of view, harmonize on a general comparison with each other,—in the relative results of any one of them,—and in all their inferable consequences. Those tables must necessarily be deduced from the mass of data hitherto collected, and each of which is understood to possess an uncertain measure of probability, or moral value, assignable to it in regard to the whole. Thus all discrepancies, in the results of actual observation, may severally concur to mutual correction, when proceeding under the control of settled principles, founded upon enlarged as well as digested experience; and contradictions, otherwise difficult to avoid, will then be best guarded against, whilst all general facts and phenomena will become capable of faithful representation, even to the utmost attainable stage of human life.

42. The plan thus traced, and executed through methods reserved for subsequent discussion, evolves Ten different modifications of the Law of Mortality, referred to Five classes of each sex. Any preferable application, of either, will be naturally suggested and justified by the specific quality of lives, the contingencies depending on which required an ascertainment of their respective values; and such application will be unattended with danger of committing errors of any consequence.

43. Granting, on a general principle, that no Law of mortality could possess the attribute of Permanence, because greater or less fluctuations of the elementary data shall

inevitably occur through lapse of time; whatsoever inconvenience arose from this circumstance would the more easily find its remedy, as any increase or decrease of life's intensity may not be unlikely to affect in nearly equal proportions the various years of age. The apportionment of any observed difference may then take place, by corresponding augmentations or diminutions, throughout the whole series expressing the Specific intensities at successive years, or else confined within certain limits of age, as the case may demand. Otherwise any two proximate modifications of the law, referred to the same sex, might be amalgamated in requisite proportions; thus producing an additional modification, suitable to the case. But it must constantly be borne in mind, that the aggregate quality of lives, in any considered population, obtains a positive and appropriate expression, from any ascertained relation between the quantity of the living at all ages, and that of the periodic births, as also of the periodic deaths, proportionally compensated.

44. This fulfilled task resembles that of the historian; who first gathers confused and contradictory memorials, tainted with partiality or prejudice, and having reference to the times he purposes to describe; who analyzes them, with the view of assigning to each testimonial its just value, from rational probability; endeavours to discriminate those parts which may on sufficient grounds be received, from others that should be rejected, according as the assumed facts obtained confirmation, or otherwise were destroyed by contrasted reports, and according as he detects the various influences of party-spirit or of individual passions, as also those of personal interest or vanity; thus establishing, from due consideration of the whole, a chain of events characterized under their true relations.

45. Before entering into particular statements, it will be proper to announce and develop the principles proceeded upon; which, together with their train of consequences, may be deemed incontestable.

CHAPTER V.

Of the DECREMENT *of human life.*

46. Consequently to imperfect conceptions respecting the Law of Mortality, and by an extraordinary exception in scientific proceedings, this matter of consideration has hitherto stood emancipated from all control of ruling principles; whilst embarrassed with denominations, either inappropriate or unmeaning. The reader must be dispensed from travelling over those rugged and unsteady paths, which may improve by the dismissal of barbarisms, such as EXPECTATION OF LIFE, and DECREMENTS; the former having been employed for expressing the measured intensity of life, understood in a collective sense, as shall hereafter be explained; and the latter having been unwarrantably used in the *plural*, to signify relative quantities of deaths occurring at successive years of age, and being mere deductions from the Law of mortality, but not its regulators. Let us however retain the denomination of DECREMENT, in the *singular*, collectively to express the decreasing series of survivors at periodic intervals, out of any quantity of births assumed to be simultaneous.

47. The *decrementum*, or *Decrement of life*, is a table deduced from the ascertained or assumed Law of mortality, for which it has not unfrequently been mistaken. It exhibits, by a progressively decreasing series, certain quantities of individuals who respectively outlive each year succeeding the birth, or outlive any other periodic interval, which

might be arbitrarily admitted instead of the annual interva usually understood. Of that series, the original term, denominated *radix*, expresses any quantity of births supposed to have taken place at the same instant; or in other words, any quantity of individuals entering upon their *first* year of age, — *i. e.* completing the year *zero*, — inasmuch as the preferable computation by annual periods is generally received; and from such original term of the series are produced all the others, in their due proportions of progressive reduction, according to a predetermined law.

48. If, instead of being annual, the periodic intervals could be discriminated *momently*, the Decrement would at the same time fulfil a second indication, being that of the quantities of individuals simultaneously existing at the ages represented by those successive periods, amongst the whole population, expressly understood to be stationary; as the quantity of periodic births would then exactly compensate and represent the periodic waste of life amongst the whole, in the same manner as each quantity of individuals, advancing one stage, would — by a difference from those who attained only the preceding — represent with similar accuracy such waste confined to individuals of ages further advanced. Under that hypothesis of a momently periodicity, the addition of all quantities successively stated in the decrement would further exhibit a total of permanent population, always supposed of stationary character; such total bearing a definite relation with the equal quantities of periodic births and deaths. But it follows from the admission of certain arbitrary periods, that the identity of the two series is disturbed; the quantity of survivors, as stated at the commencement of any one of those periods, not continuing to live throughout the next interval, which by a mere fiction is then supposed to be the case; whilst that fiction would become a reality, if momently intervals could be introduced in the stated decrement. Yet, as

regards any total amount of the quantities so stated, when the periodicity whatsoever is definite, — such amount compared with that of the relative population, or the living at all ages, — the former will invariably exceed the latter, by a quantity equal to *one-half* of the *radix*; whence and admitting annual intervals, as customary, a summation of the decrement shall represent in excess — of one-half the quantity of annual births or deaths (indifferently) — the amount of actual population.

49. In the same manner as the decrement represents successive quantities, y_0, y_1, y_2, $y_3 \ldots\ldots y_x$, of individuals completing the respective ages understood by x; the series of successive differences, Δy_0, Δy_1, Δy_2, $\Delta y_3 \ldots\ldots \Delta y_x$, represents the quantities of lives failing to complete the periodic term then entered upon. Whence the latter series also exhibits imperfectly the quantities of deaths, occurring amongst all individuals at various fractional ages, comprised between any two proximate and complete periods. But those implied inaccuracies, of representation, bear similar proportions in the two corresponding series; and $\Sigma \Delta y = y_0$ exceeds, by an invariable quantity $\frac{y_0 - y_1}{2}$, the total of deaths that occur at all fractional ages during the annual or any other period, the same as Σy exceeds by $\frac{y_0}{2}$ the exact quantity of population relative to the Radix.

50. The Decrement of life may, with reference to a stationary population, be geometrically illustrated to the eye. If on a line marked at equal distances (the *abcissa*), to represent periodic intervals, perpendicular lines (the *ordinates*) be raised at each of those distances; and if each of those perpendiculars be limited to elevations so proportioned, as to correspond with the quantities of individuals entering upon the different years of age, the junction of those succes-

sive limits will form an irregular curve, constantly inclining from the limit of the perpendicular representing the quantity of births, until it reaches the other line indicative of the ages; thus shewing, by its termination, the period at which all lives shall have dropt. This curve of mortality is not however of much practical use; but it has sometimes been set forth, especially by M. Duvillard *, as the means of solving various questions by geometrical process, the less important here to consider, as the solution could only imperfectly approximate the truth, consequently to physical limitations, with which the numerical mode of computation is unfettered.

51. The properties of the Decrement are manifold. In the first place it presents, without intermediate calculation, all the mathematical expressions of probability, that a life of any stated age shall endure throughout a further period also stated; thus enabling accurately to compute the values of life-annuities, and the present values of other sums depending on the contingencies of life or of survivorship. It next is the root of many useful deductions from the Law of Mortality, and which shall be noticed hereafter.

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* *Recherches sur les rentes, les emprunts, et les remboursemens.* Paris, 1787.

CHAPTER VI.

Of Life's intensity, *variously considered; as Absolute, Collective, and Specific.*

52. Life, or Vitality, is to be understood as an active power, inherent to its subject; and admitting such power to be measurable, it shall possess *intensity* in comparative degrees. A more convenient mode could not be found, of measuring the intensity of life, than by reference to some definite extent of time, during which the life is—or may be — carried on. But that intensity applies under different relations. Considered, first, as an average term of life, appertaining to the individuals of all ages who constitute any entire population or class selected from it, the intensity is then *Absolute*, expressing the precise measure of a *Generation*. Secondly, the average term may refer to such part only of that population, entire or select, as includes all individuals from any minimum of age upwards, exclusively of all others at inferior ages; and then the partly restrictive denomination of *Collective intensity* shall best apply; observing that a reference of the latter to an original period, namely that of the birth (when the exclusions amount to *zero*), will produce a coincidence of this with the former expression, as to quantity. Third and lastly, a *Specific intensity* of life is to be contradistinguished from the two preceding, as further restrictive; and in like manner expressing the quotient resulting from a division of that quantity only, who annually enter upon any specific year of age, by the corresponding quantity of those amongst them who fail to live throughout

the next periodic interval, which for distinctness we will continue to admit of one year.

53. Those several averages, or relative quotients, implied by the Absolute, the Collective, and the Specific intensities of life, are also to be understood as reciprocally expressing quantities annually renewed; either amongst the entire population, or select class of all ages, — amongst any part of the one or of the other, excluding those who exist at ages inferior to any conventional minimum, — or amongst such individuals, only, who of that population or class enter upon a stated year of age.

54. The respective subjects of those definitions will be best treated under distinct heads; after having noticed certain results peculiarly attendant on a progressive population.

CHAPTER VII.

Of the Contradistinguished effects produced by a Stationary and by a Progressive population.

55. Admitting always a Stationary population: it is consequent on the periodic substitution of any quantity of births, for an equal quantity of lives dropt at all ages during the last expired interval; and on the further substitution, in the detail, of individuals advancing from each year to the next in succession, for respectively equal quantities of reduction by deaths, amongst all who existed at the latter year of age and upwards; not only that the population should continue permanent as a total, but that, in its distribution into quantities of individuals existing at each age, all those fragments of population should also maintain invariable proportions between themselves and the whole. Nevertheless, the assumed stationary character is a mere fiction, indispensable towards accuracy in the calculations that rest on the Law of Mortality, and are required to proceed on undisturbed grounds; whence, and although no population continues absolutely stationary, such a law cannot be constructed without previously accommodating to that supposition the data supplied by actual observation.

56. In a progressive state of the population, whether increasing or decreasing, this supposed permanence of proportions becomes disturbed; as also is the relation, more or less approaching to identity, between the quantities exhibited by the decrement and those of the actually living at

corresponding years of age; the difference, in the latter respect, being only that the former are quantities of individuals entering on specific years, but all of whom do not outlive the next interval. In case of an increasing population, and according to the ratio of its progression, the altered distribution will produce a greater or less excess of population at the earlier ages, averaging a rate of mortality inferior to that of the whole; together with a corresponding deficiency of lives existing at more advanced years, and whose average rate of mortality is superior to the rate affecting the aggregate population. The contrary results will take place in case of a decrease; whence the Absolute intensity of life could, in neither the one nor the other case, obtain an expression from dividing the amount of population by the periodic births, nor by the periodic deaths; as the respective quotients, of those divisions, must diverge according to the greater or less elevated ratio of the progressive increase or decrease, and to the period elapsed since the commencement of either.

57. If it could be ascertained, *first*, that a nearly stationary population had at any time subsisted during a considerable number of years; *secondly*, that from such time, and during any subsequent period, the population had continued progressively increasing or decreasing; *thirdly*, the ratio of the annual increase or decrease; and *fourthly*, that, during the stated period of progression, the intensity of life had nevertheless continued invariably the same as before; all consequent modifications in the distribution of the increased or decreased population, either at the expiry of that supposed period, or at any previous term, would then be easily determinable. But those united data are scarcely to be obtained; and when, in their absence, any population is found considerably deviating from a stationary condition, the resort to hypothetical inductions may at best lead to uncertain results,

towards an approximate inference of the actual distribution of the population.

58. It is from not duly and correctly appreciating those distinctive circumstances, that many persons occasionally engaged in statistical discussions, but failing to consider this matter under its various aspects, have arrived at exaggerated conclusions, concerning the presumable improvement of vitality during the last half-century, or more protracted period; especially from having limited their consideration to the proportion between any quantity of population and that of the periodic deaths, exclusively of the births.

59. A progressive increase has the further effect of reducing the proportion of periodic marriages, compared with the quantity of population, — all other influent circumstances continuing the same, — because of the simultaneously increasing excess of individuals then existing at earlier than the marriageable ages; and that effect is reversed when the population decreases. A subsequent chapter, exemplifying the first of those instances, will afford occasion for enlarging on this effect concerning the relative quantity of marriages. And lastly it will be seen that a progressive state whatsoever, of any population, is not without effect on the average quantity of births to each marriage, as also on the proportion between the illegitimate births and the legitimate.

60. A decreasing population involves political evil; and the difference of results, in opposite cases, is considerable. Suppose two countries, at any time equally peopled; but such equality to be consequent, in the one, to a progressive increase, and in the other to a progressive and corresponding decrease. The former community shall possess, towards all advantageous purposes, a greater

number of productive members than the latter; and by reaction of the effect upon its cause, there shall also exist in the first a superior proportion of individuals at the ages most favourable for reproducing their species. The relative resources will therefore diverge more and more; whence any remarkably progressive increase or decrease of population must be admitted a principal sign of advancing or declining power, the ultimate consequences of which may with probability be anticipated.

61. All populations tend to increase, when not exposed by a troublesome neighbourhood to perpetual war, and when — not inhabiting an unproductive soil — they are neither permanently obnoxious to peculiar calamities, nor under the yoke of an unenlightened, unprotecting and oppressive government; amongst which disadvantages, those arising from the soil form the greatest obstacle, inasmuch as they altogether discourage from intermarrying and render marriages less fruitful, whilst other disadvantages may be either remedied or compensated for. The foresighted Dr. Franklin's earnest recommandation to his countrymen, at the origin of the American insurrection, was early marriage. But even under the most favourable circumstances, what should have been a blessing may become the curse of a country; and from a vicious principle introduced into the social system, multitudes may be born only to wretchedness. Agriculture is, almost every where, the main concern and leading occupation. An extensive subdivision of the soil best serves the general interest, from yielding a greater mass of produce; whence the adequate maintenance of a healthy, laborious and contented population; the numbers of which, instead of being burdensome, then form the real strength of a country. The contrary system exclusively favours the all-absorbing spirit of speculation, and a concentration of property, detrimental to the paramount interest of the community at large. Then of

the soil's produce, cultivated at less expense of manual labour, a greater proportion finds its way to market, for the exclusive benefit of the landlord and of the *gentleman-farmer;* but a smaller part is consumed on the spot, and a great proportion of unemployed population can only be supplied with the first necessaries at third or fourth hand. The interested supporters of such a system, unwilling to release their grasp, feign to ascribe the consequent evil to any other than its real cause. *Charity*, as it is called, is first tried for a palliative, in various shapes best disguising the selfish apprehensions from which it is wrung; whilst the miserable sufferers are *praised* for their patient submission to intolerable wrong. Desperate emigration, the next step, is preferably promoted, which deprives the community of its most valuable members; and depopulation, sinking a country in relative power and resources, will sooner or later be the ultimate result. A fit subject of taxation, to be substituted for other more oppressive of its branches, might be all land-tenements exceeding a certain extent and value combined; with a progressive scale.

62. Notwithstanding the invaluable advantages of an increasing population, under wholesome administration, such increase is naturally limited by the means of subsistence; but, long before these prove inadequate, the correctives of war and pestilence seldom fail to check the redundancy of numbers.

CHAPTER VIII.

Of Life's ABSOLUTE INTENSITY, *chiefly referred to a Stationary population.*

63. The expression of life's Absolute intensity, applied to an entire population or to any discriminated class, and resulting from a division of the living at all ages by the periodically returning quantity either of the births or deaths, — thus supposing the population to be stationary, — is an indicative feature, qualifying that population or class, comparatively with any other. It therefore possesses much statistical importance; a more elevated total of such relative population implying a better quality of lives, considered in the aggregate.

64. This total of the living does not however coincide with the sum of the successive quantities of the Decrement, which proceed from the election of an *annual* preferably to any other periodic interval, and represent the individuals *entering upon* each year of age. A perfect coincidence, in this respect, could take place but under a supposition of the shortest periodic intervals imaginable. Yet, as the difference amounts always to one-half of the radix, or quantity of annual births, according to what has already been stated in the 23^{d} paragraph; it will be sufficient, for obtaining a correct expression of the Absolute intensity, or number of years' average duration of life, to assume the sum of all terms of the decrement, — to divide that sum by the radix, — and to subtract half-unity from the quotient.

65 Any superior intensity, thus measured, of one population or class over another, without regard to difference of sex, is mostly derived from the circumstances attending early stages of life; for it is not so much the greater quantity of children actually born, under any standard of population, as the more considerable proportion of survivors, that contributes to render such population comparatively numerous. When infancy is subjected to unfavourable conditions of existence, no consideration of peculiar healthiness in advanced life, or of remarkable longevity amongst those attaining it, could afford adequate compensation for the curtailment resulting in any population, from either a deficiency of wholesome nutriment, or of preservative care, during the first few years of existence. In one country or district fully enjoying those advantages, though from other circumstances the rates of mortality became very elevated after traversing the meridian of life, the population that resulted from an equal quantity of periodic births might still be as *three* to *two*, compared with that of another country or district, in which infancy suffered under deprivation and neglect; notwithstanding that, from advantageous circumstances of soil and climate in the latter, the mortality proceeded at a very slow pace amongst the survivors, and that the observation of facts tended there to establish elevated probabilities of life's continuance during old age. The synoptic tables of mortality, collected in this volume, exhibit by their contrasted results, referred to Holland and to Montpellier, a remarkable instance of such very considerable difference produced by the above-mentioned causes, in the relative population.

66. It is every where acknowledged and confirmed by experience, that female life possesses, in the aggregate, a superior intensity to that of the male. If therefore an equal quantity of periodic births be supposed of each sex, in any community where both existed under similar circumstances, as far as the difference in their avocations may admit; the

relative quantity of female population shall more or less exeeed, at all times, that of the male sex; those eomparative quantities being permanent when the population is stationary. The difference indeed is such, that illustrating this remark by a refcrenee to the population of Franee at large, the quantity of females who periodieally complete their *eighteenth* year is already greater, in that country, than the quantity of males eompleting the same; after which year of age, the exeess of female survivors eontinues to inerease until an extremely advanced term of life; although it is ascertained that the male births oecur there, (at least for the present time,) in the superior proportion of *seventeen* eompared with *sixteen* births of the female sex. The male part of any population might however exceed in actual number the female, consequently to a still superior proportion of periodic births of the male sex.

67. But the measure of inequality, as to an Absolute intensity applying to the discriminated sexes, is not alike amongst eontradistinguished classes in any population, nor is it perfeetly alike between different aggregate populations; which in both cases depends on their relative qualities. The inequality is a *minimum*, when the population or selected class is characterized by the greatest superiority, and a *maximum* when the quality is most inferior; the variations taking place between 2 3/4, or perhaps less, and *four* years or more, of the Absolute intensities brought into comparison with each other. This is easily conceivable; as the more unfavourable to the preservation of life and of health may be the eonditions of existenee common to both sexes, the heavier must be the pressure of aeeumulated disadvantages falling to the lot of the male in partieular. It is in some degree probable, that the inequality of whieh we are speaking may be exclusively oeeasioned, in all cases, by the different though natural avocations of the respeetive sexes; and the admirable manner in which an equipoise is never-

theless maintained, by a corresponding excess of male births, shall be subsequently exemplified.

68. The Absolute intensity, once ascertained from a course of well-directed observations, becomes a foundation of the Law of Mortality, computable with reference to the entire population, the select class, or the distinct sex exclusively considered of its class. As it further implies an ascertainment of the relative total of such entire or partial population, compared with the periodic births and deaths understood to be compensated; the problem, remaining to be solved, is that of the corresponding decrement, and distribution of such total — or relative and permanent quantity of stationary population, — into respective quantities of the living at successive years of age. The final Decrement here alluded to, rectified and adjusted upon the definite principles hereafter set forth, may thus differ more or less in its details, from the provisional decrement produced in a crude state by actual experience.

69. The superiority of relative population, consequent on an elevated expression of life's Absolute intensity, has peculiarly remarkable effects with reference to individuals of the class more favoured than any other in social order. Their command of abundant gratifications, and of that salutary assistance which in the concerns of health is especially invaluable during infancy; together with their exemption from unwholesome employments, and possession of further privileges, obtain for them in ultimate result a very considerable advantage over all other classes, in respect to the quantity of survivors at mature age, out of a supposed equal quantity of births in each class. Of such survivors who attain their *fortieth* year, those amongst a superior class appear to be in the proportion of about *four* to *three*, compared with the survivors amongst the indiscriminate population either of England or France; and that advantage is even extended as *five* to

three, or thereabouts, when the comparison is made between the two extreme classes of individuals. Thus, and notwithstanding that the inferior class may contribute a rather superior proportion of births to each marriage, it occurs that the relative population, represented by the Absolute intensity of life, is considerably greater of the first class; and it becomes justly questionable, whether any observed increase of population should not be chiefly attributed to the classes which have the privilege of existing under a set of conditions especially favourable to the preservation of life and health at all years of age, nearly to the exclusion of an inferior class. Another consequence is, that great numbers amongst the progeny of the superior classes must be incessantly sinking into the inferior; which may sufficiently account, every where, but more particularly in this country, for the tenacious cagerness shewn by families advantageously circumstanced, to secure for themselves, and for their relatives in various degrees, a preference extending to monopoly of all profitable occupations depending on the gift of government; whether such preference be merited or not. When so doing, they merely obey a blind and irresistible impulse.

70. Inasmuch as the measure of Absolute intensity chiefly depends on that of the generally diffused comforts of life, as also more or less on the standard of moral character in any country, both of which may be susceptible of improvement; it should not pass unnoticed by the ruling powers. The expression of that intensity seldom differs materially between one civilized country and another, when referred to their aggregate and respective populations; because, with the exception of very few, there exists amongst them nearly a balance of their distributed advantages. The difference however is very considerable, as regards the extreme classes, contradistinguishable in every country; and this difference preferably results from the more or less advanced stage of early life, at which the *Specific* intensity, after having pro-

gressively increased from the period of the birth, turns to a decrease. Until a perfect development of the human frame, the vital principle is supplied in excess, over its consumption through the well-regulated excercise of our faculties; but this supply is liable to be prematurely arrested, consequently either to deprivation or to misuse. In an inferior class of the population, the Specific intensity commences to decrease even before the completion of a *tenth* year; which decrease does not take place until the *fifteenth* or *sixteenth*, in a superior class; and admitting nature's intentions to be better consulted than they usually are, whilst the human faculties, duly supported, were neither overwrought nor otherwise abused, the progressive increase would probably continue to the *twentieth* year; thus forming a more vigorous race.

71 It is demonstrable, under the same supposition, that life's Absolute intensity in the indiscriminate sexes might extend to 55 years, or more; which under the present circumstances is limited to 46 years or thereabouts, for the most favoured class, and is reduced to about 28 1/2 years for an inferior class still susceptible of reciprocal agreement, in pecuniary transactions founded upon the probabilities of life's continuance. According to that ratio of increased vitality, the quantity of births would be double that of the deaths during any equal interval of time; the population would also extend to the double of its original quantity, in less than 39 years, and be multiplied *five* times at the expiration of 90 years; admitting adequate means of subsistence, and all other influent circumstances to continue as before.

CHAPTER IX.

Of ascertaining life's Absolute intensity, when the population has continued progressively increasing or decreasing.

72. When a progressive state of the population, increasing or decreasing, has continued during an uncertain period, any consideration of the various means through which that population might resume its former equipoise could only embarrass the main question : *i.e*, how to rectify the data supplied by experience, of the periodic births and of the periodic deaths at distinct years of age, each referred to the disturbed proportions according to which the population is then distributed consequently to the circumstance of that progressive state; in order that such rectified data, in accordance with ascertained rates of mortality, may correspond with the stationary condition, to be assumed, though only fictitious.

73. The first step, towards this rectification, is to obtain a correct expression of life's Absolute intensity; being an intermediate term between the diverging quotients of the population, divided on one part by the annual births, and on another part by the annual deaths; dismissing the exclusive consideration of either. Those quotients may however be reserved; the one, stating a relation between the population and the births, as a comparative *minimum;* and the other, stating a corresponding relation with the deaths, as a comparative *maximum*, both to be understood in case of an increasing population; which implies the

converse in case of a decreasing population. The problem then stands as follows.

74. PROBLEM :: —

A population in progress of increase, from a doubtful period, is ascertained to consist in a quantity $\Sigma y - \frac{y_0}{2}$ of individuals at all ages; its exact distribution remains unknown, consequently to such increase having disturbed the original proportions; but a stationary population of equal amount, and liable to similar rates of mortality referable to the respective years of age, should be correctly represented by the decrement $y_0, y_1, y_2, y_3, \ldots y_x$; the radix of which, compared with the first-mentioned quantity, is :: 1 : n. The series $\frac{\Delta y_0}{y_0}, \frac{\Delta y_1}{y_1}, \frac{\Delta y_2}{y_2}, \frac{\Delta y_3}{y_3}, \ldots \ldots \frac{\Delta y_x}{y_x}$, expresses those rates, as actually understood with reference to each year of age immediately completed; but from the quantity of births being superior to that of the deaths during similar intervals, the latter series, representing the proportions of periodic deaths at the respective ages on the supposition of a stationary population, is so modified as to exhibit an inferior total, being :: 1 : m, when compared with $\Sigma y - \frac{y_0}{2}$. Amongst many independent causes, susceptible of opposing the coincidence of n with m, is, that in the eventual distribution, the quantity of lives at early ages, and collectively yielding a rate of mortality less than the general average $\frac{1}{m}$, are superabundant; whilst a decreasing population would have produced the contrary effect of their comparative deficiency, accompanied with a superabundance of lives at ages more advanced and yielding an average rate of mortality more elevated than $\frac{1}{m}$. Supposing that the population, at any future

time, resumed a stationary character, and maintained its equilibrium during a term of years sufficient for restoring the natural proportions of distribution now disturbed, this without regard to whatsoever operative causes producing such a result; and further admitting, as an essential condition, the general circumstances under which the population exists to continue unchanged, —whence the invariable preservation, throughout all that time, of the proportions between the quantities y_x and Δy_x respectively corresponding with each year of age signified by x, so as ultimately to realize the decrement as above; — the question is, in that case : What should be the coincident proportional fraction, superior to $\frac{1}{m}$, as also inferior to $\frac{1}{n}$, and expressing the quantity of annual births, become equal to that of the annual deaths, when both are compared with the relative quantity $\Sigma y - \frac{y_0}{2}$ of population?

75. The problem, thus reduced to its precise terms, appears insoluble by any direct means, in the absence of correct data establishing a definite period during which the population continued to progress, together with the progressive ratio, referred to the original and unobserved part of such period; but that problem may be solved by approximation in a satisfactory degree, consequently to inductions from the positive data supplied during the latter and experimental part of the same period; as will presently be seen.

76. During the supposed passage, from a progressive to a consolidated stationary state the comparative excess of youthful population must gradually diminish, and this single circumstance elevate above $\frac{1}{m}$ the proportion of annual deaths to the whole population; at the same

time as the proportion $\frac{1}{n}$, of annual births compared with that population relatively reduced from year to year, must by analogous gradation fall to an inferior standard; whence those fractional and diverging expressions must approach more and more, at each successive and periodic interval. Should indeed those two operations be produced by any combination of causes, concurring towards the assumed result of a stationary population, those causes must probably continue in a great measure under mutual dependance; and then the term of coincidence could not be remote from a geometric proportional between $\frac{1}{n}$ and $\frac{1}{m}$, if even this proved not an identical expression. But having assumed, as an essential condition, that the general circumstances of the population's existence would continue the same throughout the whole interval of time, whence the rates of mortality at specific years of age should also remain undisturbed; it follows that the conversion, from a progressively increasing to a stationary state, could not in such case be produced by any other than the single cause of a reduction in the periodic births; and the real question being not of any anticipated stationary state, which might partly arise from increased rates of mortality, but concerning a relation with the latter and fictive state to which an actually existing distribution of the population is to be reduced, the identity of the coincident term, with a geometric proportional between $\frac{1}{n}$ and $\frac{1}{m}$, may be considered as incontrovertible.

77. Discarding from consideration any other causes that might in some degree disturb this identity, though they escaped all research; there remains to ascertain whether or not the position obtains, by sufficiently extended experience, such confirmation as to warrant its admission on a general principle.

CHAPTER X.

Of life's Absolute intensity, ascertained on the foregoing principle, with reference to the indiscriminate population of France.

78. Periodic returns, concerning all movements of the French population, have long been established on a system capable of supplying efficient data towards the various objects of these researches; and for the last sixteen years, those returns have embraced additional details, which we shall hereafter find importantly available. Let us first compare, as regards the present question of life's Absolute intensity, the results of that experience for each year, distinctly considered, during a period of fourteen years, commencing with 1817 and terminating with the last returns, which are for 1830*.

YEARS.	POPULATIONS ascertained to correspond with the middle of each year respectively.	BIRTHS during each specified year.	DEATHS during each specified year.	QUOTIENTS of the population divided by the births.	QUOTIENTS of the population divided by the deaths.	GEOMETRIC proportionals between the two quotients.
1817	29 878 034	944 125	748 223	31·64627	39·93200	35·54854
1818	30 073 936	949 192	751 907	31·68372	39·99688	35·59846
1819	30 271 221	987 918	788 055	30·64157	38·41257	34·30768
1820	30 471 084	958 933	770 706	31·77603	39·53659	35·44463
1821	30 659 311	963 358	751 214	31·82546	40·81302	36·04016
1822	30 871 455	972 796	774 162	31·73477	39·87725	35·57380
1823	31 070 089	964 021	742 735	32·22968	41·83200	36·71828
1824	31 291 375	984 152	763 606	31·79526	40·97842	36·09598
1825	31 511 921	973 986	798 012	32·35369	39·48804	35·74321
1826	31 687 895	993 191	835 658	31·90514	37 91970	34·78266
1827	31 845 428	980 196	791 125	32·48884	40·25335	36·16330
1828	32 054 499	976 547	837 145	32·80385	38·26636	35·42999
1829	32 173 901	964 527	803 453	33·35718	40·04453	36·54823
1830	32 354 975	967 864	809 753	33 40859	39·93190	36·52492

* Those returns are published in an *Annual* issued by the Board of Longitude,

79. Were it not that those results, for each distinct year, must have been greatly influenced by lternations of abundant and deficient crops, as also of prevalent diseases and other passing events, the foregoing proportionals might have exhibited successive quantities nearly equalized, notwithstanding the variously diverging quotients respectively producing them, or otherwise exhibited a series uninterruptedly progressing by increase or by decrease; the former shewing that the Absolute intensity of life had continued the same, during the whole period observed upon, or the progressive series exhibiting by regular gradation the progress of that intensity's improvement or deterioration; and the general principle, set forth in the preceding chapter, would equally have found confirmation in either the one or the other case. In order therefore to neutralize, in some degree, the effects of accident; let us, under various points of view, consider those annual results as fragments only of other results, respectively founded upon more extended observation, and first compare the corresponding proportionals produced by *ten* periods, each embracing the experience of *five* consecutive years.

PERIODS.	UNITED populations of five years.	UNITED births during five years.	UNITED deaths during five years.	QUOTIENTS of the united populations by the united births.	QUOTIENTS of the united populations by the united deaths.	PROPORTIONALS between the corresponding quotients.
1817—1821	151 353 586	4 803 526	3 810 105	31·50879	39·72425	35·37880
1818—1822	152 347 007	4 832 197	3 836 044	31·52749	39·71462	35·38506
1819—1823	153 343 160	4 847 026	3 826 872	31·63654	40·07011	35·60449
1820—1824	154 363 314	4 843 260	3 802 423	31·87177	40·59604	35·97038
1821—1825	155 404 151	4 858 313	3 829 729	31·98727	40·57837	36·02763
1822—1826	156 432 735	4 888 146	3 914 173	32·00246	39·96572	35·76313
1823—1827	157 406 708	4 895 546	3 931 136	32·15304	40·04102	35·88093
1824—1828	158 371 118	4 908 072	4 025 546	32·26748	39·34152	35·62937
1825—1829	159 253 644	4 888 447	4 065 393	32·57755	39·17299	35·72338
1826—1830	160 076 698	4 882 325	4 077 134	32·78773	39·26297	35·87957

at Paris, and generally entitled to confidence. Opportunities of investigation, afforded to the writer of this volume, have enabled him however to rectify errors in the data there given for the year 1818, as will be perceived by a

80. Towards partly correcting the inconsiderable irregularities still apparent; let us further consider the results of *seven* united years, in each successive experiment:

PERIODS.	POPULATIONS	BIRTHS.	DEATHS.	QUOTIENTS by the births.	QUOTIENTS by the deaths.	PROPORTIONALS.
1817—1823	213 295 130	6 740 343	5 327 002	31·64485	40·04060	35·59579
1818—1824	214 708 471	6 780 370	5 342 385	31·66619	40·18963	35·67425
1819—1825	216 146 456	6 805 164	5 388 490	31·76212	40 11262	35·69401
1820—1826	217 563 130	6 810 437	5 436 093	31·94554	40·02197	35·75645
1821—1827	218 937 474	6 831 700	5 456 512	32·04729	40·12407	35·85900
1822—1828	220 312 662	6 844 889	5 542 443	32·18645	39·75011	35·76891
1823—1829	221 615 108	6 836 620	5 571 734	32·41589	39·77489	35·90736
1824—1830	222 879 994	6 840 463	5 638 752	32·58259	39 52648	35·88696

81. Taking another view of the matter, by comparing the results deduced from each year's experience combined with that of all preceding years, or comparing a series of generally averaged results; we find, —

PERIODS.	UNITED populations.	UNITED births.	UNITED deaths.	QUOTIENTS of the populations by the births.	QUOTIENTS of the populations by the deaths.	PROPORTIONALS.
1817.	29 878 034	944 125	748 223	31·64627	39·93200	35·54854
1817—1818	59 951 970	1 893 317	1 500 130	31·66505	39·96460	35·57357
1817—1819	90 223 191	2 881 235	2 288 185	31·31407	39·43003	35·13851
1817—1820	120 694 275	3 840 168	3 058 891	31·42943	39·45687	35·21515
1817—1821	151 353 586	4 803 526	3 810 105	31·50879	39·72425	35·37880
1817—1822	182 225 041	5 776 322	4 584 267	31·54689	39·75009	35·41175
1817—1323	213 295 130	6 740 343	5 327 002	31·64485	40·04060	35·59579
1817—1824	244 586 505	7 724 495	6 090 608	31·66375	40·15798	35·65884
1817—1825	276 098 426	8 698 481	6 888 620	31·74100	40·08037	35·66779
1817—1826	307 786 321	9 691 672	7 724 278	31·75782	39·84661	35·57304
1817 1827	339 631 749	10 671 868	8 515 403	31·82496	39·88439	35·62751
1817—1828	371 666 248	11 648 415	9 352 548	31·90702	39·73956	35·60858
1817—1829	403 840 149	12 612 942	10 156 001	32·01792	39·76370	35·68125
1817—1830	436 175 124	13 580 806	10 965 754	32·11704	39·77612	35·74200

comparison with those here set forth; and it is proper to observe, in addition, that the whole series of last returns, as stated in each Annual, remains subject to probable correction in the one next succeeding, consequently to a few *Departments* (*counties*) usually neglecting to send in due time their own quota; which partial returns are thence temporarily supplied through a method of approximation.

82. Either of the last three views goes much further, than the preceding and original one, to confirm the principle established in the foregoing chapter; inasmuch as the utmost difference, between any two quantities of each concluding series, is in those three cases very inconsiderable. The series of proportionals being generally progressive by increase, with insignificant deviations only, as resulting from the combination of fortuitous events, shew also that the intensity of life, in France, had scarcely discontinued improving at the close of the experiments; although the vacillating progression, observable in the latter terms of those concluding series, are one sign — amongst others — of an approaching discontinuance of such improvement. The various results, thus arrived at, give occasion to the following further remarks.

83. A constant decrease in the relative quantities of births, compared with the corresponding quantities of population at the stated periods, was naturally consequent on that population's progressing; whence arises, in its distribution, a constant increase of the included proportion of infants; such decrease of relative births being then referable to the same cause as that reducing the relative quantities of periodic marriages (for which see the 59th paragraph); besides which, as will hereafter appear, the average of births to each marriage has not increased, but rather the contrary. On the other hand, an equally observable increase — though inconsiderable — of the relative deaths, under a similar comparison, shews that the distribution of the actual population has, from the same cause, acquired some tendency towards the natural proportions referable to a stationary condition; the youthful, or collective part of population whose rates of mortality are inferior to the generally averaged rate, having of late years less and less preponderated.

84. The series of quotients, of the respective populations

divided by the corresponding quantities of deaths, has proceeded much more irregularly than the series of quotients resulting from a similar division by each corresponding quantity of births; which arises from the periodic mortality being always affected, by casualties, in a more considerable degree than the periodic births.

85. Leaving out of the question the opposite circumstances of emigration and of foreign settlers, an increase of population may take place, either by a greater number of periodic births, — by a reduced number of periodic deaths, — or by a combination of both; in the same manner as a decrease of population should be traceable to the reverse of those causes. Now it does not appear, by the foregoing statements, that the numerical increase of periodic births, in France, has contributed to that of its population, any more than in a very insignificant degree; whilst, on the contrary, the proportions of those births, to the population at the time being, has constantly diminished. At the same time, it appears that the periodic deaths have increased in quantities superior to those of the increased births, whilst the proportions which those deaths bear to the population have in a slight degree increased also; but as the latter proportions have still fallen considerably short of those according to which that population itself has continued increasing, it necessarily follows that the increased intensity of life in France, during the period observed upon, must be owing to an improvement in the general conditions of existence in that country, exclusively of any other cause, and especially to the exclusion of any small numerical augmentation in the quantities of annual births; part of which improvement is attributable to the cessation of war, and therefore affecting only the male sex.

86. From the middle part of those fourteen years' term of observation, the numerical quantities of population's increase,

and still more the proportions according to which that population has continued increasing to the present time, have been in progress of notable diminution; which indeed is accounted for, by the increase of periodic deaths having always, since that middle term, exceeded the increase of corresponding births. It may therefore be considered probable, that the Absolute intensity of French lives, in their aggregate, has at length attained its maximum of improvement, or thereabouts.

87. Let it lastly be remarked, that such improvement of the Absolute intensity, or of life's average duration in France, must in a great measure be attributed to consecutive good crops, at the same time as to an exemption from the calamities of war and of pestilence, during the whole period of the stated experience; and moreover, that the course of events, posterior to the last year's recorded births and deaths, will in all probability be found to have abated some portion of that absolute intensity, as latterly stated with reference to that country.

88. Failing the supply, from analogous observations in other extensive countries, of results corroborating those obtained relatively to the population of France, the latter appear fully confirmative of the general principle first set forth; *i. e.* that in case of any progressive population, whether the progression be increasing or decreasing, the Absolute intensity of life obtains a correct expression, by a geometric proportional between the respective quotients of the actual amount of such population, distinctly divided by the quantities of annual births and of annual deaths. Those present results further establish the measure of such Absolute intensity, or average term of life in France, as extending either to 35·87957, to 35·88696, or to 35·74200; according as were preferably admitted the average results of the last *five*, or of the last *seven* years' observations, or else the results so

averaged of the whole *fourteen* years during which they have hitherto been continued. No accurate conclusions could be drawn, in that respect, from an exclusive consideration of the results confined to any single year.

89. It were desirable that a complete experience had extended to distinct results, for the male and for the female sex. The data for 1817, and for all subsequent years, are in that respect satisfactory; but the previous census of population not having established the then existing quantities of each sex, their subsequent distinction is likely, during a further long period of years, to remain problematical; and the difference of life's Absolute intensity, contradistinguished for the male and for the female part of the French population, can at present be discovered only through indirect means.

90. The possessed data, aided with a few sufficiently warranted assumptions, may however be available towards ascertaining by approximation such difference of intensity. Let us first consider the French population, in the year 1817, as compounded of two parts, not very remote from equality; one part, by births in the proportion of 21 males to 20 females, referably to a former period, when that proportion was acknowledged; and another part, by births in a rather more elevated proportion of males, or that of 17 to 16 female births, as ascertained by an average of the last eighteen year's experience in the country to which we allude; whence its population, in the year 1817, may fairly be assumed to have originated in births of which 19 males to 18 females. Secondly, adverting to what has been stated in the 28th paragrah, (chapter III, concerning the increased intensity of life within a certain period,) let it further be considered that such compounded population possessed an intensity even superior to 32 years, as mentioned in that paragraph with reference to a now distant period,

yet inferior to that of 35·37880, as stated in the 79th paragraph to result from an average of the 5 years 1817 — 1821; whence we shall in all probability make a near approach to the truth, by admitting the french population, as formed in the year 1817, to have generally possessed 34 years' Absolute intensity of life. And thirdly, we shall be justified in introducing, as another element of computation, the difference of *four* years between that intensity for the discriminated sexes; because the operation of a destructive war, protracted during one quarter of a century, must necessarily have produced an inequality to that extent. From those assumptions, the population, as given for the year 1817, should have consisted of $\frac{29\,878\,034 \times 19 \times 32}{(19 \times 32)+(18 \times 36)} = 14\,463\,252$ Males, and of $\frac{29\,878\,034 \times 18 \times 36}{(19 \times 32)+(18 \times 36)} = 15\,414\,782$ Females. Thence establishing the population of each sex, for every succeeding year, by adding to those respective quantities the ascertained excesses of the births over the deaths, from year to year, the following sets of comparable results are obtained.

91. Results of each year's individual experience:

MALE SEX.

YEARS.	POPULATIONS	BIRTHS.	DEATHS.	QUOTIENTS of the population, by the births.	QUOTIENTS of the population, by the deaths.	PROPORTIONALS.
1817	14 463 252	488 457	382 813	29·61009	37·78151	33·44718
1818	14 568 896	488 978	376 412	29·79451	38·70464	33·95863
1819	14 681 462	509 311	398 260	28 82612	36·86401	32·59826
1820	14 792 513	494 378	389 822	29·92147	37·94684	33·69609
1821	14 897 069	497 621	377 062	29·93657	39·50827	34·39102
1822	15 017 628	501 094	391 443	29·96968	38·36479	33·90841
1823	15 127 279	496 517	376 101	30·46679	40·22132	35·00592
1824	15 247 695	507 770	385 785	30·02875	39·52381	34·45070
1825	15 369 680	503 532	400 444	30·52375	38·38160	34·22792
1826	15 472 768	511 898	419 613	30·22627	36·87390	33·38503
1827	15 565 053	505 307	399 864	30·80316	38·92587	34·62715
1828	15 670 496	501 669	421 956	31·23673	37·13774	34·05967
1829	15 750 209	496 163	405 366	31·74401	38·85430	35·11968
1830	15 841 006	496 997	408 558	31·87345	38·77296	35·15435

FEMALE SEX.

YEARS.	POPULATIONS	BIRTHS.	DEATHS.	QUOTIENTS of the population, by the births.	QUOTIENTS of the population, by the deaths.	PROPORTIONALS.
1817	15 414 782	455 668	365 410	33·82898	42·18490	37·77660
1818	15 505 040	460 214	375 495	33·69093	41·29228	37·29846
1819	15 589 759	478 607	389 795	32·57319	39·99477	36·13531
1820	15 678 571	464 555	380 884	33·74966	41·16364	37·27276
1821	15 762 242	465 737	374 152	33·84365	42·12792	37·75927
1822	15 853 827	471 702	382 719	33·61196	41·42681	37·31536
1823	15 942 810	467 504	366 634	34·10198	43·48427	38·50843
1824	16 043 680	476 382	377 821	33·67819	42·46373	37·81668
1825	16 142 241	470 454	397 568	34·31201	40·60243	37·32494
1826	16 215 127	481 293	416 045	33·69076	38·97446	36·23643
1827	16 280 375	474 889	391 261	34·28248	41·61001	37·76896
1828	16 364 003	474 878	415 189	34·45938	39·41338	36 85324
1829	16 423 692	468 364	398 087	35 06609	41·25654	38·03558
1830	16 493 969	470 867	401 195	35·02893	41·11210	37·94882

92. The average results of each Five consecutive years' experience will be :

MALE SEX.

YEARS.	POPULATIONS	BIRTHS.	DEATHS.	QUOTIENTS of the population, by the births.	QUOTIENTS of the population, by the deaths.	PROPORTIONALS.
1817—1821	73 403 192	2 478 745	1 924 369	29·61304	38·14491	33·60925
1818—1822	73 957 568	2 491 382	1 932 999	29·68536	38·26052	33·70129
1819—1823	74 515 951	2 498 921	1 932 688	29·81924	38·55560	33·90721
1820—1824	75 082 184	2 497 380	1 920 213	30·06438	39·10096	34·28624
1821—1825	75 659 351	2 506 534	1 930 835	30·18485	39 18478	34·39166
1822—1826	76 235 050	2 520 811	1 973 386	30·24227	38·63160	34·18051
1823—1827	76 782 475	2 525 024	1 981 807	30·40861	38·74367	34·32406
1824—1828	77 325 692	2 530 176	2 027 662	30·56138	38·13539	34·13898
1825—1829	77 828 206	2 518 569	2 047 243	30·90176	38·01611	34·27484
1826—1830	78 299 532	2 512 034	2 055 357	31·16978	38·09534	34·45900

FEMALE SEX.

YEARS.	POPULATIONS	BIRTHS.	DEATHS.	QUOTIENTS of the population, by the births.	QUOTIENTS of the population, by the deaths.	PROPORTIONALS.
1817—1821	77 950 394	2 324 781	1 885 736	33·53020	41·33685	37·23375
1818—1822	78 389 439	2 340 815	1 903 045	33·48809	41·19157	37·14064
1819—1823	78 827 209	2 348 105	1 894 184	33·57056	41·61538	37·37716
1820—1824	79 281 130	2 345 880	1 882 210	33·79590	42·12129	37·72966
1821—1825	79 744 800	2 351 779	1 898 894	33·90829	41·99540	37·73582
1822—1826	80 197 685	2 267 335	1 940 787	33·87678	41·32225	37·41476
1823—1827	80 624 233	2 370 522	1 949 329	34·01117	41·35999	37·50602
1824—1828	81 045 426	2 377 896	1 997 884	34·08283	40·56563	37·18321
1825—1829	81 425 438	2 369 878	2 018 150	34·35849	40·34658	37·23235
1826—1830	81 777 166	2 370 291	2 021 777	34·50090	40·44817	37·35637

93. The average results for each SEVEN consecutive years will be:

MALE SEX.

YEARS.	POPULATIONS	BIRTHS.	DEATHS.	QUOTIENTS of the population, by the births.	QUOTIENTS of the population, by the deaths.	PROPORTIONALS.
1817—1823	103 548 099	3 476 356	2 691 913	29·78639	38·46636	33·84929
1818—1824	104 332 ,542	3 495 669	2 694 885	29·84623	38·71502	33·99251
1819—1825	105 133 326	3 510 223	2 718 917	29·95062	38·66735	34·03103
1820—1826	105 924 632	3 512 810	2 740 270	30·15382	38·65482	34·14075
1821—1827	106 697 172	3 523 739	2 750 312	30·27953	38·79456	34·27363
1822—1828	107 470 599	3 527 787	2 795 206	30 46403	38·44819	34·22406
1823—1829	108 203 180	3 522 856	2 809 129	30·71462	38·51841	34·39590
1824—1830	108 916 907	3 523 336	2 841 586	30·91292	38·34831	34·43048

FEMALE SEX.

YEARS.	POPULATIONS	BIRTHS.	DEATHS.	QUOTIENTS of the population, by the births.	QUOTIENTS of the population, by the deaths.	PROPORTIONALS.
1817—1823	109 747 031	3 263 987	2 635 089	33·62360	41·64831	37·42147
1818—1824	110 375 929	3 284 701	2 647 500	33·60304	41·69062	37·42903
1819—1825	111 013 130	3 294 941	2 669 573	33·69199	41·58460	37·43085
1820—1826	111 638 498	3 297 627	2 695 823	33·85433	41·41183	37·44289
1821—1827	112 240 302	3 307 961	2 706 200	33·93035	41·47524	37·51359
1822—1828	112 842 063	3 317 102	2 747 237	34 01826	41·07475	37·38036
1823—1829	113 411 928	3 313 764	2 762 605	34·22450	41·05254	37·48337
1824—1830	113 963 087	3 317 127	2 797 166	34·35598	40·74234	37·41314

94. And the results of each year's experience combined with that of all preceding years :

MALE SEX.

YEARS.	POPULATIONS	BIRTHS.	DEATHS.	QUOTIENTS of the population, by the births.	QUOTIENTS of the population, by the deaths.	PROPORTIONALS.
1817	14 463 252	488 457	382 813	29·61009	37·78151	33·44718
1817—1818	29 032 148	977 435	759 225	29·70238	38·23919	33·70156
1817—1819	43 713 610	1 486 746	1 157 485	29·40220	37·76602	33·32272
1817—1820	58 506 123	1 981 124	1 547 307	29·53178	37·81158	33·41621
1817—1821	73 403 192	2 478 745	1 924 369	29·61304	38·14491	33·60925
1817—1822	88 420 820	2 979 839	2 315 812	29·67302	38·18134	33·65941
1817—1823	103 548 099	3 476 356	2 691 913	29·78639	38·46636	33·84929
1817—1824	118 795 794	3 984 126	3 077 698	29·81729	38·59891	33·92513
1817—1825	134 165 474	4 487 658	3 478 192	29·89655	38·57389	33·95879
1817—1826	149 638 242	4 999 556	3 897 755	29·93031	38·39088	33·89765
1817—1827	165 203 295	5 504 863	4 297 619	30·01043	38·44066	33·96499
1817—1828	180 873 791	6 006 532	4 719 575	30·11285	38·32416	33 97131
1817—1829	196 624 000	6 502 695	5 124 941	30·23731	38·36610	34·06006
1817—1830	212 465 006	6 999 692	5 533 499	30·35349	38·39614	34·13879

FEMALE SEX.

YEARS.	POPULATIONS	BIRTHS.	DEATHS.	QUOTIENTS of the population, by the births.	QUOTIENTS of the population, by the deaths.	PROPORTIONALS.
1817	15 414 782	455 668	365 410	33·82898	42·18490	37·77660
1817—1818	30 919 822	915 882	740 905	33·75962	41·73251	37·53497
1817—1819	46 509 581	1 394 489	1 130 700	33·35242	41·13344	37·03916
1817—1820	62 188 152	1 859 044	1 511 584	33·45168	41·14105	37·09767
1817—1821	77 950 394	2 324 781	1 885 736	33·53020	41·33685	37·23375
1817—1822	93 804 221	2 796 483	2 268 455	33·54364	41·35160	37·24356
1817—1823	109 747 031	3 263 987	2 635 089	33·62360	41·64831	37·42147
1817—1824	125 790 711	3 740 369	3 012 910	33·63057	41·75058	37·47126
1817—1825	141 932 952	4 210 823	3 410 478	33·70670	41·61672	37·45347
1817—1826	158 148 079	4 692 116	3 826 523	33·70506	41·32945	37·32307
1817—1827	174 428 454	5 167 005	4 217 784	33·75814	41·35547	37·36421
1817—1828	190 792 457	5 641 883	4 632 973	33·81716	41·18143	37·31808
1817—1829	207 216 149	6 110 247	5 031 060	33·91290	41·18737	37·37270
1817—1830	223 710 118	6 581 114	5 432 255	33·99274	41·18182	37·41500

95. Those series of geometric proportionals, resulting from an application of the data to each discriminated sex, go still further to confirm the principle first advanced; that, generally, such proportional between the quotients of the existing population, separately divided by the periodic births and by the periodic deaths, exhibits the Absolute intensity of life; and this proves equally true, with regard to either sex in particular, as with regard to the indiscriminate sexes in a whole population. If again that Absolute intensity be considered at the close of those fourteen years' experience; it is perceived to be 34·45900 years for the *male* sex, whilst extending to 37·35637 for the *female*, when considered on an average of the last *five* years; as also to be 34·43048 years for the *males*, and 37·41314 for the *females*, on an average of the last *seven* years' results; and lastly to be 34·13879 years for the *males*, and 37·41500 for the *females*, on an average of the last *fourteen* years, or of the whole period observed upon; whilst the results for the very last year, or for any other specific year of that period, should be disregarded, as having too much depended on fortuitous events.

96. But those sets of comparative series further convey information on other points. First, it is seen that the increased intensity of life, during the considered period, belongs almost exclusively to the male sex, with scarcely any participation of the female; consequently to which, the difference between their respective intensities, and assumed to be of *four* years during the circumstances of war, has been reduced to about *three and a half* on an average of the first nine years of the experience, or from the commencement of 1817 to the end of 1825, as also latterly reduced to *three* years only, according to an average of the seven years 1824—1830, both inclusive; and indeed our hypotheses, in the 90th paragraph, are justified by the harmony of those results. The intensity of female life appears, however, to have augmented in the first instance, and afterwards to have declined; whilst the gradual

augmentation of the male intensity proved constantly progressive. Secondly, the relative quantities of periodic deaths, referred to the population of each respective sex at the time being, continued only fluctuating, as to the males, without sensible difference between the results at the commencement and termination of the whole experience, though generally increasing with regard to the females; whilst the quantities of periodic births, also relative to the population at the time being, have regularly decreased in both sexes, which is naturally consequent on such population's progressing by increase, as already mentioned. Third and lastly, the excess of periodic births over the periodic deaths, or the periodic increase of numerical pupulation, has constantly proved more considerable for the male than for the female sex; consequently to which, and during the 14 years observed upon, the former have increased by 1 466 193, whilst the latter by 1 148 859 only (*); and allowing for 16 females born to 17 males, within any given time, the comparative excesses, of the births over the deaths, have been generally as six to five in favour of the latter sex. Whence it occurs that the excess of female population over the male, which was 951530, for the year 1817, has been reduced to 634196 at the expiration of the year 1830; quantities failing however to be possessed of the desirable accuracy, inasmuch as the respective populations, male and female, have not, for the first of those years, been stated without the aid of a few assumptions, probably approaching very nearly to the truth; which is left for the judgment of the reader either to admit or to reject, until better information may be obtained. It is not unlikely that this comparative increase, of male births, might be traced to a cause hereafter explained in chapter XXI.

(*) Inclusive of a last increase, during the year 1830.

CHAPTER XI.

Of Life's Absolute intensity in England, inferable on the foregoing principle.

97. Without repeating what has been said in the 30th and subsequent paragraphs, relatively to the contradictory character of all data supplied by the official returns in England; it will be sufficient, for shewing the impossibility of drawing any satisfactory conclusion from them, to compare their results referred to the *forty* counties, as stated in Mr. Rickman's recent publication, page 31. We thus have the expressions hereafter, of life's Absolute intensity, as brought out by those returns.

FOR PERIODS of TEN YEARS EACH.	QUOTIENTS of THE POPULATION, divided by the baptisms.	QUOTIENTS of THE POPULATION, divided by the burials.	PROPORTIONALS, or inferable INTENSITIES.
			years.
1790 to 1800	36	48	41·5635
1800 to 1810	34	51	41·6255
1810 to 1820	35	57	44·6655
1820 to 1830	37	54	44·6990

98. The author has stated on that occasion, and from the same source, corresponding data referred to the county of Essex in particular; being as follows, and included in the above: —

FOR PERIODS of TEN YEARS EACH.	QUOTIENTS of THE POPULATION, divided by the baptisms.	QUOTIENTS of THE POPULATION, divided by the burials.	PROPORTIONALS, or inferable INTENSITIES.
			years.
1790 to 1800	35	44	39·2428
1800 to 1810	34	46	39·5324
1810 to 1820	36	60	46·4758
1820 to 1830	37	54	44·6990

99. But we are further supplied by him (page 34th) with the results of some independant observations, respecting the population of that county, and embracing a period of 18 years, to 1830 inclusive; from which has been constructed a table of mortality, exhibiting no more than 34·4646 years' Absolute intensity of life, throughout Essex. It need only be said, in addition to the remarks regarding that specific table and stated in our 33d, 34d and 35th paragraphs, that the latter result, in all probability, comes much nearer to the truth, as expressing the intensity of life at present throughout England, than any of the results that proceed from official returns corresponding with the same period. Further there does not appear any satisfactory grounds of inference, that such intensity, in England, were even in the smallest degree superior to that which has been deduced from authentic and incontestable data relative to the indiscriminate population of France; although a mere glance at those returns may possibly have led to that erroneous conclusion.

CHAPTER XII.

Of Life's COLLECTIVE INTENSITY, *contradistinguished from the* ABSOLUTE.

100. Limiting our view to such part only of the population as may have either attained or surpassed any specific year of age, the measure of vitality, collectively belonging to that selection among the whole, is expressible by a quantity of years, being the average term of their lives' further endurance; in the same manner as the *Absolute* intensity is expressed with reference to the population at all ages, whether indiscriminately of a whole country, or only of a particular class. Hence an indentity of the *Absolute* and of the *Collective* intensities of life, when the latter applies to the birth, or completed year *zero;* which, in that case, is the understood minimum of age, referred to such collection of individuals.

101. The Collective intensity, likewise denoting a quantity of population annually renewed, or measuring a *generation* under this limited view, would be correctly expressed by the quotient of those considered individuals, divided by the relative radix, being a quantity of individuals annually attaining the understood minimum of age (in other words *borne* or *born* to that age); if the former quantity were correctly to be represented by a summation of the decrement, from such radix inclusively. But in consequence of the successive quantities, there stated, representing always in excess those lives which actually exist of all fractional ages intervening between any two proximate and completed years

generally signified by x, as already explained in the 64th paragraph; it is neccssary to subtract *half a year* from the above-mentioned quotient, in order to obtain a correct expression of this intensity, when such total of quantitics stated in the decrement is admitted for a dividend.

102. The intensity thus described and generally signified by m, with refcrencc to each completed year of age successively understood as a minimum, forms a scries m_x, relative to the corresponding terms of thc decremcnt. The lapse of cvery succeeding year might naturally lead to infer an invariably progrcssivc decrease in those average of forthcoming years; whereas that series proceeds on the contrary by increase during the first few years of life. This is because the rates of mortality considerably preponderate at such very early ages, the lives becoming more and more consolidated as they happcn to have survived those few succcssive intervals; and it is only after those rates have ceased remarkably to dccrease from each year to thc next, that the Collectivc intensity also commences decrcasing. Its maximum refers to an age varying no more than between the fourth and sixth completed years; which term, uninfluencccl by differencc of sex, appears to occur rather sooner in case of a superior quality of the considered lives; thc relative quantity of survivors, then possessed of greater Specific intensity of lifc, being the most considerable in that case. Sussmilch's tables of mortality for the population of Brandcnburgh, and those of Dr. Halley for the population of Breslaw, may bc quoted as affording exceptions to this rule, both referring that maximum to *seven* years of age; but those tables, bcsides their irregular construction, have proceeded from observations in many rcspect deficient, owing to thc causcs noticed in thc 12th, 13th and 14th paragraphs. Mr. Finlaison's tables exhibit another and indced more singular exception of this kind; as they admit not, at any stage of life, the increase of its

Collective intensity. An investigation of his tables is however reserved for a separate chapter.

103. The intensity considered in the above point of view has the more inappropriately been denominated "*Expectation of Life*", as it fails either to express or to imply any specific probability; whilst the "*Equation of Life*", to be treated of in the next chapter,—and expressing, with reference to any given age, the further term of years which there is an equal probability of outliving or not,—may the more justly be admitted for the *true Expectation*, as the probability of life's continuance, to that precise term, is greater than that of its terminating either at any earlier or at any later period.

104. Demoivre, Simpson, and since their time other Bristish authors, have variously applied the series m_x, towards obtaining, by abridged methods, the solution of questions concerning the values of sums depending on lives and on survivorships; but the results mostly consist of approximations, sometimes remote, and yet considered practically useful when greater accuracy is not required. The nearer approach to correct results is obtainable, by that means, when the lives or population are of an inferior description; as the numerical quantities of periodic deaths differ less, from any year of age to any other, in that case, than in the case of a superior quality of lives.

105. The Collective intensity may further apply to the joint-continuance of two or more lives, as also to the life of an eventual survivor; whether the stated lives be of similar or of different description, in respect to age, to class, and to sex. Its consideration may then be attended with greater practical utility, than when the view of that intensity is limited to single lives; and the more so, as a tolerable approach to correct results is, in the former of those cases, all that may rationally be expected.

106. To ascertain this intensity, or average duration of joint-life, which we will suppose limited to two individuals; let the Decrement applicable to each, according to their class and sex, be proportioned to a common radix referable to their respective ages, however different; and multiplying into each other the corresponding two terms of those decrements, for such and every succeeding year of age, a third decrement will arise, exhibiting the proportions according to which the original quantity of couples should gradually become disunited. This last decrement will retain, as regards the joint-lives, all the properties attributable to that of individual life; and the various conclusions are to be drawn in the same manner, from the one as from the other, especially all those relative to questions concerning probability. Should the two lives be of similar age, class, and sex, the process will then be simplified by multiplying into itself each term of the common decrement; and if, being of the same class and sex, the ages differed only by a few years, it might be sufficient, towards a certain degree of approximation, to proceed as already said and admitting an average between the two ages, provided that neither were less than twelve or fourteen years.

107. For an eventual survivor, the average term of forthcoming years is immediately deducible from the averages ascertained for each individual life, as also for the joint continuance; and the latter being an assignable term of the shorter life, the term which should be assigned to the longer obviously amounts to the united averages of the former two, *minus* the average belonging to the latter, or $m + m' - M$; since, taken together as described, they must in all cases be supposed to contemplate an equal quantity of those reunited and future years of life.

CHAPTER XIII.

Of the EQUATION OF LIFE.

108. The Equation of life, or term of forthcoming years which there is an equal probability of being attained or not, by the individual of a stated age, may be generally expressed by n_x; and is immediately deducible from the appropriate Decrement, according to the sex and class. Should it be required thus to ascertain any extent of future years, most probably attributable to an individual life of the specific age x; that extent n_x, as determined in the next paragraph, shall be the correct expression, differing more or less from $\dot{m}_x$, or the average duration; which difference, at certain ages, may be relatively considerable.

109. It follows from the Decrement's definition, that departing from any one of its terms, or quantity expressed by y_x, any subsequent term $y_{x+n} = \frac{y_x}{2}$ must indicate the year of age more probably attainable than any other; as, at the age $x + n$, there shall survive exactly one-half of the individuals existing of the age x; whence the probabilities are equal, for any one of them, to be amongst the number of the living or of the dead, at that future period. A single glance at the decrement would point out that period $x + n$, if this were expressible otherwise than by a fractional quantity of years; but it will be almost always intermediate between two proximate years of age, $x + n - f$ and $x + n + 1 - f$; leaving f, or the accompanying fraction,

to be ascertained by calculation; and thus $y_{x+n-f} - y_{x+n} : y_{x+n-f} - y_{x+n+1-f} :: f : 1$, whence $f = \frac{y_{x+n-f} - y_{x+n}}{y_{x+n-f} - y_{x+n+1-f}}$.

110. That such determination, of the accompanying fraction of a year, were perfectly correct, would require the rates of mortality to be exactly the same for all equal intervals during the two completed years $x + n - f$ and $x + n + 1 - f$; but this could only arise from supposing equal rates referred to those two proximate years of age. Assuming however the difference of those rates to be inconsiderable, an ascertainment of f, as above, will make the nearest approach to utmost accuracy which is likely to be requisite for any practical purpose. When $x + n$ refers to a very advanced age, those rates, probably, will so much differ as to require consideration; and then resort may be had to an arbitrary correction of the fraction f, which otherwise must be rather too small, in proportion as it approaches towards *unity* (*).

111. When referred to the birth and to an indiscriminate population, the Equation of life may represent a shorter term of years than the average of its further endurance, or the expression of Collective intensity; and especially regarding the male sex of an inferior class, the two expressions may thus differ considerably. But in case of a select class, n_0 shall always be found superior to m_0; because the elevation of the former quantity chiefly depends

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* To obviate any apparent inconvenience of this kind, but indeed of little consequence, would require entering upon calculations the labour of which must be disproportionate to their object. But in case of need, the formulæ for obtaining either n_x or m_x, with perfect accuracy, are to be found in Duvillard's work: — "*Recherches sur les rentes, les emprunts, et les remboursemens*".

on the slow progress of the decrement in early life. With the single exception of a reference to the first year of existence, and for a long series of subsequent years, the Equation of life in all cases exceeds more or less its Collective intensity. The period of the latter's commencing to preponderate, after which it retains the superiority in a constantly increasing proportion, depends on the distinctions of class and of sex. That period take places at 44 completed years, for the male sex, and at 50 for the female, when both belong to a superior class of selection; at 36 years for the male, and at 44 for the female, of a class subject to conditions of existence less favourable than those affecting the indiscriminate population; and as regards the latter, exemplified by that of France, at 44 years for the male, and at 48 for the female sex. From those considerations, it becomes important to avoid mistaking the average term of any life's further endurance, for the Equation of such life, especially at advanced age.

112. The Equation referred to Joint-lives is determinable through a combinaison of their respective decrements, as mentioned in the 106th paragraph; but that of the longest life, or equation referable to an eventual survivor, requires a special process for its ascertainment. After ascertaining N, or the most probable term of any two lives' joint-continuance, the survivor having at its expiry attained the age $x + \mathrm{N}$, a further lapse of time n', required according to the greatest probability, for reducing any quantity of the living at the age $x + \mathrm{N}$ to precisely one-half of that quantity or to $\frac{\gamma_{x+\mathrm{N}}}{2}$, will be indicated by the Decrement relative to such single life of the stated age and sex; whence $\mathrm{N} + n'$ shall be the most probable term of life's forthcoming years, for that supposed survivor, presently existing at the age x. A similar process, supposing the other life to be of a different

description and aged x', will determine a corresponding term of its most probable endurance beyond N, or carrying such life to an age $x' + N$. Thus in case of marriage, or of any other life-association between two individuals, the value of a contingency, depending either on the dissolution of such association or on the extinction of both lives, under the one as well as the other supposition of survivorship, shall become susceptible of ascertainment, with sufficient accuracy for all practical purposes.

CHAPTER XIV.

Of the DISTRIBUTED POPULATION, *supposed stationary, and its relative quantity inferable from the Decrement.*

113. In a foregoing chapter, where the Decrement of life and various properties of that series are described, it has been shewn that the total quantity of any population supposed stationary, together with its distribution into quantities of the living at different years of age, respectively bear invariable relations to the quantity of births periodically compensating for the deaths; and it has further been shewn, that the quantities successively expressed by y_x, of survivors completing each year of age and entering upon the next, are in constant excess of one-half the difference between the two proximate quantities y_x and y_{x+1}, over the real quantity of the living at various intervals of age from x to $x+1$ respectively completed years. From those considerations, it is easy to deduce another decreasing series z_x, that shall exhibit the collective quantities of the living at all ages, exclusively of those only who may not have completed the year of age signified by x; hence and by immediate inference, the collective quantities also of the living between any interval of age whatsoever.

114. The method of that deduction is simple, and requires no further elucidation than to observe that the successive differences, between each term and the next of the series z_x, shall correctly represent the quantities of individuals actually living at various intervals of age, from

x to $x+1$; as also those differences will form another series Δz_x, corresponding with and modifying the series y_x, or decrement of the living.

115. That series z_x constitutes a permanent Law of the distributed and relative population, assumed to be stationary. But supposing any other population in progress either of increase or of decrease, through in quantity bearing similar relation with a geometric proportional between the periodic quantities of births and of deaths, which implies an equal measure of the Absolute intensity of life between those supposed populations; the above-mentioned equipoise of distribution will be more or less disturbed in the latter case, according to the periodic ratio of such progression, and to the term elapsed since its commencement, as already explained in the 56th and 57th paragraphs. Two populations however might exist, possessing an equal measure of life's Absolute intensity; yet such equal measure arising from different elementary quantities of the relative births and of the relative deaths, which yielded a proportional common to both populations; but in that case, neither could the law of distribution be exactly the same, nor the Specific intensities be alike at each corresponding year of age; and the respective circumstances, or conditions of existence, would be more or less different in the detail, notwithstanding that the advantages and disadvantages of those circumstances exhibited an equal balance in their aggregates.

116. What has been stated in the two preceding chapters, relatively to the consideration of joint-lives, implies an extention of the principles there stated to a series Z_x; which shall indicate a law of the distributed population, supposed to consist of *couples*, substituted for individuals, such as might result from a corresponding decrement $Y_x = y_x^2$.

CHAPTER XV.

Of the Relative quantities of Deaths at successive years of age, as represented by a series of differences between the terms of the Decrement.

117. The series Δy_x, expressing any relative quantities of deaths that may occur at successive years of age, in a stationary population, has so often been mistaken for the Law of Mortality, as to require the characteristics of that series to be presented under a distinct head. Indeed the leading principle, upon which some received mortality-tables appear to have been constructed, consists in a certain arbitrary adjustment of those successive quantities of deaths, in nearly arithmetic progression, and not unfrequently admitting even their continued recurrence in equality; whereas the ultimate appearence of any regular progression, in that series Δy_x, whether increasing or decreasing, should be only a secondary result of the fundamental law, regulating in the first instance,—and not without due regard to physiological considerations among the rest, —a series expressive of life's Specific intensity corresponding with each year of age; the series y_x, or *Decrement*, being its primary result.

118. A distinguishing character of the Law of Mortality, applicable to a superior class of selection, which class is announced by an elevated ratio of life's Absolute intensity, is to establish a greater numerical disproportion between the *maximum* of periodic deaths, and their *first minimum* occurring at an early age, when the Specific intensity of life has attained its *maximum*; whilst in case of an inferior class, or of any entire population existing under unfavourable conditions, either of which will be marked by a depressed

ratio of that intensity, such numerieal disproportion may be only ineonsiderable. If that *first minimum* should be elevated, whilst the *maximum* quantity of deaths oecurring at any speeifie year of age should be reduced, thus making a greater approaeh to equality in the suecessive terms of the series Δy_x, an essential indieation will thereby be afforded, of inferiority in the eonditions under which may exist the entire or else the partial population yielding those results.

119. The superior or the inferior quality of any population, or diseriminated class, is further marked; the former, by more advaneed periods at which the depressed first minimum, as also the elevated maximum of numerical deaths, take plaee; and the latter quality, on the contrary, by earlier periods that admit the respective *max.* and *first min.* whatsoever of those deaths. Exemplifying those remarks, aceording to various modifieations of the law of mortality whieh it has been a chief purpose of this work to eonelude and apply to five different elasses of each sex; and referring each modification to a common radix of *one million* supposed annual births, eompensating for an equal number of annual deaths, we find: —

	FIRST CLASS, or Perfect lives.	SECOND CLASS, or Life-annuitants.	THIRD CLASS, or Assurable lives.	FOURTH CLASS, or the indiscriminate population.	FIFTH CLASS, or Inferior lives.
			MALES.		
Minimum of deaths, and corresponding age.....	2692 at 14 years.	2887 at 14 years.	3160 at 14 years.	3539 at 13 years.	4401 at 10 years.
Maximum and corresponding age.....	15130 at 72 years.	14464 at 70 years.	13372 at 68 years.	12836 at 67 years.	8801 at 63 years.
			FEMALES.		
Minimum and corresponding age.....	2428 at 15 years.	2610 at 15 years.	2869 at 15 years.	3125 at 14 years.	3911 at 12 years.
Maximum and corresponding age.....	16313 at 76 years.	15407 at 75 years.	14111 at 72 years.	13173 at 70 years.	10393 at 67 years.

CHAPTER XVI.

Of Life's SPECIFIC INTENSITY, *at each exclusively considered year of age.*

120. Hitherto the Intensity of life has been considered, first, as measuring a proportion annually renewed, either of a whole population, or of any discriminated class among the rest, without distinction of ages; and secondly, as measuring the analogous proportion referred to all individuals collectively, within that population or class, but limited by any understood minimum of age, and including all exceeding it. We have now to take into consideration corresponding expressions of life's intensity referred to each set, respectively, of individuals existing at *specific* and *exclusive* years of age, being just completed; and it may be necessary here to repeat, that the Law of Mortality is nothing else than a determination, controlled by definite principles, of the series signified by q_x, as expressing those Specific intensities.

121. The materials, for constructing such a law, consist of the provisional decrement originally deduced from data supplied by adequate experience, but requiring subsequent rectification in all cases, through a methodical regularization of the corresponding and Specific intensities resulting from it; consequently to which process of rectification, a *final decrement* shall appear, abdicating its leading character, and retaining only that of a subordinate series y_x, as will have been seen in the Vth chapter.

122. Those various expressions of Life's intensity, — the Absolute, the Collective, and the Specific, — possess this analogy; that they respectively are quotients of the successive terms of a series, referred to each year of age x, and which terms shall have been divided by the difference between each of them and its next term, referable to $x+1$; whence the *Absolute* intensity $m_0 = \dfrac{\Sigma y - \frac{y_0}{2}}{y_0} = \dfrac{z_0}{\Delta z_0}$, the *Collective* intensity $m_x = \dfrac{z_x}{\Delta z_x}$, and the *Specific* intensity $q_x = \dfrac{y_x}{\Delta y_x}$.

123. It is worthy of remark, that relatively to any class or sex, the Absolute intensity of life appears to coincide with its Specific intensity referred to the age of 55 years; with so little variation, that if any table of mortality exhibited in this respect a difference exceeding two years, such table would in all probability manifest further results bearing a character obviously contradictory with each other.

124. Nothing, in nature, remains stationary. The Specific intensity of life always progresses, increasing or decreasing; and this from assignable causes. The progression, whether of increase or of decrease, must be gradual; marking its commencement, its maximum of the ratio, and its declining period at the termination of which that ratio becomes a minimum : without those circumstances, the increasing intensity cannot turn to a decrease, nor the latter to an increase. Yet, with this incontestable principle, the greater number amongst the tables of mortality hitherto constructed are considerably at variance.

125. No uniform law indifferently governs the waste of human life, throughout all its stages. At successive periods, which shall be hereafter defined, the Law of Mortality

undergoes important alterations, that depend upon inevitable changes in the general conditions of existence, especially during active life; according to the sex—more particularly, —as also, in some respects, to the class of individuals. The discrimination of those periods belongs to the department of physiology; and the considerations depending on this are not to be disregarded, when constructing any mortality-table, if harmony is sought to be maintained in its different parts.

126. The Specific intensity of life, in both sexes, and expressed by q_x,—as measured with reference to the lapse of one year next ensuing, —is inferior at the birth to such intensity at any intermediate period from thence to an advanced age, attainable only by the privileged few. From the birth, it gradually increases, so long as nature may continue its supply of additional vitality, in excess over its waste consequent on an enlarged exercise of our various faculties; but that period of increase, which under the most favourable combination of circumstances should in all probability extend to twenty years, or thereabouts, is always more or less abridged, from counteracting causes inevitably entering into operation; whence in the present state of things, the increasing progression of intensity is arrested, at periods which may vary from the tenth to the sixteenth year of age, according to the sex and to the class of people. After such period, to which a maximum of Specific intensity refers, the quantity q_x invariably decreases, though in modified proportions, until a certain term of very advanced age; and then an anomalous increase, of short duration, once more occurs, as shall hereafter be explained.

127. The Specific intensity of female life is superior to that of the male, under equal circumstances, that of age included; yielding only such superiority, when an approach is made to the period of the just mentio-

ned anomalous increase. The difference, in respect to that superiority, and referably to the birth, — when the female superiority is more considerable than at most other periods, — may extend in the proportion of *six* to *seven*, or in that of *seven* to *eight*, according to the discriminated class amongst a whole population. It is remarkable, that external circumstances can have no influence on this result; as a similar manifestation takes place among still-born children, a much more considerable proportion of which belong to the male sex. That superior measure of original vitality in females, and apparently depending on circumstances of organization, rapidly decreases to the fifth, the sixth, or the seventh year of existence; the two sexes then exhibiting but a very inconsiderable difference of life's Specific intensity. From that period, to about the twenty-seventh year, but with a notable abridgment of this term as regards an inferior class, the female superiority re-ascends by regular gradation to an elevated *maximum;* after which a rapid decrease again takes place, terminating with the fortieth year or thereabouts, when the respective intensities become nearly levelled, for any but that inferior class; and those fluctuations are obviously the result of dissimilar callings in one sex and in the other, during that important period of their active lives. The female superiority then once more proceeds constantly increasing, to about the seventieth year, with an exception of the same inferior class, for which such *second maximum* is attained at about the fiftieth year of age; because it still retained, for that class only, a considerable elevation at the expiry of the preceding period of decline; and from this second maximum, the superior intensity of female life gradually diminishes to about the 82^{d} year, when it ultimately yields that advantage to male life.

128. An original and limited period has already been

noticed, during which the Specific intensity increases for both sexes, by a rapid progression in the first instance, and subsequently in gradually reduced ratios, until the attainment of an *absolute maximum*. It is easily conceivable that the extent of this first period should be subject to considerable variations; and that admitting it carried even to the sixteenth year of age, under the most favourable circumstances, there are others under which it may—from an accumulation of human miseries—be abridged by nearly one-half, as in the case of the manufacturing classes in England, notwithstanding our vaunted civilization. Thus the rates of mortality, expressed by $\frac{1}{q_x}$, may vary according to the sex and class, from *one* death in the lapse of an ensuing year, out of 100 or 120 individuals at nine or ten years of age, to *one* out of 260 or of 300 at fourteen or fifteen years; until which completed terms, the Specific intensity of life shall invariably have progressed by increase.

129. About one-fourth part of all individuals born, and belonging to an inferior class, die without having completed a first year's existence; whilst only one-eighth part, or thereabouts, of another class which may be selected as existing under a set of the most favourable conditions. Generally speaking, one-third of those deaths, in either case, occur during the very first month; one-half during the first three months; and the remaining half is nearly equally divided between the last three quarters of that first year : an equality partly accounted for, by the accidents of dentition, with which those three periods are similarly affected.

130. At whatever year of age a *maximum* may be obtained of the quantity q_x, expressing the Specific intensity of life, the uninterrupted decrease of that

quantity should thenceforth, and to the utmost term of life, be expected; which indeed occurs, provided that the natural course of things remain undisturbed. No medical man or physiologist will deny, that the principle of vitality has a constant tendency to its extinction, independently of any secondary or external causes. Admitting this position, as incontrovertible; it should follow, that, after the series q_x first commenced to decrease, it could not at any subsequent period resume an increasing progression, nor even remain a single moment stationary, without contradicting an express *law of nature;* thus leading to the absurd conclusion of a probability, in more or less degree, favourable to immortality. Were it possible to conceive, as being successive quantities, $q_x = a$ and $q_{x+1} = a + 1$, without supposing, from external and merely contingent causes, some favourable alteration in the general circumstances of individual existence, during the interval comprised between x and $x+1$ years of age; no adequate reason could be assigned, why, if not a similar difference, at least a smaller such as $+\frac{1}{\infty}$, should not naturally take place from q_{x+1} to q_{x+2}, from this to q_{x+3}, and so on to infinity of time; and such occurence of increased vitality could not possess even the smallest probability, between any two given years beyond *max.* q_x, that might not equally extend to any other two subsequent and successive years; hence to every other and similar interval, without end.

131. Alleged facts, however, have occasionally been opposed to the above argument; without considering that the probability of their having been ill-observed, or else badly reasoned upon, comes near to certainty, when such matter of fact has no better support than the infinitely small chance that an established law of nature shall be subverted, or its course be interrupted. Let us ne-

vertheless allow any alleged facts, either well or ill observed of that kind, the full value they could possibly possess; and admit two distinct cases, in both of which the Specific intensity of life may apparently increase, during the interval between any one year and any other more advanced year of age.

132. First, it may happen that the greater number of individuals, whether male, female, or of both sexes, — and existing within any interval of age exclusively, — became liable to excessively elevated rates of mortality, arising from peculiar but transient circumstances, that depended perhaps on social arrangements alone, and discontinued their influence at the expiry of an assigned period. In such case, the observed mortality at successive years of age might indeed represent, in the first instance, and while that influence continued, a series of excessive rates; and subsequently another series, more or less protracted, of rates progressively declining from that period. Yet adverting to the practical purposes of a Law of Mortality, — chiefly for reducing contingent sums to a present value, — it is immediately perceptible that its construction requires those influences to be abstracted, as not belonging to a natural state of things; without which, such law must defeat its main object. Reciprocal agreements, of a pecuniary description, are essentially optional. The military engaged in war could not attach, to annuities dependent on their lives, values equal to those possessed by corresponding contingencies made to depend on the lives of other individuals collectively taken at similar ages; and any government or association, granting life-annuities on valuations computed from tables of mortality founded on any other hypothesis than that of a natural state, would inevitably lie under the disadvantage of mostly dealing with parties subject to inferior rates of morta-

lity, referred to their respective ages, than the rates which those tables admitted.

133. Secondly, in very advanced life, — say from the 86th to the 90th year of age, according to the description of any population or class, — an anomalous appearance of progressive increase is manifested during a very few years, as to the Specific intensity of life referred to those respective ages onwards. Not that individual lives recommence actually to improve; but the great mass, comprised under the Law of Mortality, having then disappeared, — latterly in a very rapid progression, — the comparatively small number of remaining individuals at those ages are necessarily of superior selection, consequently to their continuing to exist under a set of very favourable conditions, including the several advantages of primary constitution and others qualifying them as privileged persons; and these ultimately stand prominent, exclusively competing for protracted longevity. Indeed this natural selection, of particular lives, subsequently recurs at different stages amongst centenarians, which mostly depends on corresponding degrees of vigour in the primary constitution; whence arises that the rate of mortality, amongst any quantity of individuals having attained a very advanced stage of life, may in reality prove inferior to the rate exhibited amongst the much greater quantity of those who existed together at less advanced years. This anomaly was first observed by Wargentin in Sweden, and afterwards by Duvillard in France : it has since been confirmed by our cotemporary Mr. Milne, and ought always to be taken into consideration, when tables of mortality are constructing; because those results are perfectly independent of external causes.

134. The greater number of mortality-tables refer to the age of *ten* completed years the maximum of Specific inten-

sity, having progressively increased from the birth, or q_0. Dr. Halley's tables for the population of Breslaw, Dr. Price's for that of Northampton, Duvillard's for France at a former period and limited to the population of its towns, have uniformly admitted various *maxima* referred to q_{10}; remarking that those different tables all apply to populations of an inferior description. The latter distinctive circumstance was probably overlooked, on a similar reference of the *maxima*, to the limited age of *ten* years, being extended to tables subsequently constructed; amongst which Mr. Milne's, relative to the population of Carlisle, as also those of Mr. Davies and of Mr. Babbage, both relative to Assurable lives. From the elevated measure of Absolute intensity announced by each of the latter three, they must be clearly understood as exclusively applicable to select classes; whence the above limitation is most likely founded in error.

CHAPTER XVII.

Of Longevity.

135. The vitality appertaining to old age is generally undervalued. The tables of mortality set forth at different periods, and by various authors, mostly assume the extinction of life before its hundredth year; consequently to which the values of contingent sums, that depend on lives exceeding 80 years of age, are either precluded from appreciation, or at best computable from those tables at hazard and without any approach to accuracy. Such a view of the chances attendant on longevity is the more erroneous, as centenarians are well-constituted and healthy, exempt from infirmities affecting the sources of life, as also from chronic diseases of inevitable tendency to abridge it; besides that they possess the further advantages of fixity to the soil, of uniform mode of living, and of general habits confirmed by experience to be best suited for them.

136. The privilege of longevity is chiefly prepared by the individual's primary constitution, the vigour of which may be infused in various degrees. To be completely effectual, this original advantage requires however the support of secondary circumstances, establishing a set of favourable conditions, under which that individual's existence shall have continued, and partly depending on the rational exercise of free agency. The life thus privileged may, notwithstanding occasional departures from the strict rules of prudence, be yet protracted to an unusual length; whilst no imaginable concurrence of favourable circumstances could

be capable of extending its term beyond the one originally assigned. It thence happens that longevity is not unfrequently propagated through successive generations, so long as the more essential conditions of a favourable description remain unaltered. Observations on the mortality of centenarians seem to indicate a periodic recurrence of the anomaly described in the preceding chapter; but those observations have hitherto borne on quantities not sufficiently numerous, for enabling to ascertain either the precise periods, or the measure of increased intensity of life probably attendant on a transition from any one of those periods to the next, as regards an aggregate of individuals so circumstanced.

137. From the benefit of Longevity almost all are debarred, who partake much of life's indulgences; nor is it the portion of those devoted to mental occupation. Easy and even affluent circumstances are indeed favourable to the preservation of life during infancy, and may continue so to operate for a period more or less protracted; but those indulgences, unless judiciously controlled, infallibly generate chronic diseases, tending to curtail the natural term. On the other hand, an excessive exercise of the intellectual powers, and generally a course of anxious life, oppose to longevity another obstacle, consequent on incessant irritation of the nervous system; and though a considerable exercise of those powers may not uncommonly allow extrance upon a rather advanced term, yet is life in that case rarely continued beyond eighty years, the individual being indebted, for such limited advantage, to his probably temperate habits, and to moderation in all other respects. The recorded instances of unusual longevity are, almost without exception, confined to old soldiers, who escaped the worse chances of war, and to peasants whose circumstances placed them but a single degree above want of the common necessaries.

CHAPTER XVIII.

Of EIGHT PERIODS, *naturally dividing the course of human life.*

138. The waste of life is not governed by any uniform law, throughout every stage of our existence. At successive periods, the conditions to which that existence is subjected undergo important alterations, consequent on our varied callings,—before,—during,—and subsequently to the term of active life. Those callings are not the same for both sexes; neither do the changes that occur, during the active part of the one and of the other's lives, correspond in respect to periodicity, character, or degree. It thence follows, that, from the period at which the Specific intensity has commenced decreasing, the progression of such decrease is governed by totally different laws, for the Males than for the Females; and that the differences, in their compared intensities of life, are extremely variable from one period to another.

139. Analyzing above a score of Mortality-tables, supplied by various authors, it is observable, notwithstanding their innumerable discrepancies and contradictory results, that human life divides into *Eight* periods, more or less protracted, yet perfectly distinct; and that the same conditions of existence are very nearly maintained throughout each period respectively, as regards each sex; but which conditions admit such modifications, on the transition from one period to another, that the Specific intensity of life proceeds on its decrease by alternately increasing and decreasing series

of the progressive ratios; both taking place from the ascertainable operation of combined causes.

140. During a *first* period, computed from the birth, the Specific intensity gradually increases according to a progressive law, which in the first instance is rapid, then gradually abating, until that intensity obtains a maximum at the conclusion of this first period, or about the age of puberty; say rather later, when circumstances concur towards that maximum being retarded, or on the contrary earlier, under a series of circumstances unfavourable to the individual; the latter being more frequent in the present state of things. The principle of this increase of intensity has been discussed in the 126th paragraph.

141. During a *second* period, the intensity commences to decrease, according to a progression the ratios of which are incessantly more elevated. Its term extends to the *twenty-fourth* year, for the male sex, except of an inferior class; respecting which, a curtailment of the first period admitted, to the *seventeeth* year only, an increase of the proportions that regulated a diminishing intensity. For the female sex, this second period is protracted to the *thirtieth* year, when nearly three-quarters of all marriages within the 53^{d} year of age are already contracted; but it is limited to the *twenty-third* year, as regards an inferior class, from the above-mentioned cause. This period is, for the male sex, one of restlessness, toil and danger: the human faculties are then exercised to the utmost, and life is more freely expended than at any other season. The female sex, of whom the assigned functions are quite different, and on whom greater restrictions are imposed, experiences a less rapid decrease of life's Specific intensity during the corresponding period, which is of greater extent. Inflammatory diseases,

often of fatal termination, are mostly prevalent, for both sexes, during this second period.

142. A *third* period is marked by the intensity's continuing to decrease, but this by a progression the ratios of which come nearer and nearer to *unity*; until at the termination of that period the intensity may, according to the class and sex, approach a stationary quantity, even in the natural state of things. It generally extends to the 36th year, for the male sex, and to a 44th for the female; but with the abridgment of a few years, in regard to an inferior class of both. It is in course of such third period that the male sex mostly enter the married state; — that activity is moderated; — that impetuous passions relinquish a portion of their wonted empire, — and that the usage of life is regulated with greater economy than before. The corresponding period of female life is carried on with greater uniformity, in the performance of duties salutary to health and conducive to happiness : it also admits, with regard to that sex, an incessant diminution in the proportions of intensity's decrease, without any appearance of disadvantage arising from maternal subjections. This third period develops only in a slight degree the chronic diseases, thereafter preparing more elevated rates of mortality.

143. A *fourth* period exhibits the decreasing intensity in considerably accelerated proportions, from year to year; which proportions of the decrease afterwards continue with very little variation for a few years, during which again they possibly may diminish. The term of this period extends at least to the 57th and at most to the 61st year, for both sexes; except for the male of an inferior class, with respect to whom it appears blended with the next succeeding period. With that single exception, the propor-

tions expressed by $\Delta \lambda q$, of that decrease, obtain an *absolute maximum* for the male sex, as also a *first maximum* for females of all classes. Chronic diseases, influencing the rates of mortality in a considerable degree, then assume a more threatening aspect, especially as regards the female sex; whose health however consolidates, subsequently to overcoming the natural crisis which usually takes place towards the latter part of this fourth period. It is characterized by a comparative calmness of the human passions; but its not unfrequent attendants are the development of diseases that were only incipient, together with increased liability to many others.

144. During a *fifth* period, the Specific intensity of life recommences a more rapid decline; and the proportions of its decrease, which may even have abated towards the conclusion of the preceding period, obtain an *absolute maximum* about the 80th year of age, regarding the female sex, generally, as also the males of an inferior class. About the middle of that period, the *maximum* of deaths, in numerical quantity, takes place; which is more elevated for the female, than for the male sex, respecting which such maximum is anticipated by three or four years; and its superior quantity then results from no other cause, than the superior number of then existing females at the corresponding age.

145. A *sixth*, but very short period, then succeeds. Its term for both sexes, extends to the 87th year for an inferior class, and to the 91st for a superior amongst all select classes. It is remarkable for a rapid diminution, from each year to the next, of the differences in the still decreasing intensities; the further decrease of which seems suspended at the expiration of that period, thus establishing a *first minimum* of Specific intensity.

During this sixth period, an immense majority jo the individuals who entered on its commeneement disappear from the scene of life; leaving those only, who were originally constituted for longevity, to compete amongst themselves. This, together with the latter part of the preceding period, is the season of nearly absolute repose; in which the character of prevailing diseases has changed, and which is not incompatible with vigorous health.

146. The *seventh* period, equally short, terminates for both sexes, and for all classes, with the 94th or 95th completed years; and during its continuanee, the Specific intensity of life apparently exhibits an incessant increase, asregards the collective masses considered at each year of such ages. This anomalous increase arises from a cause explained in the 133d paragraph; the proportions of which increase first proceed by augmentation, and next by diminution; the natural decrease of intensity afterwards resuming its course. The preservation of life, during and subsequently to this seventh period, chiefly depends on invariably persevering in the mode of living and in other confirmed habits; as at those very advanced ages, but few unhealthy subjects continue to exist.

147. The *eighth* and last period exclusively refers to centenarians; the law of mortality amongst whom is of more difficult ascertainment, than it is regarding any other period of life, consequently to the paucity of applicable data; further observing, that very little distinction, if any, is then to be made, between classes otherwise distinguishable by the different circumstances of their existence.

148. Those various periods, considered with reference to either sex, as also to distinct classes of people, differ

not much as to their commencement, nor as to their termination; but it has already been remarked, that they do not respectively coincide as regards the contradistinguished sexes, at least the second and third periods, embracing an important part of active life. Whence, and during those two periods in particular, the inequalities of comparative intensity, between males and females at similar ages, undergo considerable fluctuations; those inequalities being at one time a maximum, and at another time a minimum, within an inconsiderable lapse of years; say from the 26th to the 43^{d}, at the utmost.

CHAPTER XIX.

Of INTERPOLATION, *or a method of connecting the series of Specific intensities.*

149. For judiciously constructing a Law of Mortality, — the Absolute intensity of life, referable to any given population, being previously ascertained, — requires first to determine the commencement and termination of the respective periods described in our preceding chapter; and, secondly, the due expression of life's Specific intensity at those respective stages. Such determinations, though only by approximation in the first instance, will remove considerable difficulties; a pre-ascertainment of the absolute intensity affording, in all probability, sufficient means ultimately to rectify all irregularities in the series q_x of Specific intensities, as also in the series y_x or Decrement, the summation of which must accord with that original datum; the only difference consisting in a modified distribution, referable to a stationary state of the population, which may have been progressively increasing or decreasing. Towards this accordance, many successive trials may be requisite; by means of arbitrary — though only slight — modifications of the assumed expressions of intensity q_x, at the transition from each period to the next, until final adjustment. It is, in some degree, a work of patience; but all errors will thence find themselves mutually corrected, and there shall result from this mode of proceeding a Law of Mortality harmoniously proportioned in

all its parts, relatively to the specific class and sex being the object of consideration.

150. It cannot be concealed, that an interpolation of the successive terms q_x, for the first period, which is carried from the birth to the age of puberty or thereabouts, meets greater difficulty of execution, than the interpolation for any subequent period; and that the former may occasionally lie open to arbitrary determinations, which should always be sparingly and soberly resorted to. Nor is it to be imagined, that the crude results of direct experience may implicitly be relied on : the contrary is fully evinced by the enormous discrepancies of the various mortality-tables hitherto constructed, in respect to corresponding terms of the series, where the expressions of Specific intensity are considered in their passage from the first to a second, from this to a third, and from the latter to a fourth year of life, as also towards the approach to a maximum of that intensity. The operations of nature always proceed by gradation, conformable to some regular law, but never by abrupt transitions; and inasmuch as the purpose of a table of mortality is for generalized application, it becomes of necessity to regulate that early part of the series q_x, relative to the first period, according to a systematic progression : absolutely not otherwise.

151. Suppose two Specific intensities, q_0 and q_x, the former referred to the birth, and the latter to any completed year of age terminating the first period, during which the specific intensity of life invariably progresses by increase; and admit λq_0 and λq_x, logarithms of those quantities. Let the difference between those logarithms be the sum of another series $\Delta\lambda q$, formed according to the law of figurate numbers, resulting from several orders of differences alternately positive and negative; the last

of which orders, or subordinate series, composed of equal differences $\pm c$. Observing that the greater number of those successive orders of differences has the effect of accelerating the progression of increase, whilst the smaller would have that of retarding it; three or four orders, at most, should be adequate to establish a law of progression sufficiently approaching the results of crude experience, however irregularly the latter might progress; and to produce consistency as a whole. If the discrepancies between the one and the other series were so considerable, as to require their nearer approximation, — always supposing the actual experience to have been correctly proceeded upon, — it will then be eligible, either to admit mean results between the two series produced by three and by four orders of differences, or else to admit another series of ultimate differences, the quantities of which *positive* for any part of the considered period, and *negative* for the remaining part, or the contrary; these having the effect of causing the immediately preceding order of differences alternately to exhibit increasing and decreasing quantities. The preference of any one of those methods is discretionary; the sole object being to regularize the primary results obtained in a crude state, with as little deviation as possible from a systematic law whatsoever; but if neither made a satisfactory approach to those results, the original observations must then be presumed defective, more or less. It is apparent that this synthetic process, depending on the determination of a series of quantities c, either positive or negative, or on successive series of both, precludes every inconvenience; and that a rectification of any irregularities, incident to the data supplied by experience, may thus be arrived at; ascertaining that part of the series q_x, relative to an interval comprised between the birth and the term of that period which we first discriminated, the Specific intensity of life then commencing to decrease.

152. Inasmuch as the differences in present value of sums depending on the contingencies of life, at the severally completed years expressed by $x = o$, by $x = 1$, and by $x = 2$, are very considerable; it may not be unimportant, for the purpose of obtaining a sufficient approach to correctness in those valuations, to determine the decrement and probabilities of life, with reference to various intermediate periods between the birth and the first completed year, as also referably to an intermediate term between the latter and the completion of a second year of age. In regard to the former interval, the proportions according to which the lives successively drop during the first, second and third months of existence, respectively, and likewise during the subsequent three quarters completing a first year, have already been stated in the 129th paragraph; the Decrement may then be adjusted, in conformity with such proportions of deaths during those fractional intervals. Analogous results are to be obtained referably to a period $x = 1\frac{1}{2}$, sufficiently approaching the truth for all practical purposes; by admitting $q_0' + q_1$, to express the life-intensity attached to a first completed year, when measured in relation with the specific interval between $x = 1$ and $x = 1\frac{1}{2}$; this interval supposed to participate, in an equal degree, of the intensities attached to the latter half of that first year and to the first half of a second.

153. The interpolations, for periods subsequent to the first, are in many respects to be conducted from analogical considerations; and generally, three orders of differences, between λq_x and λq_{x+n}, have been adopted in constructing the Laws of Mortality applicable to each class and sex, which it was our purpose to discriminate.

Let us now particularize the method of those successive operations.

154. Being given any two quantities, λq_x and λq_{x+n}, referred to the termination of consecutive periods; as also given their last connecting differences, $\Delta\lambda q_{x-1}$, ${}^2\Delta\lambda q_{x-2}$, and ${}^3\Delta\lambda q_{x-3}$; the continued influence of each of the three latter, on λq_{x+n}, being ascertained, any arbitrary type of calculation, founded upon the law of figurate numbers, will enable likewise to ascertain the relative *unit*, or element c of that calculation, referable to the last order of differences, during the period entered upon, and at the termination of which the quantity λq_{x+n} shall have been predetermined. That quantity c may indifferently be made positive, negative, or both alternately, at certain intervals best suiting the required adjustment of the terminating differences of the three orders; so as to facilitate, at every successive process of this kind, the transition from one period to another, by a natural and easy connexion of increasing and of decreasing quantities; avoiding the sudden breach of any one amongst those connecting links. Those proceedings embrace a great extent of discretionary latitude; respecting which it is proper to recall, that a succession of landmarks, q_x, are understood to be previously provided at the commencement and termination of each period in particular, whence the important object of regularity may be fully obtained; and all deviations from the true law of progression, however impossible precisely to discover, — the more so from its being perpetually fluctuating, — are then circumscribed within very narrow limits.

155 When the series of negative quantities $\Delta\lambda q$ have either to increase or to decrease, the corresponding series ${}^2\Delta\lambda q$ cannot naturally pass from the positive to the negative, nor from the latter to the former, otherwise than

by a succession of gradual proportions having their alternate *maxima* and *minima*, both in that second and in the third order of differences; and the small portion of discretionary latitude which we have admitted, being incessantly controlled by the series of facts actually observed, must remain exempt from objection; unless a permanent character were unduly attributed to those fortuitous results of experience, notwithstanding their discrepancies and the irregularities of their mutual connexion. Hence an absolute conformity is to be sought only in the general and periodic results; whereas regularity of progression is at all times an essential requisite, under the view of an useful and generalized application of the Law of Mortality. All results, thus obtained, are certainly nothing else than systematic approximations; but in things of this nature, where positive data are — and ever must be — partly wanting, no one could possibly flatter himself with obtaining nearer approaches to absolute certainty.

156. The anomaly described in our preceding chapter, as attaching to the *seventh* period, does not prevent its interpolated quantities being determined by the method employed for all other periods; always carefully and gradually operating, in each of the elementary series that resolve into an ultimate series λq_x, the transitions to and from that period. Regarding the *eighth* and last period, rather more obnoxious than any other to arbitrary determinations; and in order that the law of mortality may, with all possible correctness, exhibit the phenomena especially belonging to longevity, at its variously advanced stages, the following method of proceeding, to determine the remaining part of the series of Specific intensities, has appeared best to answer the desired purpose.

157. Whatever may be the quantity λq_{94}, or Loga-

rithm of the Specific intensity measured for the ensuing year, from the completed 94^{th}; suppose, for the male sex, *nine* equal subdivisions of that last period, each of which embracing *twelve* years; whilst *eight* only, in similar extent, of those subdivisions for the female sex; and assume the utmost term of longevity to coincide with the termination of the last subdivision, in both cases. Then, and according to the sex referred to, admit an abatement either of *one-ninth* or of *one-eighth* part of the quantity $\lambda\, q_{94}$, at the expiry of each twelve years; as also 30 c, to represent such equal quantities of abatement; and lastly, interpolate for each year of that interval, by successively abating 0, c, 2 c, 3 c, 4 c, 5 c, 5 c, 4 c, 3 c, 2 c, c, and 0; whence the Specific intensity will be represented as stationary during three years, of which one to precede and another to follow each completed subdivision of the eighth and last period of life. It is very probable that, about the termination of such respective subdivisions, the corresponding expressions of intensity should admit further anomalous increases, as remarked in the 133^{d} paragraph; causing those expressions to proceed alternately increasing and decreasing, during six years respectively, though with preponderation of the decrease at each stage of advance. But this, as a matter of fact, is not sufficiently confirmed by indubitable experience, to allow of its being as yet introduced into the Law of Mortality.

CHAPTER XX.

Of the tables admitted, by an Act of the British Parliament, to regulate the valuation of Life-annuities granted by the Exchequer.

158. It is not our purpose unnecessarily to dilate on the numerous Mortality-tables of which the public is already in possession. Amongst their different authors, — Halley, Sussmilch, Kersseboom, Price, Simpson, Deparcieux, Duvillard, Mourgue, Milne, Davies, Babbage, Gompertz, Finlaison, and Riekman,—the latter half are our respectable cotemporaries; and it may be sufficient to exhibit under a synoptic view the results at which they severally arrived, however discrepant, consequently to the diversity of time, place, and circumstance. In the number of those tables, however, are *two* constructed by Mr. Finlaison, and respectively referred to the discriminated sexes, as also understood applicable to the specific class of Life-annuitants and Tontine-nominees. They having been admitted, as a law of the land, to serve as regulators in the valuation of Life-annuities thenceforth to be granted by the Exchequer of this country; and the writer of these pages having conceived proper, at that time, to warn the legislature against blindly adopting a measure of such nature and importance, without previously obtaining the opinion of a *plurality* of persons competent on a matter of their department; it becomes the more imperative on him, here to consign his principal objections to those tables, as, — in disregard of his petition hereafter transcribed, — the ministerial influence obtained a Bill to

pass, sanctioning such a practical application of Mr. F.'s tables, as they are unlikely to meet any where else.

159. The following petition is copied from the official reports of the House of Commons; bearing date the 20th March 1829, n° 2447, pages 1031 to 1034 : —

A Petition of *Francis Corbaux*, of *No* 5, *Hercules Buildings*, in the parish of *Lambeth*, County of *Surrey*, Gentleman, was presented and read; setting forth, That a Bill for enabling the Commissioners of the National Debt to grant Life Annuities, as also deferred Annuities of a similarly contingent description, is understood to be before the House, called upon for sanctioning a certain scale of valuations applicable to those periodic and contingent payments, although every means of ascertaining not only the accuracy, but (what is still more important) the specific fitness of such proposed scale, seem to be purposely withheld; the Petitioner humbly submits, that the possession of adequate information on the subject by the House is not attainable otherwise than through the publication of any tables of mortality upon which that computation of relative values has necessarily been founded, whence the scientific men with which this country abounds being afforded an opportunity of investigating those elementary data would not fail to cast such light upon the matter in discussion as to remove from the House all causes of doubt or uncertainty; the Petitioner further submits that, from the sole motive of contributing to the advancement of general knowledge, he has devoted many years, at great personal sacrifices, to arduous researches concerning the matter now before the House, and in particular as regards the natural law, according to which the waste of human life at its successive stages is governed, as also regarding the very considerable modifications which that Law undergoes, consequently to a discrimination of the different circumstances attending the existence of a whole population, or of any select portion of it requisite to be taken into especial consideration, and that, having applied analytical methods of his own, and of a most elaborate description, to those researches, with a view to results more accurate and precise than those usually obtained from analogous investigations, he may, without incurring the charge of presumption, venture to assert his competency for entertaining a digested opinion on those subjects; in hope, therefore, that this apology for interference will be received with indulgence, the Petitioner begs leave, additionally, to submit that a report commonly prevails of certain statements urged in the shape of information for the House, and in support of the above-mentioned Bill under its' consideration, but which statements, or rather allegations, are ascertained by him to be devoid of foundation, and completely at variance with the best authenticated facts; one of those allegations appears to consist in the pretended discovery that a life aged fifty years, had a superior probability to that of another life aged forty years only, of

enduring for the term of one more year, viewing those two lives as respective averages, and it is said that this extraordinary and general position was thought to have been proved by a reference to specific tables of mortality, usually denominated the *Northampton*; justly fearful, lest such an allegation, if received upon trust in the supposition of its emanating from indisputable authority, and if coupled with any others errors of which it warrants the suspicion as still more extensively vitiating the whole set of proposed valuations, obtained undue influence on the decision of the House, the Petitioner conceives it of urgent necessity that he should here consign a correct representation of the mis-stated fact, in order that their vigilance may be called forth to avert the misfortune of legislating in utter darkness upon a subject involving a series of complicated questions, beset with difficulties of which none but scientific persons can be sufficiently aware, thus endangering the high character for justice and for sagacity, which the *British* Nation and its Representatives in Parliament are accustomed to maintain; the Petitioner abstains, for brevity's sake, from dilating on a physiological principle, which at once disproves the possibility that any collection of persons aged fifty years should possess an intensity of life superior to that of another collection equally numerous, of persons aged forty years only, and in other respects existing under similar conditions with the former; that principle, known to medical men, being that the phenomenon of respiration, whilst it maintains the vital spark, is also one of effectual though slow combustion, in proportion with whose advance the human frame retains in a less degree the power of repelling any causes of destruction by which it may be assailed; neither will the Petitionner permit himself the latitude of adducing, as proof relatively to a controverted matter of fact, any results to which he may have arrived through his own researches, but he begs leave unhesitatingly to state in the first place, that the *Northampton* tables of mortality show, on the contrary of what appears to have been quoted from them, that if any quantity of deaths returned during the next twelve months, amongst a collection of individuals aged fifty years, be referred to one thousand living at that age, not less than one thousand three hundred and fifty-six amongst the living at forty years only, will be requisite for returning an equal quantity of deaths during the year following, or next interval of age; and secondly, the Petitioner, after carefully analyzing not less than twenty different statements of the law of mortality published at various periods, as also in various countries or districts, each of which statements, deduced from a specific set of actual experiments, is enabled beyond all possibility of mistake to state before the House, that on an average of the whole, a superiority is exhibited in the proportion of fourteen hundred and twenty-one to one thousand, as to the intensity of life at forty over that at fifty years of age, the superiority on the same side being also manifested by every one of those statements individually, whilst no set whatsoever of experiments on the mortality of mankind, and known amongst scientific men, has even the smallest tendency to revert this position; the Petitioner again has to submit, that inasmuch as the gradual

waste of life is demonstrated to proceed by a series of annual proportions, differing very considerably with reference to the discriminated sexes, it cannot become indifferent to admit or reject the application of a specific law of mortality for each sex in particular, but that he is perfectly convinced of the indispensable necessity to proceed upon distinct tables for male and for female annuitants, towards a correct valuation of the life-annuities that may henceforth be granted, without which, in this age of speculation, profitable systems would probably be acted upon to the detriment of public economy, through the selection of female nominees at suitable ages, which might also be attempted through a selection of peculiarly healthy nominees of either sex, and admitted at very advanced ages, in case that any adopted law of mortality were not perfectly appropriate; and in the latter respect the Petitionner begs leave to submit, for the consideration of the House, a few concluding remarks, the peculiar importance of which he hopes to be allowed to press upon their attention; from a spirit of indiscriminate routine, it has been too prevalent a custom to assign in the construction of mortality-laws, a greater value to the fortuitous results of limited experiments, than they are entitled to possess, and to admit an indiscriminate application of those laws, whence enormous miscalculations have frequently been generated, which cannot be too much guarded against for the future; any law of mortality embracing a whole population can apply but to statistical purposes only; for all others, and especially with reference to financial or pecuniary transactions, the application of specific laws, deduced from an exclusive consideration of the classes of persons respectively to be dealt with, becomes an indispensable requisite; few, amongst those whose special attention has not been directed to these matters, are aware of the wide difference existing between the extremes, in respect to the classification of which an entire population is susceptible; in such classification the annuitants must be assumed to hold the first rank, as existing under a set of definable conditions nearly common to them all, and being peculiarly favourable to the preservation of life throughout its successive stages; whilst of the same population, that part which is the object of our Benefit-Societies may be considered very nearly as the other extreme; no public institution undertaking periodic payments made to depend on the continuance of life amongst the first of those classes, or else receiving from individuals of the other class periodic contributions of a similarly contingent description, and computing in either case the present value of such contingencies according to the law of mortality referable to an indiscriminate population, could possibly escape ultimate ruin, whilst the reverse may happen in other instances, when the applied law is too favourable for the undertaking party; but with regard to the first remark, as connected with the immediate object before the House, the Petitioner firmly believes that any series of experiments afforded by the Government Annuity-Office alone, must be still too circumscribed towards the construction of laws of mortality applicable, without danger of material error, to the discriminated sexes, and for an object so permanent as the one contemplated for the House to legislate

upon, and he conceives that their construction, in order to establish correct proportions, as also to maintain a proper gradation of those proportions in the respective valuations, ought to proceed upon a much more enlarged basis, which cannot otherwise be supplied than through extensive research aided by mathematical analysis, without excluding the consideration of data supplied by other Countries; it would be useless to conceal that our own Country can at best afford very scanty materials towards that desirable object, consequently to a loose and imperfect system of registering the births, marriages, and deaths, especially in what relates to the ages of the parties concerned; to admit that the construction of any mortality-law, truly and equitably applicable to the Annuitants of this Country, should require its being proceeded upon a series of observations confined to *British* lives only, would be arguing from the most frivolous distinction, and demanding what at present is scarcely obtainable in any satisfactory shape; indeed, whether in *Great-Britain*, or in almost any other part of *Europe*, very little, if any distinction at all, is to be made between the values of lives existing under similar circumstances, and supposing that the class alluded to were defined, first, as possessing a physical Constitution and conformatio n exempt from any material defect; secondly, as having the means of wholesome subsistence in all probability assured; thirdly, as being dispensed from employments endangering life, or obviously tending to abridge it; fourthly, as habitually residing on a salubrious soil; fifthly, as being free from disease or chronic complaints at the time of their becoming nominees, besides a presumed non-liability to the small-pox; a Law of mortality deduced from the consideration of circumstances thus generally defined, whilst a discrimination of the sexes were provided, would without danger of important error be found applicable to all life-annuitants existing throughout the world; from all which considerations the Petitioner humbly prays the House, first, that neither the present nor any other Bill for the purpose of enabling the Commissioners of the National Debt to grant Life Annuities on a specific scale of valuations, may pass the House without their previously having ordered the publication of all grounds upon which such valuations are to be computed, nor without having afforded the whole body of scientific men an opportunity of rectifying the elements of those computations, and of casting all possible light on that intricate and highly improvable subject; secondly, that no Bill for sanctioning the valuation of periodic payments whatsoever, intended by the Government, and to depend on the contingencies of human life, may at any time so pass without its being provided for the computation of a distinct scale of their valuation with reference to each sex, as also without a previous sanction of the specific tables of mortality upon which such computations are to be founded; thirdly, that no Bill, such as above described, may pass without an adequate provision for preventing frauds which might be practised, through the substitution of living persons, for nominees whose lives were actually extinct; fourth and last, that before granting their sanction to any scale of the valuations above-mentioned, the House do take into its enlightened consideration

such inconveniences as are not unlikely to arise from the admission of fluctuating values, to correspond with casual fluctuations in the market-price of other public securities, which inconveniences the Petitioner conceives to outweigh any others attending the adoption of a standard ratio of perpetual interest, towards computing the relative values of the different contingencies.

160. The tables, to which the matter of this chapter alludes, should be repudiated on the following grounds.

161. First : Because the *Absolute intensity* of female life is there exhibited in the very exaggerated excess of *five years and seven-tenths*, over that of male life; although the question is concerning a class of *select lives*, which admits only a *minimum* of superior intensity possessed by the former sex, or at the utmost an excess of *three* years.

162. Second : Because the *Collective intensity*, in regard to the one and to the other sex, is exhibited as invariably decreasing from the very first year of existence; although an increase, during the first five or six years, at least, is an incontestable result of the vitality's rapidly progressive consolidation after that first year; but which progression has never failed to become manifest, according to experience, proved by every one of the numerous Mortality-tables hitherto constructed, except these two only.

163. Third : Because the *Specific intensity* of life is there presented, regarding the males, as *eight* times greater, and regarding the females as even *nine* times greater, for the interval separating the second from the third year of existence, than it is for the immediately preceding interval, or that from the first year to the second; being a most unaccountable and utterly inadmissible disproportion, to whatsoever *minima* such intensity might by possibility be reduced for the first year of life,—as also for the respective

sexes, — and to whatsoever *maxima* it might upon justifiable grounds be elevated for the second year, especially with reference to a select class. It should however be remarked, that those tables have left entirely out of consideration every result concerning such first year of existence; which has required to supply the expression of its Specific intensity, in order to complete the decrement, and to discover, by summing up its successive terms for each sex, their respectively Absolute intensities, which any law of mortality has necessarily to render manifest. At the same time, the vacuity thus filled up, — by admitting for that first year, and with reference to each sex, measures of Specific intensity equal to those corresponding with the present writer's tables relative to the same described class of people, — will by no means be found to the disadvantage of those now criticised.

164. Fourth: Because, under the admission of those supplementary results,— without which, and if more elevated intensities were introduced for that Specific year, this fourth ground of objection would acquire but greater force, — it is made to appear that *one-half* of all females born, of the class referred to, attain the comparatively advanced age of *fifty-seven and a half* years, whilst a similar proportion of the males appeared to outlive their *forty-eighth* year of age, only. Although the latter result, as unconnected with the former, may unquestionably be admitted, an Equation of life so elevated at the birth has no example amongst any class of individuals congregated together in considerable number, even of the female sex exclusively; neither any example of a difference so enormous as *ten* years, between the Equation of life for the respective sexes and referred to the birth. Further observing, as regards the female, that not less than three-quarters of the whole are supposed, by Mr. F's tables, to attain the completion of *twenty-one* years; which is another result of these, quite

failing to be borne out by ascertainable facts. The various results observed upon, under this head, are set forth notwithstanding that the progressive increase of female life's Specific intensity is made to terminate with the *eleventh* year, whilst that of male life is exhibited as extending to the *thirteenth* completed year of age; which implies the subversion of an established fact,—*i. e.* that such increasing progression of intensity is generally carried rather further on, in case of the female, than in case of the male sex.

165. FIFTH: Because, — comparing the Specific intensities of life, as announced, —there appears two consecutive quantities $q_3 = 80{\cdot}088$ and $q_4 = 96{\cdot}332$, relative to the male sex; whilst, as regards the female, two other corresponding and consecutive quantities $q_3 = 91{\cdot}092$ and $q_4 = 94{\cdot}549$. Now at the ages of *three* and of *four* years, at which any consideration of sex has the least possible influence towards diversifying such results between the contradistinguished male and female, — when the conditions of their existence, and all other concomitant circumstances, are alike, — it is utterly impossible that a difference of the Specific intensity, referable to so short an interval, should thus extend to 20 1/4 *per centum* in the case of males, and at the same time to no more than 3 3/4 *per centum* in the case of females. Considerable disproportions of the same kind, between the compared intensities for both sexes, at intervals of a single year, again recur referably to the ages from 7 to 8, from 12 to 13, from 14 to 15, from 17 to 18, and from 19 to 20 years, etc.; and disproportions so intolerable, between results which should naturally bear due analogy with each other, could doubtless not have failed to strike the author of the tables, had he but enlarged his general considerations as far as to those comparative intensities.

166. Sixth : Because a further discrepancy of magnitude is observable, in the corresponding results referred to the different sexes, and consisting of the Absolute intensity of female life being made to assimilate with the Specific intensity referred to 61 or 62 years of age; whilst the Absolute intensity of male life is assimilated, with its Specific intensity, even *eight* years earlier, or at the age of 53 or 54; thus shewing, as in many other instances of compared results, that the advantages especially belonging to female life have been greatly overrated by the same author.

167. Seventh : Because the Specific intensity of male life is misrepresented as equal, at the very remote ages of *twenty-four* and of *forty-eight* years; at the same time as an increasing progression, of that intensity, has been admitted during the first half of that interval, and then a decreasing progression — even divested of regularity — during the other half; in such manner, that the intensities at *thirty-four* and at *thirty-five* years of age are made to exceed those at *twenty-three* and at *twenty-four* years, in elevated proportions as *eight* to *seven*. The motives of objection to those contradictory results have been substantiated in the preceding paragraphs, 124th, 130th, 131st, and 132d; consequently to which motives, such relative statements, in the table referred to male life, ought to forbid its application for practical purposes; unless the individuals of that sex, and existing at a certain interval of age, were clearly shewn to be subjected, exclusively of those at any other ages, to special and disadvantageous circumstances, capable of disturbing in so material a degree the naturally and gradually decreasing proportions of the Specific intensity of life at successive years of age, after the previous increase had terminated. When statements are advanced, thus at variance with a law of nature, there is sufficient warrant for unhesita-

tingly pronouncing them absurd, notwithstanding a few favourable but probably fallacious appearances; and then it is ineligible to generalize such apparent results, without a previous and thorough investigation, which should satisfactorily account for the cause whatsoever of such obvious discrepancy.

168. Eighth: Because the Specific intensities of life, compared with respect to the contradistinguished sexes at similar ages, are occasionally exhibited in most exorbitant disproportions, favourable to the female; namely, at the age of *twenty-three* years, where that intensity is made to appear in a ratio of superiority as *five* to *three*, over the intensity possessed by the males; which elevated ratio is even exceeded for all ages comprised between the 53^{d} and 62^{d} year, and carried to an excess extended in the proportion of 1·77 with reference to the particular years 55th and 85th, as also to some others more advanced. Although the superior intensity of female life is fully established, yet is it circumscribed within narrower limits than the above, and attains a maximum at about *twenty-five* years of age; when, comparatively with the intensity of male life, it takes place nearly in the proportion already very remarkable of *ten* to *seven*, but afterwards obtains a rapid decrease to about the *fortieth* year; the respective intensities then becoming almost levelled, consequently to the male sex being rather favourably circumstanced at that time of life, from a more settled and better regulated mode of living than at preceding periods. But the tables, alluded to, exhibit even at the latter age a superior female intensity, in the proportion of *six* to *five*; which indeed should not, after the *thirty-fourth* year, re-appear until the *sixty-fifth*, nor then continue so elevated any longer than a few years. The present remarks are in accordance with enlarged experience, evinced by the analysis of a

great many tables of mortality, brought under a comparative point of view, in all their particulars.

169. Ninth: Because, regarding either of the two criticised tables, the series of Specific intensities q_x, resulting therefrom, — or preferably the corresponding series of logarithms λq_x, the question being of geometric proportions which the expressions of intensity bear to each other, — render conspicious, on proceeding to analyze, by deducing from such respective series various orders of their successive differences, that all notion of regular progression, in connecting with each other those quantities λq_x, or their elements, has been unthought of or disregarded; thus manifesting the absence of controlling principles whatsoever, in the construction of those tables, from materials employed in a most crude state.

170. Tenth; Because a numerical maximum of the periodic deaths, — which, considering the reference to a superior class of selection, happens not very inaccurately to be rendered apparent at the 71st completed year of age for the Male sex, — is made to correspond with the completed age of 78 years as regards the Female, and then in an unwarrantably disproportionate excess over the former maximum, or that of male deaths; whilst in fact the latter, taking place even as late as the 71st year, precludes for the other sex the occurrence of a corresponding event later than the 75th. The contradictory character of those statements is obvious; inasmuch as it will immediately strike the observer, that if any given quantity of either sex, and existing at *seventy-one* years of age, produces *three* deaths within the next succeeding year, the necessarily much reduced quantity of the other sex and having outlived the more advanced age of *seventy-eight* years, — admitting equal quantities born of both, — could not, with even the smallest probability, produce

four deaths; which excess in the proportion of three to four, or thereabouts, is actually rendered apparent by those tables.

171. Eleventh: Because it is there stated, as outliving the 91st year of age, a quantity *six* times greater of the female than of the male sex; a disproportion which, only three years later, is made to extend to *ten* times more female than male survivors; and again, three years further on, to upwards of *twenty* times more of the one than of the other. The excess of female survivors had already been presented in those tables, and referably to *eighty-four* years of age, as extending to twice the quantity of males, this even constituting a most inadmissible disproportion; whence any further commentary, under this head, is uncalled for.

172. Twelfth and last: Because the vacillating progression of each series, that express the Specific intensities of life at successive years of age relatively to the respective sexes, proclaims a lamentable estrangement from any sort of settled principles, that should have guided and controlled the computation of tables intended for application to enlarged and public purposes, whilst laying claim to so imposing a sanction as that of the legislature. In the progressive quantities set forth by those tables, as well as in the natural deductions from them, a mathematical regularity, founded upon admissible principles, and due harmony between the various parts, not less than between each part and the whole, were not any thing short of indispensable requisites.

173. Each of the above-stated objections is forcible; and when taken collectively, they may be expected, in the judgment of scientific men, to outweigh even the authorities upon which the tables alluded to are at pre-

sent received. Without adverting therefore to objections of a minor description, it is safely to be pronounced, that any computations, which from those tables might be made of the values of contingent sums depending on human life, must in a greater or less degree be remote from accuracy; and that any professed tabulation of values, so grounded, could not fail to exhibit series of quantities unwarrantably disproportionate, with still greater disproportions and inaccuracies in the comparative valuations referred to the discriminated sexes.

174. The adoption of any principle, or method, implies the acceptance of all its possible consequences. Had Mr. F.'s attention been but for a moment arrested on one single consideration, — that an enormous and utterly inadmissible excess of nearly *six years*, in the average duration of female life over that of the male, became the unavoidable result of his other admissions, — he could not have failed to perceive many of those errors made the subject of the present chapter; and he must have shrank from seeking the sanction of a British parliament, to an assemblage of unharmonious and incorrect results, deduced from his undigested data.

CHAPTER XXI.

Of the Comparative quantities of Births, Male and Female.

175. This important question, of the comparative quantities of births belonging to each sex, has undergone frequent discussion, without precise result; and it requires to be solved from data ascertained on an extensive scale. The proportions which those quantities bear with each other are variable, according to time, place, and circumstance; the latter being apparently connected with some physiological cause, assignable only as more or less probable, from repeated coincidences of similar or analogous results equally traceable to such assumed cause. It may be remarked, that in France, in Prussia, and in some other countries, — where no inconsiderable portion of the male population has been periodically consumed by protracted and destructive wars, — the births of that sex have occurred in proportions more elevated, comparatively with the female births, than in countries wholly exempt from, or in less degree obnoxious to a like circumstance; and it is further remarkable, that the births in wedlock also take place, universally, in a more elevated proportion as to the males compared with the females. It is therefore likely, that some natural cause may operate to the same effect in both instances; and before inquiring into that cause, it will be proper to establish the results of the best authenticated data in our possession.

176. A general understanding, derived however from

data of great uncertainty, is that in Great-Britain the male births are to the female in the proportion of about 22 to 21, exactly corresponding with what appears to have taken place in France at a period not very far removed from the present; for we are informed by Mr. Milne, that on an average of the three years, 1800, 1801, and 1802, the superority of male births was there in the proportion of 1·0477. The same author states, with reference to experience in England and Wales, during 40 years ending with 1810, that the male births were as 1·042 to *one* of the female, being nearly as 25 to 24; and Mr. Nicander states nearly the latter proportion, or 1·04595, with reference to Sweden and Finland, during 20 years' observations ending with 1795. At the same time it is ascertained, by experience of the last twenty years or more in France, that marriages, there, produce *sixteen* male births to only *fifteen* female; that the illegitimate births of the respective sexes, occur in nearly the same proportion as the general births formerly did; and that all births, indiscriminately considered, have been comparatively as *seventeen* males to *sixteen* females, or very nearly in that proportion.

177. The decennal returns of births, deaths, and population, throughout the extent of Great-Britain, fail to supply a satisfactory solution of the above question, relatively to this country; the returns of baptisms and of burials, — besides their being incomplete, — omitting the distinction of sexes, and inasmuch as the returns of population, at the expiry of each decennal period, though introducing that distinction, are justly suspected of error. A discrimination of the sexes, referably to the births and to the deaths, through some mode independent of the church-registers of baptisms and of burials, — which are very far from completely accounting for the two former, — would be conclusive, as also of easier attainment

than correct data by a direct enumeration of the population of both sexes. We must therefore again resort to the public records in France, for complete, correct and authentic data; which with their compared results, towards a solution of the proposed question as regards that country, are as hereafter.

178. Those records, for the fourteen years commencing with 1817 and terminating with 1830, convey the following information:

YEARS.	MALE births.	FEMALE births.	PROPORTIONS of the male births' superiority		AVERAGED EXPERIENCE, from the commencement.		
			Each year.	Average of 5 years.	Male births.	Female births.	Male superiority.
			LEGITIMATES.				
1817	456 570	425 002	1·074277	"	456 570	425 002	1·074277
1818	456 717	429 489	1·063396	"	913 287	854 491	1·068807
1819	475 651	446 606	1·065035	"	1 388 938	1 301 097	1·067513
1820	460 463	432 121	1·065588	"	1 849 401	1 733 218	1·067033
1821	463 069	432 803	1·069930	1·067612	2 312 470	2 166 021	1·067612
1822	465 274	437 774	1·062818	1·065303	2 777 744	2 603 795	1·066806
1823	460 807	433 552	1·062864	1·065240	3 238 551	3 037 347	1·066243
1824	471 490	441 488	1·067957	1·065832	3 710 041	3 478 835	1·066461
1825	468 151	436 443	1·072651	1·067244	4 178 192	3 915 278	1·067151
1826	474 837	445 883	1·064936	1·066246	4 653 029	4 361 161	1·066924
1827	469 209	440 219	1·065854	1·066850	5 122 238	4 801 380	1·066826
1828	465 745	440 098	1·058252	1·065922	5 587 983	5 241 478	1·066108
1829	460 887	434 289	1·061245	1·064589	6 048 870	5 675 767	1·065736
1830	461 756	436 838	1·057042	1·061487	6 510 626	6 112 605	1·065112
			ILLEGITIMATES.				
1817	31 887	30 666	1·039816	"	31 887	30 666	1·039816
1818	32 261	30 725	1·049992	"	64 148	61 391	1·044909
1819	33 660	32 001	1·051842	"	97 808	93 392	1·047284
1820	33 915	32 434	1·045662	"	131 723	125 826	1·046866
1821	34 552	32 934	1·049129	1·047336	166 275	158 760	1·047336
1822	35 820	33 928	1·055765	1·050525	202 095	192 688	1·048820
1823	35 710	33 952	1·051779	1·050881	237 805	226 640	1·049263
1824	36 280	34 894	1·039720	1·048382	274 085	261 534	1·047990
1825	35 381	34 011	1·040281	1·047278	309 466	295 545	1·047103
1826	37 061	35 410	1·046625	1·046790	346 527	330 955	1·047052
1827	36 098	34 670	1·041188	1·043906	382 625	365 625	1·046496
1828	35 924	34 780	1·032892	1·040163	418 549	400 405	1·045314
1829	35 276	34 075	1·035246	1·039284	453 825	434 480	1·044525
1830	35 241	34 029	1·035617	1·038366	489 066	468 509	1·043877

179. The following further results are deduced from the above stated data:

YEARS.	PROPORTIONS of the male births' superiority, generally.			PROPORTIONS of the legitimate to the illegitimate births; the latter being represented by *unity*.		
	Each year.	Average of the last five years.	Average of the whole experience.	Each year.	Average of the last five years.	Average from the commencement.
1817	1·071958	—	1·071958	14·09320	—	14·09320
1818	1·062501	—	1·067206	14·06989	—	14·08151
1819	1·064153	—	1·066158	14·04574	—	14·06922
1820	1·064197	—	1·065668	13·45286	—	13·91043
1821	1·068459	1·066227	1·066227	13·27493	13·77849	13·77849
1822	1·062310	1·064322	1·065567	12·94729	13·54786	13·63164
1823	1·062059	1·064229	1·065064	12·83855	13·30198	13.51268
1824	1·065888	1·064581	1·065169	12·82741	13·06212	13.42162
1825	1·070311	1·065803	1·065744	13·03599	12·98229	13.37739
1826	1·063589	1·064831	1·065523	12·70467	12·86917	13.30543
1827	1·064053	1·065152	1·065387	12·85084	12·85008	13.26244
1828	1·056417	1·064056	1·064633	12·81176	12·84470	13.22353
1829	1·059372	1·062742	1·064228	12·90790	12·86062	13.19889
1830	1·055491	1·059800	1·063603	12·97234	12·84805	13.18250

180. Those results, deduced from incontrovertible facts collected on a large scale, establish that the male births constantly occur in quantity superior to that of the female; that the proportion of the former births' superiority is not permanent, but fluctuating under a dependance on some variable and perhaps ascertainable cause; and that this cause, whatsoever, has continued to operate with a progressive decrease of intensity, throughout fourteen years of the latest recorded experience in France. The same results also establish, that the superior proportion of male births is much greater in respect to those taking place in wedlock, than it is amongst the illegitimate; which remarkable circumstance indicates probable identity between a cause permanently operating, in the latter case, and the cause which in the former produced a regularly progressive reduction of such male superiority. It is further remarkable, that the proportion of this superiority, amongst the illegitimate births, has undergone only slight and irregular variations, partly ascribable to

the smaller compared quantities; leaving the results more under the dominion of chance, in this, than in the other case. Adverting to the commencement of this chapter, where warlike circumstances have been pointed out as probably determining an increased proportion of superiority in the male births, it is seen that such probability has derived support from the additional fact of a deviation from the regularly progressive decrease of that superiority for the years 1824 to 1827, which period exactly coincides with the event of an army having been, a year or two previously, raised in France for the invasion of Spain; and those various circumstances, together with the announced inferences from them, are in perfect accordance with the principal fact, fully established with reference to all times and to all places, *i. e.* that the males, whose lives are of more precarious tenure, and whose Absolute intensity of life measures at least *three* years less than the absolute intensity of female life, are at the same time born in quantity superior to that of the females; thus shewing Nature's constant tendency to maintain or to restore a requisite equilibrium between the sexes. Let us now recall those statements, from which our argument take its departure.

181. Admitting, at each stage of the fourteen years' experience, average results of the last *five* years, in order to obviate inevitable irregularities produced by the fortuitous events of specific years; it is found, in the distinct case of legitimate births, that, during the years 1817 to 1821, those of the male have exceeded those of the female sex, as 1·067612 to *unity;* being in a proportion even superior to *sixteen* of the former, compared with *fifteen* of the latter: a proportion ultimately, or on averaging the five years 1826 — 1830, reduced to 1·061487, which is even inferior to that of 17 compared with 16. It is also found, in the distinct case of illegitimate births,

that the first five years have averaged a superiority as 1·047336 to *unity*, or nearly as 22 to 21; whilst the ultimate and equal period exhibits a superiority expressed by 1·038366, or nearly as 27 to 26. And lastly it is found that all those births indiscriminately considered, whether in or out of wedlock, have taken place in the proportion of 1·066227 male to *one* female, or rather less than 16 of the former to 15 of the latter, in respect to the first five years of the experience; which proportion of superiority has, for the last similarly averaged period, been reduced to 1·0598, or as 17·7 to 16·7.

182. Having regard also, at each stage of that Experience, to average results from its commencement to the periods successively arrived at, it is otherwise found, that amongst legitimate births the superiority of males has been originally 1·074277, or nearly as 14 1/2 to 13 1/2, and ultimately 1·065112 or nearly as 16·4 to 15·4; further that amongst illegitimate births, the superiority has gradually increased during the first half of the period to 1·049263, or nearly as 21 1/2 to 20 1/2; thence decreased during the other half, to 1·043877, or nearly as 24 to 23; and lastly that all births without distinction, which had for the first year exhibited 1·071958 as the proportion of male superiority, or nearly as 15·to 14,' have ultimately yielded that of 1·063603 only, or about 16 3/4 to 15 3/4, as an average result of the whole fourteen years' experience. It is then very likely, that in case of a renovated state of continental warfare, the excess of male births over the female, in France, would re-ascend to the proportion of 14 1/2 compared with 13 1/2, as in the specific year 1817, if not become still more elevated; and those results of experience confirm the highly probable hypothesis, that any greater relative quantity of population, either male or female, when compared with that of the opposite sex, — and admitting those only of both who exist at ages fitted for procreation,—

will tend to elevate the future proportion of births among the sex in which such relative quantity is the least.

183. During the same fourteen years' experience in France, the male population has increased by 1 377 754, excess of the births over the deaths, whilst the female population by 1 079 187 only; and if we admit the statements in our 90th paragraph, — subdividing the population of that country, in the year 1817, into 14 463 252 males and 15 414 782 females, — it will appear that the excess of the latter, over the population of the former sex, was reduced in the year 1830 to 652963 individuals; which excess, in the quantity of females, extended to 951530 individuals thirteen years previously. It is further observable that, relatively to the then existing quantities of each respective sex, the male's increase has been in the proportion of *six* to *five*, compared with that of the female by such excess of births over deaths among the latter.

184. Another point worthy of being considered, and on which the last three series stated in the 179th paragraph convey accurate information, is, that during those fourteen years' experience in France the relative quantity of illegitimate births, compared either with the legitimate or with all births generally, has constantly increased for the first *ten* years; after which, and for the last *four* years of that experience, such relative quantity has slightly decreased. Regarding each year individually, the proportion in 1817 was *one* illegitimate to 14·09320 legitimate births; the latter quantity reduced in 1826 to 12·70467, and this raised in 1830 to *one* illegitimate birth compared with 12·97234 births in wedlock. An average of the first *five* years yields the proportion :: 1 : 13·77849, and that of the last *five* the proportion :: 1 : 12·84805; whilst the general average is :: 1 : 13·18250, for the whole *fourteen* years' experience.

185. Towards a comparison of the preceding, with analogous results for the population of Great-Britain, we fail to be possessed of the requisite data. From such however as are accessible, through the decennal returns under parliamentary authority, a few valuable inferences may be deduced. Adopting the principle, — that in case either of a stationary or of a progressive population, in stated amount, the respective quantities of each sex, though not ascertained, are determinable with near approach to the truth, by combining two elements only, *i. e.* the relative quantities of periodic births, respectively male and female, and the relative measures of life's Absolute intensity in each sex; — it has accordingly been proceeded, in the 90th paragraph, to subdivide into respective totals of male and female the established population of France in the year 1817. The statements in the 91st paragraph have then shewn, — consequently to the periodic increase of those respective totals, by the births' excess over the deaths for each sex, — that the population of that country, in the year 1830, consisted of 15 841 006 males and of 16 493 969 females; those quantities being in the proportion of 1·04122 to *unity*, and expressing the relative superiority, in number of the latter sex, at the close of fourteen years' experience. Admitting on the other hand, in order to proceed conformably with the above-mentioned principle, average results of the first seven years of that experience; the Absolute intensity of male life has been found 33·84929 years, whilst 1·065064 the proportion of superiority as to the births of that sex, and the corresponding intensity of female life has also been found 37·42147 years; whence the quotient of this quantity, divided by the product of the preceding two, indicates 1·03800 as a proportionate excess of the female population over the male; and the latter quantity differing so little from 1·04122, or the proportion of excess manifested with reference to the year 1830, it may safely be concluded

that any possible errors, which might be consequent on the computation, partly proceeding from hypothetical admissions, must be circumscribed within very narrow limits. Then, considering 1·04 to be a very probable expression of the female population's excess over the male, in France, we have to compare with it the following results, deduced from official returns respecting Great-Britain, as far as their accuracy may be relied on :

YEARS.	MALE POPULATION.	FEMALE POPULATION.	RELATIVE QUANTITIES OF FEMALES.
In 1800	5 450 292	5 492 354	1·00772
In 1810	6 340 214	6 269 650	0·98887
In 1820	7 137 018	7 254 613	1·01648
In 1830	8 161 618	8 375 780	1·02624

186. Notwithstanding the discrepancies of those relative quantities; and observing only that the female superiority of numbers here appears to have proceeded by increase, whilst in France it has been obviously proceeding by decrease; it is on the whole perceptible, that our female population exists in less excess than the female population of that country, over their respectively male populations. Further considering the quantity of female births, compared with that of the male, to be rather more considerable in Great-Britain than it is in France; it follows, that the above-stated proportions inferior to 1·04, could not result from any other cause than an inferior standard of female life's Absolute intensity or average duration, in the former country, comparatively with that intensity in the latter. Whatever increase, therefore, such intensity may for sometime past have generally obtained in England,

it may be considered almost certain that its female population has failed to partake of it in a corresponding proportion; whilst it is highly probable that life's Absolute intensity for both sexes indiscriminately considered, in this country, remains inferior to its present standard in France.

187. The manifested proportions of superiority in the male births, over the female, must partly depend on the comparative quantities existing of each sex, not only amongst the whole population, but also amongst the males and females within certain intervals of age. In which point of view, it is remarkable that the Law of Mortality relative to an entire and considerable population,— exemplified by that of France, in which the sexes however are discriminated, and admitting *seventeen* male births to *sixteen* female, — represents very nearly equalized quantities of survivors at *twenty-one* completed years of age, amongst the former, as also at *fifteen* years amongst the latter; and it is further remarkable, that compared according to the same law, as also under a similar admission, the quantity of males living between *twenty-one* and *fifty-nine* years of age, and the quantity of females living between *fifteen* and *fifty-three* years, — both those intervals of age supposed preferably eligible, — are likewise found very nearly alike. But it must always be understood, that those remarkable results are expressly referable to a Stationary population, from which condition the population of France is considerably divergent; the data being wanting, towards a precise ascertainment of its actual distribution in that case. As any present divergency, from a distribution referable to the former case, ought to have a corresponding operation in regard to both sexes, the apparently excessive superiority of male births, compared with the female in that country, should be chiefly imputable to a greater or less disturbance, also, of

equilibrium between the existing numbers male and female, either within the above-stated intervals of age, or within any other best appropriated to the intercourse of sexes; and to such a law of nature is, doubtless, to be referred any observable disproportions between the quantities of periodic births of each sex in other countries.

188. The question may be worth a more diligent investigation than shall here be attempted: — Whether or not, among the many admirable fitnesses of means to Nature's final purposes, an equilibrium of the populations is maintained consequently to each sex being collectively supplied with a nearly equal quantum of vitality; reciprocally counterpoising the respective products of the births multiplied into any standard of life's intensity referred to certain intervals of age, and involving an adequate allowance for such variations of that intensity as depended on accidental modifications in the general conditions of human existence? — Further, may it not be, that in such providential dispensation, any disproportion in excess of quantity, as to the living of either sex in particular, and within certain limits of age, should determine with greater or less proximity a more elevated proportion of births of the other sex? — Again, to what cause should be ascribed a very remarkable difference of proportion, as to the births divided between the contradistinguished sexes, when those births are referred to the wedded state, or else considered in its absence? These are indications to be presented only in their greatest generality; and the conjectures to which they lead, in respect to sufficient causes, are not devoid of support from positive data, together with their results exhibited in the present chapter.

189. A gradual reduction in the proportions of male births' superiority over the female, in France, has been stated in the 178th and 179th paragraphs, as also shewn

to coincide with successive periods more and more removed from the last at which that country continued in a state of destructive warfare. The proportion of that superiority, stated at 1·071958 for the year 1817, is not unlikely to have been even more elevated at preceding periods, when the male youth were periodically decimated; and it is not unlikely that a protracted peace would further abate from the considerably reduced proportion at the close of the recorded experience. Inferring from those premises, that the quantities of each respective sex are mutually sufficient for each other, so long as the equilibrium adverted to in the 187th paragraph is maintained; it is easily conceivable that, on such equilibrium being disturbed, Nature calls forth all the resources capable operating its re-establishment. Observing that the excess of male births falls to a *minimum*, in the special case of illegitimacy, — being then the result of vitality's probably greater exaltation in the male sex than in the other; — the reversed effect may from analogy be admitted, as probably attending the case of any material subtraction from the quantity of male population, within the limits of age best appropriated for reproducing the species. Suppose any extraordinary circumstance, which on the contrary had the effect of periodically subtracting any considerable quantity amongst the female population, between the *sixteenth* and *fortieth* years of age; it becomes probable that the comparative quantities of births would, after a year or two from the origin of such influential cause, be manifested under an aspect tending gradually to restore the deficient quantity of that sex. A longer experience of correct records in France, than is yet possessed, and the aid of comparative experience in some other countries, would better enlighten this question of the true proportion between the births of both sexes; but which clearly appears subordinate to variable circumstances.

190. The proportion which the quantity of illegitimate births bears to the legitimate, or else to the whole, is a matter of no unimportant question; and that proportion, depending on many causes, is also subordinate to variable circumstances. There exists, on public record, no data whatsoever towards solving that question as regards Great-Britain; but those data are completely obtained for France, as stated in the 178th and 179th paragraphs. The proportion now under consideration is there exhibited, respecting that country, by an uninterruptedly decreasing series, from *one* illegitimate birth comparable with 14·09320 births in wedlock, during the year 1817, to *one* comparable with 13·18250 of the latter, on an average of fourteen years' experience, terminating with 1830. The first *five years* of that period, being averaged, yield the proportion of *one* to 13·77849; gradually reduced to 12·84805 legitimate births, comparable with *one* illegitimate, on an average of the last *five years*, or from 1826 to 1830. Much regularity has also attended the decreasing proportion, even for each successive year individually considered, during the greater part of the period observed upon; but during the last few years a slight increase appears to have taken place, the proportion being as *one* to 12·97234 for the year 1830. It should be borne in mind, that the proportion of which we are speaking is more or less influenced, among other causes, by the distribution of any population; which distribution, when this is progressive, becomes modified from what it is with respect to any population of a stationary character, though in equal number; admitting the Absolute and the Specific intensities, together with all other circumstances, to be alike in both cases. The continued and increasing preponderance of youthful population may, concurrently with other causes, have occasioned the illegitimate births periodically to increase, in France, from being rather less than *one fifteenth* part, to a proportion even exceeding *one fourteenth* of all

births indiscriminately; and that special cause, to which the increase is partly referable, has probably operated with still greater effect in this country, where the population has increased by *one-fifth*, during the same interval of time producing in France the increase of its population in the of ratio *one-twelfth* part only. The proportion of illegitimate births to the whole, in the metropolis of France, is considerably more elevated than any amongst those above-stated; further to observe upon which could lead to no useful result. There is little reason to doubt, that in England, and especially with the inferior classes,—amongst whom less moral importance than in France apparently attends the circumstance of illegitimacy,—the proportion of births out of wedlock would, upon investigation, be found comparatively greater than it is in the latter country.

191. We have hitherto limited our consideration to the comparative births of children *alive*, distinctly of each sex. But observations at Paris, during the *eight* years 1824 to 1831 inclusive, shew that the *still-born* of the Male sex have been in excess, over the Female, in the proportion of *six* to *five*; and this, together with other corresponding experiments, should be admitted to possess its due weight towards establishing, as regards the whole, a nearly correct proportion between the respective quantities of infants destined to be born of each sex. There appears then to exist some unknown cause, operating with a high degree of energy,—as also exclusively depending on the difference of organization between one sex and the other,—which occasions, even previously to parturition, the destruction of male infants preferably to the female; a cause partly retaining its original intensity during the first subsequent year, but progressively attenuated, from that period until the completion of a *fifth* or *sixth* year of age, when the intensity of that cause becomes a *minimum*.

192. Analogous observations have been made by Mr. Mourgue, at Montpellier, as also by the late Mr. Wargentin in Sweden; and it were desirable that they had been further extended. The former has found 346 still-born of the male sex, and 269 of the female; whilst the latter, 1455 males comparable with only 1079 females of the said description; such respective quantities accompanying others of infants born alive, both male and female, equally proceeding from certain given quantities of marriages. Considering only the superior quantities of males over that of females, amongst the still-born, the proportion of that superiority appears to have been more elevated according to the experience at Montpellier, and still more so according to that of Sweden, than by the result of observations at Paris; at the same time as each of those proportions, supplied by direct experience, is considerably more elevated than that of the superiority of males born alive, over the female, either in France or elsewhere.

193. There remains to establish in that respect, and as far as such limited experience may admit, the influence of those very elevated proportions of still-born Males; towards modifying the proportion previously discovered to have taken place amongst the children born alive of both sexes. Thus we find : —

	STILL-BORN.			BORN ALIVE.			INDISCRIMINATE Conceptions.		
	Males.	Females.	Proportions.	Males.	Females.	Proportions.	Males.	Females.	Proportions.
Paris, 8 years. .	7075	5886	1·20200	119378	114902	1·03895	126453	120788	1·04690
Montpellier. . . .	346	269	1·28625	11200	10514	1·06525	11546	10783	1·07076
Sweden.	1455	1079	1·34847	46981	45318	1·03670	48436	46397	1·04395

194. The respective quotients resulting from a division of those superior proportions of *conceptions*, by the corresponding and inferior proportions of superiority amongst the males actually born alive, are for Paris 1·00765, — for Montpellier 1·00517, — and for Sweden 1·00699; the average of all which, or mean quantity of the increased superior proportion amongst all males over all females born either alive or otherwise, is 1·0066; amounting to *one-tenth* part of the proportion of male's superior number as stated in the 179th paragraph, consequently to this adjunction of the still-born of both sexes. Some observations in England, by Dr Bland and Clarke, as quoted by Mr. Milne, yield the proportion of 580 male to 395 female still-births, quantities equally corresponding with *ten thousand* births alive; whence the superior number of the former appears to be 1·46835, compared with *unity* of the latter; an excess greater indeed than was manifested even in Sweden.

195. The proportion of still-born individuals, compared however with those born alive, depends much on the circumstances by which the period of gestation may be accompanied. In this respect, the offspring of illegitimate connexion generally stand at a disadvantage; and it is observable that, at Paris, — where illegitimate births occur in a fivefold proportion, compared with those throughout France at large (*), — the relative quantity of still-born nearly doubles what it has proved either at Montpellier or in Sweden. But as the tables of mortality, deduced from the Montpellier experience, limit the Absolute intensity of life to 25·29 years, — shewing the population of that place to exist under very unfavourable conditions, especially in early life, — the proportion there exhibited, of the still-

(*) This disproportion is accounted for by the convenience Paris affords, of lying-in hospitals, and of a foundling hospital where all infants are admitted without an inquiry; which renders that metropolis a place of general resort.

born to all other births, should not be admitted to guide the object of our present calculation. The value apparently possessed by the remaining experiment, or that of Sweden, where the life-intensity makes a near approach to its standard both in England and France, may then be admitted as the least objectionable. Hence, and until a supply of data more conclusive is obtained, it may be considered that any superior proportion of male births over the female, both understood alive, should be increased in the ratio of 1,00699, being rather more than the mean result of the three sets of observations; in order to obtain a nearly correct expression of the male superiority, in respect to the Conceptions of both sexes. Consequently, and reverting to the statements in the 178th and 179th paragraphs, we find: instead of 1·063603, the proportion 1·071038 of male superiority, or about 15 to 14, admissible in respect to all births indiscriminately in France, on an average of the fourteen years' recorded experience; and instead of 1·059800, the proportion 1·067208 of that superiority, being as 15 3/4 to 14 3/4, equally admissible as an average result of the last five years of that experience. Regarding the births in wedlock, particularly, the corresponding proportions to be admitted become 1·072577, instead of 1·065112, or very nearly as 14 3/4 to 13 3/4 on a general average of those fourteen years; as also 1·068907, instead of 1·061487, or very nearly as 15 1/3 to 14 1/3, on an average of the last five years 1826 — 1830; and lastly, regarding the illegitimate births in particular, the admissible proportions, on a general average of the experience, should be 1·051174, or rather more than 21 males to 20 females, instead of 1·043877; as also 1·042856, or the proportion of 24 1/3 to 23 1/3, instead of 1·035617, on an average of the last five years.

CHAPTER XXIII.

Of the quantities of Periodic Marriages, compared with the Population.

196. The proportions according to which, comparatively with any quantity of population at the time being, marriages are contracted during an Annual or any other period, depend on many combined circumstances. Some of these, relating to conditions under which the individuals in greater or less number are understood to exist, amongst an entire population, may be only transient; but a circumstance of paramount influence, on those proportions, is the actual distribution of any given quantity of population, into subordinate quantities of the living at specific years of age, or else within certain intervals of age, as to each sex; and it has already been observed upon the differences of that distribution, in contradistinguishable cases, — of a stationary population, — of one progressively increasing, — and of another progressively decreasing. The ratio of either progression, as also the period during which it may have continued, both exert their respective influences in modifying the distribution of which we are speaking. Admitting the continuance of a progressive increase, such as occurs amongst the populations under our present consideration, the relative quantity of periodic marriages, compared with the population; must — all other circumstances supposed the same — decrease so long as the accession of infants, below the age fitted to

a married state, shall exceed the due proportion of corresponding accession as to individuals attaining that age under the hypothesis of a stationary population; and the contrary, or an increased relative quantity of marriages, must commence taking place, whenever the still progressive population shall so far have abated its ratio of increase, as to produce a preponderate accession of individuals entering that fitted age. There simultaneously exists, therefore, two causes arising from the same source, yet mutually counteracting their respective operations, whilst the increase of population is not entirely discontined; from which follows, that under the last-mentioned circumstance, the quotients of any population divided by its periodic marriages, and expressing relative quantities of the latter, shall exhibit, from each period to the next, a constantly decreasing series, until an ultimate quotient corresponds with the permanent distribution belonging to a stationary state.

197. Let us now resort to the recorded experience, ascertaining its results under the operation of those influential causes; and first, from the data supplied in France, we have:

YEARS.	MARRIAGES of each specific year.	QUOTIENTS of the population, by the marriages of those years respectively.	MARRIAGES of each five consecutive years.	QUOTIENTS of the united populations of five years, by the corresponding marriages.	MARRIAGES during periods of years successively protracted.	QUOTIENTS of the united populations, by the marriages corresponding with those periods.
1817	205 244	145·5732	—	—	205 244	145·5732
1818	212 979	141·2061	—	—	418 223	143·3493
1819	215 088	140·7388	—	—	633 311	142·4627
1820	208 893	145·8693	—	—	842 204	143·3077
1821	221 868	138·1872	1064 072	142·2400	1064 072	142·2400
1822	247 495	124·7357	1106 323	137·7057	1311 567	138·9369
1823	262 020	118·5791	1155 364	132·7228	1573 587	135·5451
1824	231 680	135·0629	1171 956	131·7143	1805 267	135·4849
1825	243 674	129·3200	1206 737	128·7805	2048 941	134·7518
1826	247 194	128·1904	1232 063	126·9681	2296 135	1 4·0454
1827	255 738	124·5236	1240 306	126·9096	2551 873	133·0912
1828	246 839	129·7789	1225 125	129·2694	2798 712	132·7990
1829	248 796	129·3185	1242 241	128·1987	3047 508	132·5149
1830	270 435	119·5665	1269 002	126·1438	3317 943	131·4595

198. The preceding statement shews that the proportional quantities of marriages, relatively to the population, are subject to great variations when referred to specific years in succession; this being consequent on the alternations of abundant and deficient crops, and likewise on other circumstances qualified as prosperous or adverse: all which have, at the time being, a considerable influence on the determination towards marriage. With regard to France in particular, the state of war, or even a mere anticipation of approaching war, has usually the effect of increasing the quantity of marriages at the time of such occurrences, as affording the male youth a cause of exemption from military service; whence during the years 1822 and 1823, — the invasion of Spain then being in progress of execution, — as also in the year 1830 on the apprehension of impending war, marriages were considerably more numerous than in either the immediately preceding or succeeding years; thus disturbing the progressive decrease, otherwise observable, of the series of quotients resulting from an annual division of the quantity of population by the quantity of marriages. By admitting average results, each of *five* consecutive years, the proportions which the marriages in France have borne to its population, form a series decreasing with very little interruption, from *one* marriage compared with 142·2400 individuals, being a result of the first *five* averaged years 1817-1821, to *one* marriage amongst 126·1438 individuals only, during the last *five* years terminating with 1830; and by admitting, each year, results generally averaged from the commencement of the experience in 1817, when the proportion of marriages was found to be *one* in 145·5732, the series of subsequent proportions has gradually decreased to *one* marriage amongst 131·4595 individuals, being an average result of the whole experience of fourteen years duration.

199. Comparing the foregoing results, with those of the same description and deduced from the decennal returns relative to the forty counties of England, it is found, as Mr. Rickman has stated them, that the ten years terminating with 1800 have averaged *one* marriage to 123 inhabitants; that the ten next succeeding years averaged *one* marriage to 122; the ten subsequent years, *one* to 127; and the last ten years, ending with 1830, *one* marriage to 129; a general average, according to those returns, having yielded *one* marriage to each 125 1/4 individuals, amongst the existing population of England at the time being. Supposing that those data were sufficiently correct for all purposes of the present comparison, it then would appear that the relative quantities of marriages in England continued rather decreasing, whilst those relative quantities in France considerably increased, as to corresponding periods of observation; which comparative circumstances, with reference to what has been set forth in the first paragraph of this chapter, indicate — regarding the population in England, — a periodic accession of infants below the marriageable age, to be still preponderating over the corresponding accession of individuals to that age, whilst the reverse has occurred in France; and those opposite results should naturally be consequent on the British population continuing rapidly to increase, at the same time as the French population no longer increased in so elevated a ratio as before. The same comparative circumstances supply another valuable indication; *i. e.* that the marriages in England have generally occurred in relative quantities superior, when compared with its population, to the relative quantities of marriages in France; whence is inferable, that any ascertained increase of the Absolute intensity of life, in England, should be attributable in greatest part to more numerous and to earlier marriages than in France, with less influence of any amelioration as to the general condition of the people to the same effect; whilst, in the latter

country, the ascertained increase of life's intensity should chiefly be attributed to improved circumstances, and less than in England to the increased number of periodic births. Mr. Rickman's statements however shew, — regarding the county of Essex in particular, where the observations appear to have been carefully directed, — that during the four periods corresponding with those of the decennal returns for all England, the marriages have successively occurred as *one* in 125, *one* in 130, *one* in 146, and *one* in 154 individuals; which considerable reduction in the proportions of periodic marriages in Essex, renders the preceding remark still more applicable to that county than to the generality of England. Again the increased intensity of life throughout France, as evinced by our statements in the 91st and next succeeding paragraphs, is clearly seen to have benefited its male population in a greater proportion than its female; which doubtless should be solely ascribed to the conversion of a state of warfare into another of peace, enjoyed during a period of fifteen years.

200. With reference always to a stationary population, it is found, amongst other results attending female life's superior intensity to that of male life; first, that according to the Law of Mortality applicable to France, and notwithstanding the great excess there ascertained of male births over the female, the quantities of survivors at *eighteen* years of age become equalized for both sexes; and secondly, that the males at all ages from 18 to 60 years, as also the females at all ages from 15 to 53,— both which understood in very nearly equal numbers under the above hypothesis, — should then exhibit a quantity of couples, either married or marriageable, amounting to *ten* times the united annual births of both sexes; the quantity of marriages, in each year, thence being in the proportion of *one* to about 36 of

those couples, or very nearly the same as the annually renewed proportion of the whole population. But in its progressive state, the equilibrium of those various proportions is disturbed; and then the quantity of marriageable females shall be, over the quantity of males similarly circumstanced, in a greater or less excess, depending on any degree of the population's proving divergent from a stationary condition. Such divergency being at present more considerable in England than in France, the disproportion, in excess of marriageable females, must be superior in the former country; and to this circumstance, perhaps, may be ascribed the inexcusable arrogance of young men in these days, together with the not less extraordinary departure from female dignity in the other sex, who tolerates such presumptuousness on occasions of contemplated matrimonial connexion.

201. In the foregoing attempt at ascertaining any proportion which the annual quantity of marriages may, according to late experience, have borne to the population, it has been omitted to discriminate between marriages susceptible of becoming fruitful, and those in which the female parties should from advanced age be supposed incapable of obtaining issue. Assuming the age of *fifty-three* completed years, as an utmost term of female fruitfulness, the experience presently to be stated will shew that *eighteen* marriages in every *thousand* are to be considered as contracted above that age. The writer of these pages has gathered with the utmost care, from the registries of 121525 marriages at Paris, during the eighteen years 1813-1830, the precise ages of all female parties who thus contracted; and the comparative quantities of marriages at each year of age, referred to *one million* of those at all ages, are accordingly exhibited under the following aspect; after methodically correcting, for the purpose of generalized application, the incidental

irregularities of progressing quantities. It were desirable to have obtained analogous information extending to marriages in the country; but the means failed of securing a requisite accuracy of the results.

COMPLETED years of age.	DISTRIBUTION of 121525 marriages, according to direct expérience.	CORRESPONDING distribution of one million marriages.	IRREGULAR differences, of the progressive increase or decrease.	CORRECTED distribution.	REGULARIZED differences.	TOTALS.
				M.	Δ M.	Σ M.
12 to 15	811	6669	+ 9134	6669	+ 9134	6669
16	1920	15803	16775	15803	16775	22472
17	3959	32578	13276	32578	15276	55050
18	5816	47854	9394	47854	9394	102904
19	6957	57248	5439	57248	5439	160152
20	7618	62687	3287	62687	3293	222839
21	8017	65974	— 1888	65980	— 1785	288819
22	7788	64086	4794	64195	3962	353014
23	7206	59292	3209	60233	4027	413247
24	6815	56083	2921	56206	4006	469453
25	6461	53162	4411	52200	3950	521653
26	5924	48751	3937	48250	3863	569903
27	5446	44814	3197	44387	3747	614290
28	5058	41617	4192	40640	3607	654930
29	4548	37425	3625	37033	3447	691963
30	4107	33800	3761	33586	3271	725549
31	3651	30039	2473	30315	3082	755864
32	3350	27566	3768	27233	2884	783097
33	2892	23798	2288	24349	2682	807446
34	2614	21510	2938	21667	2479	829113
35	2257	18572	1851	19188	2275	848301
36	2032	16721	1922	16913	1963	865214
37	1798	14799	1695	14950	1696	880164
38	1593	13104	1831	13254	1471	893418
39	1370	11273	874	11783	1277	905201
40	1324	10899	1633	10506	1112	915707
41	1126	9266	918	9394	970	925101
42	1015	8348	1251	8424	848	933525
43	862	7097	559	7576	743	941101
44	795	6538	321	6833	653	947934
45	755	6217	387	6180	574	954114
46	709	5830	967	5606	548	959720
47	591	4863	37	5058	583	964778
48	586	4826	1028	4475	592	969253
49	462	3798	383	3883	548	973136
50	415	3415	502	3335	411	976471
51	354	2913	+ 49	2924	319	979395
52	360	2962	— 576	2605	238	982000
53	290	2386	189	2367	206	984367
54	267	2197	276	2161	204	986528
55	233	1921	65	1957	211	988485
56	226	1856	325	1746	220	990231
57	186	1531	445	1526	224	991757
58	132	1086	53	1302	224	993059
59	125	1033	+ 4	1078	215	994137
60	126	1037		863		995000
61 etc.	578	4756		5000		1000000

202. The further ascertainment in our next chapter, of an average quantity of births attributable to each marriage, — together with previously ascertaining the Absolute intensity of life, as also any proportion between the respective quantities of legitimate and of illegitmate births, — may enable to establish, with nearer approach to certainty than through the medium of the series stated in paragragh 193[d], the proportion that should be expected to appear, between the periodic marriages and any given quantity of population, when stationary; admitting always the maintenance of those conditions of existence whence the ascertained measure of such Absolute intensity resulted.

CHAPTER XXIII.

Of the Average quantity of Births, attributable to each Marriage.

203. The average quantity of births, assignable to each marriage, is a question which seems to have been at all times beset with difficulties; and those who entertained that question have arrived at results not only materially diverging, but often irreconcilable with established facts, besides resting on considerations very superficial, if not fallacious. The well-directed observations on this subject have been few. The authentic data collected in France, within the last sixteen years or more, afford however very valuable materials towards solving that question, with reference to a special but very extensive locality; and in the absence of corresponding data from elsewhere, on a scale capable of being contrasted with those materials, the results inferred from them may justly be admitted for generalized application. When that experience shall be further enlarged, so as nearly to equalize the annual proportions of recent marriages, concurring with the rest to produce any quantities of births within similar intervals of time, — which proportions have been greatly disturbed consequently to the increasing population, — it may be expected that the question before us will obtain as accurate a solution as could possibly be expected.

204. The average of births, to each marriage, does not

appear very considerably to differ, between any one country of Europe and another. Early marriages, as also moral habits, concur to elevate such average quantity; and this is not ascertainable with any approach to accuracy, when — as the case occurs in England — the legitimate and the illegitimate issue are blended into an indiscriminate mass, whilst the baptismal registries are misunderstood correctly to represent the births. An increasing population determines a more elevated proportion of early marriages, and therefore of corresponding births; both which circumstances are consequent on the proportion of youthful population — in the distribution of the whole — being then superior to what it is in a stationary population; and an apparent decrease of the births, compared with the marriages, will follow any diminution of the ratio according to which the population progressed. The latter of those results is exemplified by the statements hereafter.

205. The data supplied in France, by fourteen years experience terminating with 1830 — being the latest returns,—are with their results as follows; first comparing the legitimate births during each year, with the marriages of the same year.

YEARS.	MARRIAGES during each year.	BIRTHS during each year.	AVERAGE births to each marriage.	MARRIAGES during five consecutiue years.	BIRTHS during five consecutive yaars.	AVEBAGE births to each marriage during five years.	PERIODIC averages of births, from the commence-ment.
1817	205 244	881 572	4·29524	—	—	—	4·29524
1818	212 979	886 206	4·16100	—	—	—	4·22688
1819	215 088	922 257	4·28781	—	—	—	4·24757
1820	208 893	892 584	4·27293	—	—	—	4.25386
1821	221 868	895 872	4·03786	1064 072	4478 491	4·20882	4·20882
1822	247 495	903 048	3·64875	1106 323	4499 967	4·06750	4·10314
1823	262 020	894 359	3·41332	1155 364	4508 120	3·90191	3·98828
1824	231 680	912 978	3·94069	1171 956	4498 841	3·83874	3·98217
1825	243 674	904 594	3·71231	1206 737	4510 851	3·73806	3·95007
1826	247 194	920. 720	3·72486	1232 063	4535 699	3·68139	3·92581
1827	255 738	909 428	3·55609	1240 306	4542 079	3·66206	3·88876
1828	246 839	905 843	3·66977	1225 125	4553 563	3·71681	3·86945
1829	248 796	895 176	3·59803	1242 241	4535 761	3·65127	3·84729
1830	270 435	898 594	3·32277	1269 002	4529 761	3·56955	3·80454

206. But, as the births of any one year could not properly be referred to the marriages of that year, a rather nearer approach to correct results will be obtained, consequently to comparing the quantity of births in each year with that of the marriages during the year immediately preceding. Hence we find: —

YEARS.	MARRIAGES	YEARS.	BIRTHS.	AVERAGES of one year.	MARRIAGES of five years.	BIRTHS of five years.	AVERAGES of five years	PERIODIC averages.
1817	205 244	1818	886 206	4·31786	—	—	—	4·31786
1818	212 979	1819	922 257	4·33027	—	—	—	4·32416
1819	215 088	1820	892 584	4·14986	—	—	—	4·26496
1820	208 893	1821	895 872	4·28867	—	—	—	4·27084
1821	221 868	1822	903 048	4·07020	1064 072	4499 967	4·22901	4·22901
1822	247 495	1823	894 359	3·61364	1106 323	4508 120	4·07487	4·11289
1823	262 020	1824	912 978	3·48438	1155 364	4498 841	3·89387	4·00823
1824	231 680	1825	904 594	3·90450	1171 956	4510 851	3·84899	3·99492
1825	243 674	1826	920 720	3·77849	1206 737	4535 699	3·75865	3·96918
1826	247 194	1827	909 428	3·67901	1232 063	4542 079	3·68656	3·93794
1827	255 738	1828	905 843	3·54207	1240 306	4553 563	3·67132	3·89827
1828	246 839	1829	895 176	3·62656	1225 125	4535 761	3·70228	3·87431
1829	248 796	1830	898 594	3·61177	1242 241	4529 761	3·64644	3·85287

207. It being unquestionable, that the quantities of marriages and of births, at any particular period, are both subject to the influences of good and of bad crops *, as also of other accidental circumstances; any observable progression, whether generally increasing or generally decreasing, of the proportions between those corresponding quantities referred to successive years distinctly considered, must be expected considerably to fail of regularity; whence the foregoing series of those proportions, so referred, should be discarded from consideration, as incapable of leading even to an approximate ascertainment of the true average of births appertaining to each marriage at any time being.

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* The influence of favourable and of unfavourable harvests, on the quantity of births during a next succeeding year, has been demonstrated by M. Milne, Actuary of the Sun life-office; and Dr. Villermé, of Paris, has established their corresponding effects on the marriages.

If therefore we admit, as on former occasions, a series of results in regular succession and each averaging *five* consecutive years, to be the safest guide in this research, it appears that such series of average births assumes in its progressive decrease sufficient regularity for being entitled to confidence; and that, owing to causes already assigned, the decrease has proceeded — not without remarkable rapidity — from 4·22901, an average referable to the first five years of the recorded experience, even down to 3·64644, being a corresponding average referable to the last five years; whence a reduction as : : 7 : 6, or thereabouts, within an interval less than ten years. It may be remarked, however, that during the last five years of such interval, the variations between those stated averages have been nearly insignificant; from which is inferable that an approach is now making towards such an average as a stationary population should exhibit. Let it further be remarked, that although an analogous series stated in the 205th paragraph has been discarded, it nevertheless deserves notice under another point of view, as it is perceptible that each two corresponding series of averages should very nearly coincide in case of a Stationary population; whereas those series generally preponderate in the ultimate statement.

208. From those various considerations, as also that such series of averages had not entirely discontinued decreasing when the experience closed, a very small abatement in the last expressed quantity 3·64644, arbitrarily reducing it to 3·625, or *three and five-eighths* births to each marriage in France under the actual conditions of its population's existence, should in all probability approach nearly to a correct average which is our object in the present inquiry. Yet the motive for preferring those elements of computation which are stated in the 206th paragraph might be susceptible of a more extended operation, causing the

terms of each series to require on the contrary some small addition; and then the correct average would come nearer to 3·66667, or *three and two-thirds* births, instead of *three and five-eighths* only. Hence the question is left undecided between those two results.

209. With reference to a period already fifty or sixty years removed from the present, the late Mr. Duvillard's researches concluded to the adoption of *three and a-half* births, assignable on an average to each marriage in France; but as such ascertainment appears to have been only a secondary object with him, — besides that his data were collected in Towns, exclusively of the Country, — some doubt may be entertained as regards the accuracy of that conclusion by a rather rounded quantity. It is further observable, on this occasion, that the same author found *one* marriage to every 112 individuals of the population at that period; therefore the marriages, proportionally more numerous there than at present, in all probability took place at less early ages, and must have been rather less productive.

210. When investigations of this nature are proceeded upon, it is proper to guard against a prevailing propensity to admit, merely for saving trouble, the general average of numerous sets of results afforded by protracted experience. Thus the general average 3·85287, of births to each marriage during the whole period of fourteen years' recorded experience in France, should be understood as considerably more elevated than any true average referable to the present, or probably to any other period. The influence of such elevated but delusive averages, as are exhibited by the first few years of that experience, — when the marriages were in comparatively inferior quantity, must long continue to present a

fallacious proportion, expressed by the ultimate term of the series; and it is only after that influence shall have been neutralized, by long lapse of time, that the general average may nearly coincide with any one relative to a short period, such as the last consecutive *five* years. So long as the population continues to increase, the antecedent marriages will contribute in a decreasing proportion, comparatively with those of more recent date, to any actual quantity of periodic births; whence the quotient of that quantity, divided by any actual quantity of marriages during the corresponding period, must continue also to express averages in greater or less excess over the real. On the whole, it is obvious that the quantum of average births, appertaining to each marriage, depends not less than many other general results on the aggregate conditions — more or less favourable or unfavourable—under which the population referred to may exist. Let us now consult the analogous results of a few other well-directed observations.

211. Mr. Mourgue, at Montpellier, has found 21714 Births *alive* to result from 5926 observed Marriages, thus yielding 3·66419 to each marriage; which last quantity does not materially differ from an average of the last five years' experience throughout France. On the other hand, the late Mr. Wargentin's experience, relative to the population of Sweden, has shewn 92299 births *alive* to have proceeded from 24073 marriages; yielding 3·83413 births to each of the latter. This last average, more elevated than any ever found in England or in France, may be ascribable to a superiority of moral habits amongst the Swedish population; which advantage its extended dissemination sufficiently accounts for. Hence the latter average, more roundly expressed by *three and five-sixths* births to each marriage, may be considered as a *maximum* generally referable to a set of favourable circumstances; whilst *three and two-thirds*

the more probable average at present, as also *three and one-half* a comparative *minimum;* either of which quantities preferably applicable, according as the contradistinguished cases may require for a complete surety in any contemplated transactions.

212. For further comparison, with the preceding results of extensive and indubitable experience, we do not find any other to rest upon sufficiently authentic data; and regarding analogous results deducible from the population-returns in Great-Britain, they are contradictory with each other, as also divested of value, from its having been omitted to discriminate between the legitimate and the illegitimate births. The decennal returns closing with the year 1800 yield the proportion of 3·57901 Baptisms, compared with each marriage; those closing with the year 1810, the proportion of 3·80403; those closing with the year 1820, the proportion of 3·85125; and lastly, the returns closing with the year 1830 exhibit the proportion of 3·75944 baptisms; an average of all which proportions is 3·74843. But *births* and *baptisms* are things very different. Even assuming their identity, as also the stated quantities both of the latter and of the marriages to be correct and respectively complete, there would still be to abate from that general proportion a quantity corresponding with the still uncertain ratio of the illegitimate births. We have seen that, in France, the latter have not, at any time of the recorded experience, been less than *one-fifteenth* part of all births indiscriminately; whence 3·74843 would be reducible to 3·49853 legitimate births referred to each marriage, whilst in all probability a more considerable reduction should take place, leaving an utterly inadmissible *minimum* as the result. There does not appear any sufficient reason for supposing that the proportion of illegitimate births, throughout the British dominions, were inferior to what it is in France; the contrary indeed

being rather inferable from the laxity of moral principle, in that respect, amongst our inferior classes. On the other hand, even the last-mentioned resulting quantity should the more be inferior to any correct standard referable to this country, as therei sscarcely any doubt of its marriages being in some degree more prolific than those taking place in France, where the increase of population has proceeded in a less elevated ratio.

213. But it has been shewn in the preceding chapter, that about *eighteen* marriages, in every *thousand*, are contracted by females at such advanced ages as to preclude the expectation of issue. If therefore the total quantity of births in wedlock be compared with the total of marriages within the limits of *fifty-three* completed years of age, as to all female parties, the *maximum* of average births, attributable to those marriages exclusively, would become $\frac{3{\cdot}83333}{{\cdot}982} = 3{\cdot}90360$; the *medium* quantity of births would become $\frac{3{\cdot}66667}{{\cdot}982} = 3{\cdot}73388$, and their *minimum* $\frac{3{\cdot}5}{{\cdot}982} = 3{\cdot}56415$.

214. Having now three important data, referred to the actual and indiscriminate population of France; — *first* the Absolute intensity of life, expressed by 35·87957 years (see the 79th paragraph), and also indicating the amount of relative population compared with the equalized births and deaths of each year, under the hypothesis of that population being stationary; — *secondly* the average quantity 3·666667, of births assignable to each marriage (see the 211th paragraph); — *third* and lastly, on a general average of the last fourteen years' experience, the proportion of births in wedlock to be $\frac{131825}{141825}$ of the whole

(see the 179th paragraph); all which data thus ascertained with the utmost attainable approximation to the truth; we are thence enabled further to ascertain, also by approximation in a satisfactory degree, the relative quantity of annual marriages that should occur in France, supposing that its population became stationary, and the present conditions of its existence to remain unchanged. By multiplying into each other the above-specified quantities, we find that, under the premised suppositions, *one* marriage should take place amongst 122·2823 individuals in the whole population. Comparing this last quantity with 126·1438, the ultimate term of a corresponding and decreasing series in the 197th paragraph; it follows, that the present proportion of periodic marriages is susceptible of a small decrease only, for bringing it to the standard referable to a stationary population.

215. The corresponding results of official returns, in Great-Britain, do not materially differ from those last-mentioned; but the relative quantity of its youthful population must preponderate over that of France, in their respective distributions, consequently to the increase of population having proceeded more rapidly in the former country; whence the marriages probably take place rather earlier, and yield issue in a rather superior proportion.

CHAPTER XXIV.

Of ascertaining the quantities of Births, attributable to marriages contracted by females at each specific age.

216. The purposes of an intended Institution, alluded to in the Preface of this book, required not only that the quantity of births assignable to each marriage, according to a general average, should be ascertained with all possible accuracy, but also that corresponding ascertainments should be obtained, with distinct reference to each year of age at which the females might contract such marriage. The means of solving this difficult question are much to be simplified, without vitiating the results, by leaving out of consideration the male party's specific age; which, in all cases, may be assumed to exceed by *six* years that of the female, towards establishing with sufficient approximation the probabilities of their joint-lives, being one amongst the necessary elements of computation. Having premised thus much, the following method has been proceeded with.

217. Admit x, as before, to represent a series of completed years of age, from 16 to 52; all which being respective *minima*, any of those ages will be correctly expressible by $x + 0{\cdot}5$, as a mean quantity; and further admit a_x, a series of ages assumed to correspond with the utmost term of fecundity, extending by equal intervals from 40·5 years, for females marrying under *seventeen* completed,

to 52·5 years for those who married at this latest admitted age, the term of their fecundity then supposed to be outrun. Another series f_x, made to correspond with the successive years of age signified by x, shall thus exhibit 37 periods of fecundity decreasing by an arithmetic progression; attributing a 24 years' continuance of that faculty to the earliest of those ages, which term is gradually reduced to *zero*. Those respective periods have reference to certain *maxima* of age, generally expressed by $a_x + 0{\cdot}8$, and assignable as the latest of parturition; being 41·3 years with regard to the earlier marriages, as also 53·3 years regarding the latest assumed capable of having issue; the diminution of only *two-third* parts of a year being allowed to attend each advance of a full year, in the actual ages, from considering that early child-bearing has a tendency sooner to exhaust the reproductive powers, and to multiply the chances of accident susceptible of destroying the aptitude to procreate.

218. The years of *virtual* fecundity, generally expressed by that series f_x, are next convertible, according to the probabilities of two lives' joint-continuance, into quantities more or less reduced, of years assumed to be average periods of the *effectual* or productive fecundity belonging to females at their respective ages x; and towards this conversion, the age of the male being always understood as represented by $x + 6$, an application is proper of the Law of Mortality referable to the respective sexes, as also to a class not inferior in quality to that of Assurable-lives, inasmuch as marriage is always presumable to take place amongst no other than the healthy. A new series F_x will thus be produced; its respective terms corresponding with those of the preceding series. Without further entering into the details of complicated calculations, it may be sufficient for the present purpose to state that such new series exhibits a first term F_{16}, expressing about 20 years'

effectual, substituted for 24 years' *virtual* fecundity; the subsequent terms gradually decreasing to 0·25, or *one-quarter* of a year, and being a term F_{52} corresponding with any interval of female age above 52 completed years, until entrance into another year. It is observable, however, that such series F_x required a methodical adjustment of its differences ΔF_x, the regularity of which must have been in some degree disturbed by the irregular operation of the Law of Mortality, introduced as a requisite element.

219. Consequently to this mode of proceeding, any given quantity of legitimate births discontinues its reference to any specific quantity of marriages; the former becoming co-relative with the series F_x, expressing the years of fecundity collectively appertaining to those marriages, according to their distribution announced in the concluding paragraph of chapter XXII.

220. A further series g_x, consisting of the successive products $F_x \times M_x$, establishes the several quantities of years' fecundity collectively contributed by each year of age at which the marriages are contracted; and the sum of those products, generally expressed by Σg, is found (by the actual computations) amounting to 14 153 171 years of that fecundity understood to be contributable by *one million* of marriages at all ages, or more properly by 982000 marriages contracted within the limit of 53 years of age; whence $\frac{14\,153\,171}{0{\cdot}982} = 14{\cdot}413$ should be the quantity of years' fecundity corresponding with 3·666667 average Births to each Marriage, or 3·9308 years to each birth *alive*; and it is also found, that those 14·413 years correspond between F_{26} and F_{27}, thus indicating that the marriages of females at 27 years of age yield the same

average of births as all marriages indiscriminately under the age of 53 completed years.

221. A last series n_x, formed of successive quantities generally expressible by $\frac{F_x \times 3{\cdot}666667 \times 0{\cdot}982}{\Sigma g}$, exhibits the various quantities of births respectively assignable, on an average, to each marriage contracted at the specifically corresponding ages signified by x; whence it further appears, that an average of 5·1322 births appertains to the earliest marriages, whilst only a fraction 0·0636 to the latest within the understood limits of age; those quantities of average births, independently of the *still-born*, being susceptible of distribution into male and female, according to their recognized proportions. Should any other general average of births to each indiscriminate marriage be admitted, preferably to the quantity 3·666667, the various averages n_x shall then be modifiable accordingly.

222. Although the question, of an average quantity of births assignable to each marriage contracted at any specific age of the wife, may hitherto have been prejudged insoluble; it is now seen that its solution is attainable, with sufficient accuracy for all practical objects.

223. With a view to the same intended Institution, further computations from the foregoing data, as also from an application of the appropriate Mortality-tables hereafter introduced, have the result of ascertaining, with reference to the time of marrying at any specific age, a present value of equal sums supposed to be due or forthcoming at the expiry of each succeeding year, the quantity of which is generally expressed by F_x, such equal instalments substituted for the uncertain periods of births

in their generality; moreover ascertaining a common period, — found to be *eight years and two months* remote from the date of marriage, — at which those sums might equitably be resolved into a single payment, admitting the rate of interest at *four and a half per centum per annum*.

CHAPTER XXV.

Of FIVE CLASSES, *both Male and Female, to be discriminated in any population.*

224. The object of consideration now before us is that of various classes susceptible of being discriminated amongst any extensive population, with the view to apply a general Law of Mortality under its appropriate modifications corresponding with those respective classes; and the chief purpose of such application is to regulate, on equitable terms, all pecuniary contracts understood to involve a correct appreciation of the chances of life. The relative superiority, or the relative inferiority, of any specific class contradistinguished from any other, results from a comparison of the Absolute intensity of life, as measured with reference to each class in particular, and also with the distinction of each sex; which measure of intensity shall have been ascertained by adequate, enlarged, and digested experience.

225. An Absolute intensity more elevated, than its standard referable to the indiscriminate population, is manifested in minor extent amongst a class of persons generally fulfilling the conditions required for admission to an insurance of their lives. Towards ascertaining such intensity of life, referred to that class, the experience supplied in Great-Britain has been in some degree extensive; but from its hitherto excluding all consideration of the lives under *ten* completed years of age, a necessity

has arisen to complete the tables resulting from an investigation of the data thus supplied, by admitting, as regards the earlier ages, such results as harmonized in proportions to correspond with those of experience obtained amongst the other classes.

226. A still more elevated degree of superior intensity, compared with its general average, is manifested amongst a class including the Life-annuitants and Tontine-nominees; all whom, from the circumstances of their existence, and from a more effectual exclusion of defective lives than is obtained amongst the aggregate of Assurables, reunite in a higher degree those conditions requisite for constituting a select class. Compared statements of crude facts, observed at various times and places amongst the life-annuitants and tontine-nominees, have — though liable to much correction in order to reconcile their inconsistencies — supplied, on the whole, very valuable and probably sufficient data, towards ascertaining not only the Absolute, but also the Specific intensities of those lives at their successive years of age.

227. But there is further to discriminate a class, amongst which the Absolute intensity of life is even superior to that of the two preceding. Though incapable of immediate exemplification, by individuals in very considerable number congregated together, it is nevertheless requisite to assume the virtual existence of such a class, however disseminated, and describable as consisting of comparatively *Perfect* lives; towards supplying, from its especial consideration, sets of corresponding tables that should secure either the State or private associations, as occasion offered, against eventual loss arising from individual speculations, so directed as possibly to defeat public objects; or else to answer any other purpose. Supposing, for example, a numerous collection of lives otherwise

select; and that, amongst those only, any part were to be considered at the precise period of their contracting marriage; or supposing a transaction such as occurred during the last century, in which the French government contracted to grant annuities depending on the limited number of *thirty female lives*, carefully chosen amongst the inhabitants of Geneva; it is certain that, in neither of those cases, the contingencies depending on lives so described could be adequately valued by applying tables of mortality exactly corresponding even with the general class of life-annuitants and tontine-nominees, than which no one superior has been at any time taken into consideration.

228. A *fourth* class, consisting in the aggregate population, indiscriminately considered, of any considerable country or district, is thus sufficiently described; and the Law of Mortality then applicable will be such as chiefly to answer statistical purposes, or otherwise to afford the requisite security in transactions of a public nature, when the individuals, on whose lives the valued contingencies are made to depend, shall be distinctly understood superior or inferior to general lives; according as the contract may then be, either to receive the certainty against the contingency, or else to receive the contingent sums in exchange for the unrestricted disbursement.

229. Regarding all classes of inferior lives, it is sufficient to discriminate one only; being a *fifth*, composed of individuals who, — though existing under a set of conditions generally less favourable to the preservation of life and health at all ages, than those characterizing the existence of any population at large, — may nevertheless, and consequently to mutual agreement, become the object of pecuniary transactions, relative to contingent sums depending on their various chances of life and of survivorship. This class, whose condition is still remote from

one of abjectedness, are mostly the object of Institutions abounding throughout Great-Britain, under the denomination of *Benefit-societies;* and it is of paramount importance that the laborious and provident, amongst that class, should be dealt with on terms of perfect equity, which can only be secured by applying to all transactions with them, of a contingent description, such a modification of the general law of mortality as may be found sufficiently appropriate.

230. Let us now recapitulate, regarding both Males and Females of those different classes, the conditions of existence considered as best characterizing them respectively.

231. Suppose any collection of individuals to possess in common the following qualifications: — *First*, an original constitution and conformation both exempt from defect, each individual ascertained to proceed from healthy parents, as also not to have been prematurely born; — *Second*, a presumable non-liability to the Small-pox, whether from any undoubted preservative, at least against its appearance in a dangerous character, or from having overcome that disease; — *Third*, circumstances in all probability affording the permanent means of sufficient and wholesome subsistence, as also of proper care towards the maintenance of health, especially during infancy; — *Fourth*, habitually to reside on a salubrious soil, with the benefit of pure air and of wholesome waters; — *Fifth*, exemption from employments susceptible of endangering life, or obviously tending to abridge it; — *Sixth*, the unquestionable enjoyment of mental health; — *Seventh*, to be of moral and temperate habits; — *Eighth*, freedom from anxious cares, and from sedentary occupation attended with excessive exercise of the mental faculties; — *Ninth*, to continue, if in very advanced age, the same diet and mode of living that led to such age; — *Tenth*, abstention from long voyages by sea, and from

other voyages obviously perilous, as also from changes of climate that should probably impair the general health; — *Eleventh*, actually perfect health at any special period selected for consideration, such as when admitted a nominee to any life-annuity, or in case of other transactions of a pecuniary nature, that should require to apply, regarding the individual, an appropriate modification of the general law of mortality; — *Twelfth* and last, that the casualties of War, Famine and Pestilence, were understood not to exert any influence on the rates of mortality, amongst the aggregate individuals otherwise circumstanced as above. It is certain that any collection of persons, re-uniting those conditions, would constitute the very first of all classes describable as Select, out of any considered population; and for practical purposes, the existence of such a class must necessarily be assumed.

232. Admitting, amongst the above-enumerated conditions of existence, that a few—though not positively excluded, — were merely neglected to be taken into consideration, as mostly escaping observation; there still would remain a set of such favourable conditions, as should be quite applicable to a *second* class of selection, usually falling under the collective description of Life-annuitants and Tontine-nominees; although many purchasers of annuities made to depend on the event of their lives' continuance, as also many sharers of tontine-speculations, may fail to unite all the conditions here supposed generally to qualify that class.

233. Should there further be discarded from consideration a few more of those conditions, essentially qualifying the first select class and in greatest part retained for the second; absolutely insisting on no other than the 2^{d}, the 5th, the 6th and the 10th, with the 11th more or less mitigated, the 3^{d} condition being implied from the

nature of the transaction, and the 12th generally assumed; a *third* class will thence arise, still participating in the advantage of selection amongst the whole population, as that class expressly excludes all individuals existing under circumstances especially unfavourable. Such third class is appropriately denominated of *Assurable lives*, with which indeed a very considerable proportion of the population is susceptible of being assimilated.

234. The class taking rank as the *fourth* qualifies itself from an aggregate of all the circumstances under which any extensive population may actually exist; and accordingly, it stands characterized by the measure of life's Absolute intensity, expressed by the proportion of such population's periodic renewal in case of its being stationary; or otherwise expressed by a geometric proportional between the diverging quotients, of the population distinctly divided by the periodic births and by the periodic deaths, in case of its being progressively increasing or decreasing. The Law of Mortality referable to an indiscriminate population doubtless affords ample security in its application to the transactions of life-insurance societies, and generally to transactions of all societies receiving periodic premiums or other contributions contingent on the endurance of lives qualifiable as select, in exchange for contracts to pay definite sums at periods either certain or uncertain; though it could not consist with the requisite security of such public institutions, to admit the contingent sums, thus receivable, according to valuations founded upon an application of mortality-tables strictly referable to the classes of people dealt with. Great inconvenience attends the usual practice of life-insurance societies who preferably compute from the *Northampton* tables, which apply only to lives of a very inferior description; considering that a double error of no inconsiderable magnitude is thence generated: first, by materialy undervaluing the contingent

premium of insurance, and secondly by inferring a more proximate period than the probable one at which the insured sum should be disbursed; whilst any supposed remedy, consisting in the promise subsequently to restitute a certain portion of the excessive profit, must be ineffectual, as such restitutions, — in the shape of a *bonus* or in any other shape, — are inevitably regulated upon doubtful principles, as also according to arbitrary proceedings foreign to the spirit of such contracts.

235. The *fifth* or inferior class, alluded to in the 229th and 235th paragraphs, necessarily excludes all Male individuals of the military and naval professions, as also a considerable mass of people so disadvantageously circumstanced in social order, that they are inevitably shut out from the benefit of reciprocal contracts. The lives of this class, in their generality and independently of discriminating the sexes, are represented with great approach to the truth, by the united mortality-tables of Duvillard, — referred to the population of towns in France at a former period, with liability to the Small-pox, — and of Dr. Price for the population of Northampton towards the same period; those tables differing little more than from the former's attributing, to lives under 56 years, Specific intensities rather superior to those expressed by the latter, which on the contrary admits rather superior intensities above that age.

236. If it were inquired, respecting any probable distribution of the population, into relative quantities of each class; it would be, as regards the present population of France, in the following proportions, or thereabouts. Amongst every *hundred*, in the whole quantity, *one* of the first class, *nine* of the second, *fifty* of the third, and *forty* of the fifth joined with any still inferior and rejected classes; the fourth forming a general average. Those unimportant indications, however, are given without

pretension to great accuracy, being only the result of calculation on more or less unsettled grounds; besides that differences, from the above proportions, should inevitably become apparent with reference to the contradistinguished sexes, as also to the various ages, and that the operation of time further tends to disturb more or less those proportions.

CHAPTER XXVI.

Of the Law of Mortality, modified relatively to the Five *classes before described; distinguishing the Male from the Female; and qualifying each class, of those respective sexes, by the measure of life's Absolute intensity represented under the corresponding modifications.*

237. It has been observed, in the 68th and in the 149th paragraphs, that the measure of life's Absolute intensity, ultimately rendered apparent by any Law of Mortality, should be determined previously to attempting the construction of such a law; which may then be proceeded with, according to the principles and method set forth in chapters XVIII and XIX. The general law which it is the present purpose to establish, relatively to entire populations without distinction of particular classes, and though exemplified by a class rated the *fourth* in successive order, demands a prior consideration to that of any one amongst its eligible modifications. With this understanding, it is further to be premised, that a Law of Mortality would be likely to fail answering the purpose of an enlarged application, if such law were constructed on the exclusive grounds of data referable altogether to any special locality and to a state of things there existing at an exclusive period. It has been seen that the facts on public record in France, during a long series of years, are the only source whence data indisputably correct could be obtained, towards discovering the law's leading features; whilst any analogous experience, afforded by returns

concerning all movements of the British population, has, — from an incomplete system of public records, and from the inconsistency of their announced results, — proved utterly incapable of supplying data on which a reliance could be placed. At the same time it is apparent, on the grounds explained in the chapters III and XI, that the Absolute intensity of life in England is in some degree inferior to its measure in France, ascertained by indubitable experience. It appears on the other hand, and by statements in the 79th paragraph, that such intensity in France had not progressed by increase beyond the first half of the observed period, after which it continued vacillating by inconsiderable differences; denoting, on the whole, that the intensity of life in that country had probably attained its *maximum*, with indications of subsequent decline; whilst the progressive increase, during a first part of the recorded experience, should be ascribed to many successively favourable crops, together with improved circumstances of the population, consequently to a protracted state of peace and total absence of calamitous events.

238. Premising those considerations; and observing that it could not consist with the present object, to set forth, for general application, a Law of Mortality constructed from data referable to an extreme case; as also in order to meet the concomitant circumstances, — of a rather inferior standard of life's intensity in England compared with that manifested in France, and of a commenced reduction there, from the maximum of such intensity extending to full 36 years referably to an average of the *five* commencing with 1821; — it has been conceived preferable to adjust the Law of Mortality, intended for construction, with a standard of life's Absolute intensity represented by the population of each sex in France, on an average of the four year's experience 1817 to 1820, both inclusive. By the statements in paragraph 94th, the averages corresponding

with that period are found to be 33·41621 years for the Male, as also 37·09767 years for the Female sex; and by a very near accordance with those quantities, the constructed Law of Mortality represents on one part 33·4583 and on the other part 36·9583 year's Absolute intensity, or average duration of life; establishing precisely a difference of *three years and a half*, in excess of the Female's over the Male's. If it were at any time desirable to modify the law thus constructed, either elevating or reducing to any other standard the resulting intensities of male and of female life, the process of computation to that effect would not be very difficult; consisting only of raising or lowering each term of the series q_x in equal and adequate proportions, which is to be accomplished by either adding or subtracting equal quantities, to or from each of the corresponding $\lambda\, q_x$; the application of which method may however require a few successive trials for completing the adjustment. In all transactions between individuals, the valuation of contingent sums depending on lives or on survivorships, — when no sufficient motive arises for entering into any distinction of classes, — may with great equity be computed from the Law of Mortality thus constructed; which is hereafter detailed under the *fourth* class, and modified according to a due discrimination of the sexes.

239. Regarding the *inferior class* of lives; which, in its generality, appears to obtain a fair representation through jointly considering several tables constructed, — by Dr. Price with reference to the town of Northampton, — by the late Mr. Duvillard, and applicable to the towns in France, — as also by Mr. Mourgue, from his observations on the population of Montpellier with discrimination of the sexes; — those modifications of the law, which are adapted to the lives comprised in a *fifth* class, have the result of expressing an Absolute intensity, or average duration, respectively of *twenty-six years and a half* for the Male sex and of *thirty*

years and a half for the Female; thus admitting, between the one and the other, a difference of *four* years, which Mr. Mourgue in particular has ascertained to exist in an analogous case. Those results have been determined after numerous attempts at reconciling the discrepancies observable in the tables above alluded to, with due attention to maintain the requisite harmony in respect to all other admitted modifications of the Law of Mortality, and to all corresponding expressions of life's Specific intensity at each year of age. Hence the tables accordingly introduced, and referred to that *fifth* class, may be considered especially applicable to all pecuniary transactions between public institutions and the individuals it comprises; when contingent sums, the receipt of which should depend on the endurance of such lives, are intended for reduction to a present value.

240. The results in the same manner brought out by the adopted modifications of a general Law, in their reference to the *three* classes described as select, may not require — after what has already been explained concerning those comparative classes — any further elucidation, than merely to state the following leading features of that law, under those of its modifications regarding the different sexes of each class.

241 To the *first* select class, or that of lives making a near approach to physical perfection — on considering the present state of civilized countries, — an Absolute intensity, expressing the average duration of life, has been extended to 45·1 years for the Male sex, and to 47·9 years for the Female; the difference, in favour of the latter, being thus limited to 2·8 years. And it is presumable that complete security, through an application of the modified Law of Mortality yielding those results, would in all cases be afforded, either to Governments or to Public institutions

whatsoever, on their granting life-annuities, or contracting for any other contingent sums made to depend on select of lives, and receiving in exchange a present value of those contingencies.

242. To the class standing *second* in the order of selection, namely the class of Life-annuitants and Tontine-nominees, — all lives otherwise susceptible of assimilation with them being included, — the resulting Absolute intensity considered in the greatest generality of such lives, is 41·9764 years for the Male and 44·9130 years for the Female sex. And all transactions of a contingent description, between private individuals, — when the contingent sums, reducible to a present value, are depending on the continuance of lives that obviously fall under the present description, — may with great equity be regulated by applying a corresponding modification of the Law of Mortality, distinctly referred to the one and to the other sex of that *second* class.

243. The leading results brought out by those modifications, of a general Law, which distinctly refer to males and to females of the *third* select class, or that of lives who fulfil only the requisite conditions for being admitted to life-insurance, are 37·4781 years as regards the Males, and 40·6259 years as regards the Females; respectively expressing, with every correctness a careful investigation of the supplied data could admit, the Absolute intensity of life or its average duration amongst that *third* class.

244. From duly considering all difficulties attendant on the analysis of data that involve — as to the *third* class — many omissions, and exclude the distinction of sexes, it has been a principal object, in providing that distinction, to maintain harmonious proportions with those established

relatively to other classes, regarding the Specific intensities of life referred to successive years of age and to each sex respectively.

245. The following tables exhibit the Law of Mortality, under its modifications referred to the five classes of each sex; such as those classes have been defined, in the present and in the preceding chapter.

246. Consequently to limitations at present unavoidable, those tables are much curtailed; reduced indeed to mere skeletons, consisting only of *two* principal series. These are: First, the Decrement of Life, as defined in chapter V; observing that, in the original, the respective quantities are extended to *nine* places of decimals, which here are contracted into *seven*: Secondly, the Specific intensities of Life, as defined in *chapter* XVI and essentially constituting the Law of Mortality. All the developments of — and deductions from — that law, are omitted; but those two principal series are strictly sufficient for enabling to obtain any others; and all deductions may, for the present, be supplied by any Actuary willing to take the requisite trouble.

THE LAW OF MORTALITY,

UNDER ITS MODIFICATIONS REFERRED TO THE DISCRIMINATED SEXES OF FIVE CLASSES;

ADMITTING, IN THOSE MODIFICATIONS, EQUAL QUANTITIES OF BIRTHS;

AND STATING, IN EACH CASE,

THE **DECREMENT OF LIFE**, OR PROPORTIONS OF INDIVIDUALS WHO ATTAIN THE SUCCESSIVELY INDICATED YEARS OF AGE,

WITH THE **SPECIFIC INTENSITIES OF LIFE**, OR RATES OF MORTALITY DURING EACH YEARLY INTERVAL.

MALES.

Completed Years of Age.	First Class, or Perfect Lives. Decrement.	First Class, or Perfect Lives. Intensities.	Second Class, or Life-Annuitants. Decrement.	Second Class, or Life-Annuitants. Intensities.	Third Class, or Assurable Lives. Decrement.	Third Class, or Assurable Lives. Intensities.	Fourth Class, or Indiscriminate Population. Decrement.	Fourth Class, or Indiscriminate Population. Intensities.	Fifth Class, or Inferior Lives. Decrement.	Fifth Class, or Inferior Lives. Intensities.
0	1·0000000	7·5975	1·0000000	6·7904	1·0000000	5·7799	1·0000000	4·8705	1·0000000	3·9877
1	8683781	14·7807	8527334	13·2105	8269833	11·2445	7946803	9·8927	7492278	7·6281
2	8096273	26·3137	7881836	25·5183	7534395	20·0183	7143500	18·1591	6510080	13·8045
3	7788590	43·1404	7546700	38·5574	7158019	32·8193	6750115	30·3593	6038488	23·6221
4	7608030	65·5475	7350973	58·5841	6939915	49·8656	6527774	46·5898	5782860	38·0230
5	7491981	92·8857	7225496	83·0181	6800743	70·6633	6387663	66·1412	5630772	57·0021
6	7411323	123·5424	7138461	110·4187	6704501	93·9855	6291087	87·5421	5531990	78·6226
7	7351332	155·2064	7073811	138·7181	6633166	118·0741	6219223	108·8698	5461628	98·8884
8	7303968	185·3456	7022817	165·6556	6576988	141·0027	6162098	128·2110	5406398	113·5261
9	7264560	211·7322	6980423	189·2390	6530343	161·0764	6114036	144·0961	5358776	120·4410
10	7230250	232·8499	6943536	208·1132	6489801	177·1417	6071606	155·7652	5314283	120·7483
11	7199199	248·0858	6910172	221·7306	6453165	188·7326	6032626	163·2154	5270272	117·4339
12	7170180	257·7019	6879008	230·3251	6418973	196·0480	5995665	167·0731	5225393	112·3486
13	7142357	262·6488	6849141	234·7464	6386231	199·8114	5959779	168·3791	5178882	106·6505
14	7115163	264·3188	6819964	236·2391	6354270	201·0819	5924384	167·1649	5130323	100·8644
15	7088244	262·4070	6791095	234·5304	6322670	199·6275	5888943	163·6642	5079459	95·2793
16	7061232	256·7542	6762159	229·4781	6290998	195·3271	5852961	158·2813	5026148	89·9797
17	7033730	247·3743	6732672	221·0947	6258790	188·1913	5815983	151·5399	4970289	85·0231
18	7005296	234·7288	6702220	209·7925	6225533	178·5711	5777604	144·0251	4911831	80·4441
19	6975452	220·1672	6670273	196·7779	6190670	167·4934	5737489	136·1813	4850772	76·2602
20	6943769	205·0755	6636376	183·2895	6153709	156·0125	5695358	128·3158	4787164	72·4748
21	6909910	190·3924	6600169	170·1662	6114265	144·8420	5650972	120·6155	4721111	69·0815
22	6873617	176·6689	6561382	157·9006	6072052	134·4018	5604121	113·1684	4652770	66·0666
23	6834710	164·2273	6519828	146·7807	6026874	124·9368	5554601	106·0587	4582345	63·4116
24	6793093	153·2180	6475409	136·9410	5978634	116·5617	5502228	99·4189	4510081	61·0942
25	6748757	143·6448	6428123	128·3848	5927343	109·2786	5446884	93·4103	4436260	59·0905
26	6701774	135·4947	6378054	121·1005	5873102	103·0783	5388573	88·1506	4361184	57·3776
27	6652313	128·6693	6325387	115·0002	5816125	97·8858	5327443	83·6687	4285175	55·9286
28	6600612	123·0881	6270383	110·0119	5756707	93·6399	5263770	79·9296	4208557	54·7157
29	6546987	118·6168	6213386	106·0157	5695230	90·2384	5197915	76·9060	4131640	53·7103
30	6491792	115·0794	6154778	102·8540	5632117	87·5472	5130327	74·5283	4054715	52·8822
31	6435381	112·2612	6094938	100·3361	5567785	85·4040	5061490	72·6925	3978041	52·2095
32	6378057	109·9810	6034193	98·2972	5502591	83·6686	4991861	71·2630	3901833	51·5291
33	6320064	108·0034	5972806	96.5315	5436825	82·1656	4921813	70·1202	3826258	51·1337
34	6261548	106·1892	5910931	94·9082	5370656	80·7839	4851622	69·1553	3751430	50·6742
35	6202582	104·4610	5848651	93·3637	5304174	79·4692	4781466	68·2669	3677400	50·2081
36	6143205	102·7540	5786007	91·8380	5237429	78·1706	4711425	67·4056	3604156	49·7156
37	6083419	101·0175	5723005	90·2860	5170429	76·8496	4641529	66·5338	3531661	49·1780
38	6023198	99·2042	5659617	88·6653	5103149	75·4701	4571767	65·6161	3459847	48·5807
39	5962483	97·2828	5595786	86·9480	5035531	74·0084	4502092	64·6189	3388629	47·9098
40	5901193	95·2250	5531428	85·1089	4967491	72·4429	4432421	63·5199	3317899	47·1562
41	5839222	93·0063	5466436	83·1258	4898920	70·7550	4362641	62·2991	3247540	46·3116
42	5776439	90·6172	5400675	80·9905	4829682	68·9375	4292614	60·9389	3177416	45·3723
43	5712693	88·0316	5333992	78·6975	4759623	66·9857	4222172	59·4331	3107386	44·3358
44	5647814	85·3068	5266214	76·2443	4688569	64·8976	4151132	57·7782	3037299	43·2039
45	5581608	82·3939	5197145	73·6408	4616323	62·6816	4079285	55·9732	2966997	41·9797
46	5513865	79·3263	5126571	70·8992	4542676	60·3479	4005406	54·0278	2896320	40·6698
47	5444357	76·1195	5054263	68·0330	4467401	57·9083	3932252	51·9537	2825105	39·2841
48	5372833	72·7995	4979972	65·0657	4390255	55·3826	3856564	49·7653	2753186	37·8285
49	5299030	69·4014	4903434	62·0286	4310984	52·7975	3779069	47·4843	2680406	36·3225
50	5222676	65·9585	4824383	58·9514	4229333	50·1783	3699483	45·1384	2606611	34·7794
51	5143495	62·5092	4742546	55·8686	4145046	47·5542	3617525	42·7538	2531664	33·2158
52	5061211	59·0878	4657659	52·8106	4057882	44·9513	3532912	40·3606	2455445	31·6489
53	4975556	55·7307	4569463	49·8102	3967609	42·3974	3445378	37·9851	2377862	30·0962
54	4886277	52·4683	4477726	46·8944	3874028	39·9155	3354675	35·6551	2298853	28·5743
55	4793149	49·3314	4382240	44·0907	3776972	37·5291	3260588	33·3936	2218401	27·0972
56	4695987	46·3140	4282849	41·4153	3676331	35·2510	3162947	31·2233	2136533	25·6747
57	4594645	43·3012	4179437	38·8799	3572043	33·0918	3061646	29·1572	2053317	24·3126
58	4489024	40·8249	4071941	36·4879	3464107	31·0577	2956641	27·2049	1968862	23·0140
59	4379066	38·3055	3960344	34·2362	3352569	29·1411	2847960	25·3689	1883312	21·7792
60	4264746	35·9390	3844666	32·1211	3237523	27·3408	2735698	23·6498	1796839	20·6070
61	4146080	33·7205	3724973	30·1382	3119109	25·6530	2620023	22·0460	1709643	19·4937
62	4023126	31·6446	3601377	28·2829	2997521	24·0738	2501180	20·5543	1621941	18·4356
63	3895991	29·7057	3474043	26·5499	2873007	22·5987	2379493	19·1702	1533962	17·4287
64	3764838	27·8965	3343193	24·9329	2745876	21·2224	2255369	17·8886	1445949	16·4691
65	3629880	26·2099	3209106	23·4255	2616490	19·9393	2129290	16·7032	1358151	15·5527
66	3491388	24·6392	3072114	22·0217	2485268	18·7444	2001812	15·6080	1270825	14·6766
67	3349687	23·1766	2932610	20·7145	2352680	17·6317	1873556	14·5964	1184237	13·8386
68	3205158	21·8149	2791037	19·4974	2219246	16·5958	1745199	13·6621	1098662	13·0370
69	3058233	20·5474	2647888	18·3645	2085523	15·6315	1617458	12·7988	1014389	12·2708
70	2909395	19·3669	2503703	17·3094	1952105	14·7334	1491082	11·9997	931722	11·5390
71	2759170	18·2660	2359059	16·3255	1819610	13·8960	1366822	11·2584	850977	10·8414
72	2608115	17·2382	2214558	15·4069	1688665	13·1140	1245417	10·5683	772483	10·1772
73	2456817	16·2767	2070820	14·5475	1559897	12·3826	1127573	9·9241	696580	9·5461
74	2305876	15·3755	1928472	13·7421	1433922	11·6970	1013953	9·3207	623610	8·9475
75	2155905	14·5287	1788139	12·9853	1311333	11·0528	905168	8·7546	553913	8·3810
76	2007516	13·7311	1650434	12·2724	1192691	10·4460	801774	8·2228	487821	7·8461
77	1861314	12·9785	1515950	11·5997	1078514	9·8735	704268	7·7235	425647	7·3425
78	1717899	12·2678	1385262	10·9646	969280	9·3328	613084	7·2552	367677	6·8696
79	1577866	11·5962	1258922	10·3643	865423	8·8219	528581	6·8171	314155	6·4271
80	1441799	10·9644	1137455	9·7994	767324	8·3398	451043	6·4093	265275	6·0149
81	1310301	10·3751	1021381	9·2719	675316	7·8868	380670	6·0334	221173	5·6361
82	1184007	9·8327	911223	8·7855	589689	7·4647	317576	5·6920	181931	5·2977
83	1063592	9·3427	807503	8·3443	510693	7·0774	261783	5·3898	147589	5·0110
84	949750	8·9115	710731	7·9537	438534	6·7300	213213	5·1332	118136	4·7922
85	843175	8·5463	621372	7·6192	373373	6·4302	171677	4·9313	93484	4·6482
86	744515	8·2511	539818	7·3474	315308	6·1876	136863	4·7970	73373	4·5815
87	654283	8·0277	466347	7·1460	264349	6·0149	108332	4·7489	57358	4·5843
88	572780	7·8770	401087	7·0246	220400	5·9291	85520	4·7827	44846	4·6497
89	500065	7·7989	343990	6·9959	183228	5·9544	67639	4·8920	35201	4·7657
90	435945	7·7935	294820	7·0484	152456	6·0705	53812	5·0564	27815	4·9132
91	380008	7·8473	252992	7·1631	127341	6·2384	43170	5·2194	22153	5·0636
92	331582	7·9349	217673	7·3110	106929	6·3939	34899	5·3535	17778	5·1929
93	289794	8·0305	187900	7·4723	90205	6·4897	28380	5·4470	14355	5·2830
94	253708	8·1207	162754	7·6365	76306	6·5000	23170	5·4958	11638	5·3241
95	222466	8·1208	141441	7·6365	64566	6·5000	18954	5·4958	9452	5·3122
96	195071	8·0580	122919	7·5792	54633	6·4551	15505	5·4613	7673	5·2794
97	170863	7·9340	106702	7·4659	46169	6·3662	12666	5·3928	6219	5·2145
98	149327	7·7515	92410	7·2992	38917	6·2352	10317	5·2916	5027	5·1187
99	130063	7·5147	79749	7·0826	32676	6·0647	8367	5·1597	4045	4·9936
100	112755	7·2288	68490	6·8210	27288	5·8580	6746	4·9994	3235	4·8415
101	97157	6·9538	58449	6·5689	22630	5·6585	5396	4·8441	2567	4·6941
102	83185	6·7413	49551	6·3740	18630	5·5037	4282	4·7234	2020	4·5794
103	70845	6·5862	41777	6·2317	15245	5·3904	3376	4·6348	1579	4·4952
104	60089	6·4849	35073	6·1385	12417	5·3162	2647	4·5767	1228	4·4399
105	50823	6·4347	29359	6·0925	10081	5·2795	2069	4·5479	951	4·4125
106	42925	6·4347	24540	6·0925	8172	5·2795	1614	4·5479	735	4·4125
107	36254	6·4347	20512	6·0925	6624	5·2795	1259	4·5479	569	4·4125
108	30620	6·3850	17146	6·0468	5369	5·2430	982	4·5193	440	4·3853
109	25824	6·2867	14310	5·9564	4345	5·1708	765	4·4626	340	4·3314
110	21716	6·1421	11908	5·8234	3505	5·0644	594	4·3789	261	4·2518
111	18181	5·9545	9863	5·6506	2813	4·9259	458	4·2697	200	4·1479
112	15127	5·7279	8117	5·4418	2242	4·7580	351	4·1371	152	4·0216
113	12486	5·5100	6626	5·2408	1771	4·5955	266	4·0086	114	3·8991
114	10220	5·3417	5361	5·0853	1385	4·4702	200	3·9087	85	3·8038
115	8307	5·2188	4307	4·9717	1075	4·3782	149	3·8353	62	3·7339
116	6715	5·1385	3441	4·8974	830	4·3179	110	3·7872	46	3·6880
117	5408	5·0988	2738	4·8607	638	4·2881	81	3·7634	33	3·6652
118	4348	5·0988	2175	4·8607	489	4·2881	59	3·7634	24	3·6652
119	3495	5·0988	1727	4·8607	375	4·2881	44	3·7634	18	3·6652
120	2809	5·0594	1372	4·8242	287	4·2585	32	3·7397	13	3·6426
121	2254	4·9815	1088	4·7521	220	4·1992	23	3·6928	9	3·5979
122	1802	4·8669	859	4·6460	168	4·1134	17	3·6236	7	3·5317
123	1431	4·7182	674	4·5081	127	4·0009	12	3·5332	5	3·4454
124	1128	4·5387	524	4·3416	95	3·8646	9	3·4235	3	3·3405
125	880	4·3660	404	4·1812	71	3·7329	6	3·3171	2	3·2388
126	678	4·2326	307	4·0571	52	3·6308	4	3·2345	2	3·1596
127	518	4·1353	231	3·9665	37	3·5561	3	3·1738	1	3·1015
128	393	4·0716	173	3·9072	27	3·5071	2	3·1340	1	3·0634
129	296	4·0402	129	3·8779	19	3·4829	1	3·1143	1	3·0445
130	223	4·0402	96	3·8779	14	3·4829	1	3·1143	·	3·0445
131	168	4·0402	71	3·8779	10	3·4829	1	3·1143	·	3·0445
132	126	4·0089	53	3·8488	7	3·4588	·	3·0947	·	3·0257
133	95	3·9472	39	3·7913	5	3·4112	·	3·0559	·	2·9385
134	71	3·8564	29	3·7066	3	3·3410	·	2·9985	·	2·9336
135	52	3·7386	21	3·5966	2	3·2496	·	2·9238	·	2·8619
136	38	3·5964	15	3·4638	2	3·1389	·	2·8330	·	2·7747
137	28	3·4596	11	3·3358	1	3·0320	·	2·7450	·	2·6902
138	20	3·3539	8	3·2368	1	2·9491	·	2·6766	·	2·6245
139	14	3·2767	5	3·1645	1	2·8884	·	2·6264	·	2·5763
140	10	3·2263	4	3·1172	·	2·8486	·	2·5934	·	2·5446
141	7	3·2013	2	3·0938	·	2·8289	·	2·5771	·	2·5289
142	5	3·2013	2	3·0938	·	2·8289	·	2·5771	·	2·5289
143	3	3·2013	1	3·0938	·	2·8289	·	2·5771	·	2·5289
144	2	3·1766	1	3·0706	·	2·8094	·	2·5609	·	2·5133
145	1	3·1277	1	3·0247	·	2·7707	·	2·5288	·	2·4824
146	1	3·0558	·	2·9572	·	2·7137	·	2·4813	·	2·4368
147	1	2·9624	·	2·8694	·	2·6394	·	2·4195	·	2·3772
	45·6000000		42·4764181		37·9780763		33·9582822		27·0000000	

FEMALES.

Completed Years of Age.	First Class, or Perfect Lives. Decrement.	First Class, or Perfect Lives. Intensities.	Second Class, or Life-Annuitants. Decrement.	Second Class, or Life-Annuitants. Intensities.	Third Class, or Assurable Lives. Decrement.	Third Class, or Assurable Lives. Intensities.	Fourth Class, or Indiscriminate Population. Decrement.	Fourth Class, or Indiscriminate Population. Intensities.	Fifth Class, or Inferior Lives. Decrement.	Fifth Class, or Inferior Lives. Intensities.
0	1·0000000	8·6673	1·0000000	7·7628	1·0000000	6·6384	1·0000000	5·5680	1·0000000	4·6378
1	8846234	16·2139	8711809	14·5219	8493628	12·4185	8204029	10·9023	7843808	8·4551
2	8500637	28·0472	8111901	25·1205	7809681	21·4820	7451540	19·5184	6916110	14·7593
3	8004685	45·0982	7788981	40·3922	7446135	34·5417	7069769	32·1535	6447531	24·6476
4	7827191	67·7582	7596147	60·6876	7230566	51·8975	6849894	49·0527	6185942	39·1530
5	7711674	95·6234	7470979	85·6450	7091242	73·2401	6710250	69·7468	6027948	58·5519
6	7631028	127·4186	7383747	114·1225	6994420	97·5927	6614041	93·0235	5924997	81·3981
7	7571139	161·1515	7319047	144·3351	6922751	123·4294	6542940	117·1244	5852207	104·2122
8	7524157	194·4624	7268338	174·1699	6866664	148·9426	6487077	140·1096	5796050	122·9369
9	7485465	225·0625	7226607	201·5769	6820361	172·3802	6440777	160·2630	5748904	135·2345
10	7452205	251·1331	7190756	224·9269	6780994	192·3482	6400588	176·4098	5706393	141·3025
11	7422531	271·5841	7158787	243·2439	6745741	208·0121	6364306	188·0683	5666009	143·5790
12	7395201	286·1353	7129357	256·2766	6713311	219·1572	6330465	195·4301	5626540	143·8506
13	7369356	295·2376	7101538	264·4291	6682679	226·1288	6298073	199·2183	5587432	142·3571
14	7344395	299·8967	7074682	268·6020	6653126	229·6974	6266459	200·4973	5548183	139·3992
15	7319905	301·4660	7048343	270·0076	6624161	230·8994	6235204	199·5044	5508382	135·3073
16	7295624	300·1046	7022238	268·7883	6595473	229·8566	6203951	196·5547	5467672	130·4169
17	7271314	296·0572	6996113	265·1632	6566779	226·7566	6172387	192·0105	5425747	124·9671
18	7246753	289·6331	6969729	259·4094	6537819	221·8362	6140241	186·1981	5382330	119·1877
19	7221733	281·1844	6942861	251·8423	6508348	215·3652	6107264	179·4456	5337171	113·2786
20	7196049	271·0852	6915293	242·7971	6478128	207·6300	6073230	172·0663	5290056	107·4127
21	7169504	259·7127	6886811	232·6113	6446928	198·9196	6037935	164·3003	5240806	101·7042
22	7141899	247·4310	6857204	221·6112	6414518	189·5127	6001185	156·3630	5189276	96·2456
23	7113034	234·5792	6826262	210·1005	6380671	179·6693	5962805	148·4420	5135359	91·1098
24	7082712	221·4628	6793771	198·3528	6345157	169·6231	5922636	140·6551	5078995	86·3224
25	7050730	208·3475	6759520	186·6062	6307750	159·5779	5880529	133·1006	5020157	81·9009
26	7016889	195·4581	6723297	175·0618	6268222	149·7059	5836347	125·8574	4958862	77·8563
27	6980989	182·9775	6684892	163·8835	6226352	140·1464	5789975	118·9534	4895169	74·1811
28	6942837	171·0492	6644101	153·2000	6181924	131·0103	5741300	112·4084	4829180	70·8667
29	6902248	159·7866	6600732	143·1126	6134738	122·3840	5690225	106·2354	4761035	67·9040
30	6859051	149·3588	6554610	133·7730	6084611	114·3971	5636663	100·4440	4690921	65·2726
31	6813128	139·8842	6505612	125·2871	6031422	107.1403	5580545	95·0684	4619054	62·9543
32	6764422	131·3824	6453686	117·6724	5975128	100·6286	5521845	90·1602	4545683	60·9337
33	6712936	123·8570	6398842	110·9323	5915750	94·8647	5460600	85·7568	4471082	59·1873
34	6658737	117·3012	6341159	105·0606	5833390	89·8435	5396925	81·8596	4395541	57·6847
35	6601970	111·6541	6280802	100·0028	5788239	85·5182	5330996	78·4432	4319341	56·3997
36	6542842	106·8634	6217996	95·7120	5720555	81·8490	5263036	75·4612	4242757	55·3094
37	6481615	102·8407	6153030	92·1091	5650663	78·7679	5193291	72·8515	4166047	54·3842
38	6418590	99·4697	6086229	89·0898	5578925	76·1859	5122005	70·5609	4089444	53·5973
39	6354061	96·6527	6017913	86·5668	5505697	74·0284	5049415	68·5217	4013144	52·9243
40	6288320	94·2651	5948395	84·4284	5431324	72·1997	4975724	66·6741	3937316	52·3330
41	6221611	92·1973	5877941	82·5764	5356098	70·6159	4901097	64·9445	3862080	51·7932
42	6154130	90·3109	5806759	80·8868	5280250	69·1711	4825631	63·2667	3787513	51·2759
43	6085986	88·4791	5734970	79·2461	5203913	67·7680	4749356	61·5993	3713648	50·7535
44	6017202	86·6104	5662601	77·5724	5127123	66·3367	4672255	59·9054	3640477	50·1724
45	5947727	84·6211	5589603	75·7908	5049834	64·8131	4594261	58·1521	3567918	49·4552
46	5877441	82·4645	5515853	73·8592	4971920	63·1613	4515257	56·3233	3495773	48·5301
47	5806168	80·1004	5441172	71·7418	4893202	61·3506	4435091	54·4062	3423740	47·3583
48	5733682	77·4966	5365328	69·4097	4813444	59·3563	4353572	52·3913	3351446	45·9342
49	5659696	74·6552	5288029	66·8649	4732350	57·1801	4270475	50·2838	3278484	44·2585
50	5583885	71·5844	5208944	64·1144	4649588	54·8280	4185548	48·0908	3204408	42·3692
51	5505880	68·3215	5127699	61·1921	4564784	52·3289	4098514	45·8311	3128778	40·3209
52	5425293	64·9274	5043902	58·1521	4477552	49·7293	4009087	43·5327	3051181	38·1838
53	5341733	61·4793	4957166	55·0639	4387513	47·0884	3916993	41·2300	2971277	36·0270
54	5254847	58·0445	4867142	51·9875	4294337	44·4576	3821990	38·9531	2888804	33·9163
55	5164315	54·6983	4773521	48·9905	4197743	41·8946	3723872	36·7349	2803629	31·8939
56	5069901	51·4834	4676083	46·1110	4097545	39·4322	3622501	34·6022	2715724	29·9909
57	4971424	48·4329	4574674	43·3788	3993652	37·0938	3517811	32·5689	2625172	28·2248
58	4868779	45·5558	4469215	40·8019	3885974	34·8921	3409800	30·6453	2532163	26·5964
59	4761904	42·8574	4359681	38·3852	3774603	32·8254	3298533	28·8322	2436956	25·0919
60	4650793	40·3247	4246104	36·1168	3659613	30·8856	3184129	27·1268	2339835	23·6904
61	4535460	37·9456	4128538	33·9859	3541124	29·0634	3066749	25·5246	2241068	22·3744
62	4415934	35·7091	4007060	31·9828	3419282	27·3504	2946600	24·0203	2140905	21·1338
63	4292270	33·6051	3881772	30·0984	3294264	25·7389	2823929	22·6069	2039603	19·9317
64	4164544	31·6245	3752802	28·3244	3166277	24·2219	2699015	21·2769	1937376	18·8182
65	4032856	29·7589	3620309	26·6535	3035557	22·7930	2572163	20·0230	1834424	17·7273
66	3897339	27·9991	3484480	25·0773	2902378	21·4451	2443702	18·8371	1730944	16·6740
67	3758143	26·3346	3345531	23·5865	2767038	20·1702	2313974	17·7084	1627133	15·6559
68	3615436	24·7563	3203690	22·1729	2629854	18·9614	2183303	16·6283	1523202	14·6714
69	3469395	23·2541	3059204	20·8275	2491158	17·8108	2052003	15·5865	1419380	13·7206
70	3320200	21·8219	2912321	19·5447	2351291	16·7139	1920350	14·5780	1315932	12·8053
71	3168050	20·4542	2763313	18·3198	2210611	15·6663	1788620	13·5992	1213167	11·9552
72	3013165	19·1483	2612475	17·1502	2069506	14·6661	1657097	12·6506	1111457	11·0899
73	2855806	17·9035	2460146	16·0353	1928398	13·7127	1526107	11·7351	1011235	10·2940
74	2696295	16·7203	2306725	14·9756	1787769	12·8064	1396060	10·8575	912999	9·5415
75	2535037	15·6002	2152692	13·9723	1648170	11·9485	1267481	10·0216	817312	8·8341
76	2372536	14·5436	1998624	13·0259	1510231	11·1392	1141006	9·2317	724794	8·1723
77	2209403	13·5503	1845189	12·1363	1374653	10·3785	1017409	8·4908	636105	7·5570
78	2046351	12·6207	1693151	11·3037	1242201	9·6665	897585	7·8005	551931	6·9880
79	1884209	11·7542	1543364	10·5277	1113695	9·0028	782517	7·1625	472948	6·4670
80	1723909	10·9504	1396763	9·8075	989990	8·3869	673265	6·5774	399816	5·9946
81	1566480	10·2117	1254345	9·1448	871950	7·8203	570905	6·0486	333119	5·5747
82	1413080	9·5422	1117180	8·5430	760452	7·3056	476519	5·5847	273364	5·2096
83	1264993	8·9473	986409	8·0060	656360	6·8464	391194	5·1975	220891	4·9041
84	1123611	8·4331	863200	7·5386	560491	6·4467	315929	4·9013	175849	4·6618
85	990373	8·0037	748693	7·1463	473549	6·1112	251470	4·7016	138127	4·4894
86	866634	7·6624	643927	6·8354	396061	5·8453	197984	4·5997	107360	4·3907
87	755532	7·4099	549722	6·6138	328304	5·6558	154941	4·5955	82909	4·3682
88	651839	7·2458	466604	6·4923	270257	5·5520	121225	4·6679	63928	4·4241
89	561878	7·1696	394734	6·4866	221579	5·5471	95255	4·7992	49478	4·5457
90	483508	7·1810	333830	6·5761	181634	5·6236	75407	4·9500	38594	4·7054
91	416177	7·2568	283108	6·7233	149335	5·7495	60173	5·0765	30392	4·8556
92	358827	7·3507	240999	6·8685	123361	5·8737	48320	5·1537	24133	4·9604
93	310011	7·4148	205912	6·9687	102359	5·9393	38944	5·1562	19268	4·9982
94	268202	7·4339	176364	7·0002	85183	5·9862	31391	5·1562	15413	4·9992
95	232075	7·4240	151169	7·0002	70953	5·9862	25303	5·1562	12330	4·9992
96	200815	7·3623	129574	6·9436	59100	5·9418	20396	5·1211	9863	4·9658
97	173539	7·2403	110914	6·8319	49154	5·8538	16413	5·0516	7877	4·8997
98	149570	7·0611	94679	6·6677	40757	5·7243	13164	4·9490	6269	4·8021
99	128388	6·8291	80480	6·4550	33637	5·5561	10504	4·8156	4964	4·6750
100	109588	6·5497	68012	6·1985	27597	5·3528	8323	4·6538	3902	4·5209
101	92856	6·2818	57040	5·9523	22441	5·1569	6534	4·4975	3039	4·3718
102	78074	6·0754	47457	5·7623	18090	5·0054	5082	4·3762	2344	4·2561
103	65223	5·9250	39221	5·6238	14476	4·8947	3920	4·2874	1793	4·1714
104	54215	5·8269	32247	5·5334	11518	4·8222	3006	4·2292	1363	4·1158
105	44911	5·7784	26419	5·4887	9130	4·7864	2295	4·2004	1032	4·0883
106	37139	5·7784	21606	5·4887	7222	4·7864	1749	4·2004	780	4·0883
107	30712	5·7784	17669	5·4887	5713	4·7864	1332	4·2004	581	4·0883
108	25397	5·7304	14450	5·4444	4520	4·7509	1015	4·1718	445	4·0610
109	20965	5·6354	11796	5·3568	3568	4·6805	772	4·1151	335	4·0069
110	17245	5·4960	9594	5·2281	2806	4·5770	584	4·0316	252	3·9271
111	14107	5·3154	7759	5·0612	2193	4·4425	439	3·9229	188	3·8231
112	11453	5·0979	6226	4·8601	1699	4·2799	327	3·7911	139	3·6971
113	9206	4·8894	4945	4·6571	1302	4·1233	241	3·6638	101	3·5752
114	7323	4·7287	3885	4·5181	986	4·0022	175	3·5650	73	3·4806
115	5775	4·6117	3025	4·4095	740	3·9136	126	3·4926	52	3·4113
116	4523	4·5353	2339	4·3386	551	3·8557	90	3·4452	37	3·3658
117	3525	4·4976	1800	4·3036	408	3·8271	64	3·4217	26	3·3433
118	2741	4·4976	1382	4·3036	301	3·8271	45	3·4217	18	3·3433
119	2132	4·4976	1061	4·3036	223	3·8271	32	3·4217	13	3·3433
120	1658	4·4602	814	4·2688	164	3·7986	23	3·3984	9	3·3210
121	1286	4·3863	624	4·2002	121	3·7424	16	3·3523	6	3·2767
122	993	4·2777	475	4·0992	89	3·6596	11	3·2843	4	3·2115
123	761	4·1372	359	3·9684	65	3·5521	8	3·1957	3	3·1263
124	577	3·9679	269	3·8108	46	3·4221	5	3·0884	2	3·0234
125	432	3·8056	198	3·6594	33	3·2969	4	2·9846	1	2·9237
126	318	3·6806	144	3·5426	23	3·2000	2	2·9041	1	2·8463
127	232	3·5895	103	3·4574	16	3·1292	2	2·8452	1	2·7897
128	167	3·5300	73	3·4018	11	3·0829	1	2·8066	·	2·7525
129	120	3·5007	52	3·3744	7	3·0600	1	2·7874	·	2·7341
130	86	3·5007	37	3·3744	5	3·0600	·	2·7874	·	2·7341
131	61	3·5007	26	3·3744	3	3·0600	·	2·7874	·	2·7341
132	44	3·4715	18	3·3471	2	3·0373	·	2·7685	·	2·7158
133	31	3·4140	13	3·2933	1	2·9923	·	2·7309	·	2·6797
134	22	3·3295	9	3.2141	1	2·9261	·	2·6755	·	2·6263
135	15	3·2201	6	3·1116	1	2·8401	·	2·6033	·	2·5568
136	11	3·0884	4	2·9879	·	2·7362	·	2·5159	·	2·4725
137	7	2·9621	3	2·8692	·	2·6361	·	2·4313	·	2·3910
138	5	2·8647	2	2·7777	·	2·5586	·	2·3658	·	2·3277
139	3	2·7938	1	2·7109	·	2·5020	·	2·3178	·	2·2813
140	2	2·7476	1	2·6673	·	2·4650	·	2·2867	·	2·2509
141	1	2·7247	·	2·6458	·	2·4467	·	2·2707	·	2·2359
142	1	2·7247	·	2·6458	·	2·4467	·	2·2707	·	2·2359
143	·	2·7247	·	2·6458	·	2·4467	·	2·2707	·	2·2359
144	·	2·7020	·	2·6244	·	2·4285	·	2·2553	·	2·2210
145	·	2·6573	·	2·5822	·	2·3926	·	2·2246	·	2·1914
146	·	2·5915	·	2·5201	·	2·3396	·	2·1795	·	2·1477
147	·	2·5064	·	2·4397	·	2·2709	·	2·1207	·	2·0909
	48·4000000		45·4129710		41·4259184		37·4582830		31·0000000	

CHAPTER XXVII.

Of some prominent features exhibited by the Law of Mortality.

247. Bearing in mind what has been stated in our foregoing pages, concerning the method of constructing a Law of Mortality, and of deducing from it many useful results; it may not be uninteresting for the reader to find here a synopsis of the prominent features which that law exhibits, including a few results susceptible of further extension by tabulating them referably to each year of age.

248. Confining this synopsis to the results, for each sex, of the general law applicable to an indiscriminate population, exemplified by that of France (see the paragraph 234th, 237th and 238th); the following are relative to *one million* of annual births, and to an equal quantity of annual deaths, supposed to occur under the hypothesis of such population being stationary.

RELATIVE POPULATION *and its distribution.*
(*See chapter XXIV.*)

	MALES.	FEMALES.
Permanent quantity of population, when stationary; to result from one million of births, annually compensating for an equal quantity of deaths; observing that a summation of all the terms of the decrement shall exceed that quantity by half a million. (See paragraph 48th).	33 458 282	36 958 282

	MALES.	FEMALES.
Permanent distribution of that quantity of stationary population; observing that the proportions of youthful shall exceed those here announced, when the population progressively increases, and the contrary when the population progressively decreases.		
Living at and above 5 completed years.	29 802 080	33 165 248
At and above 10 years.	26 700 472	29 901 223
At and above 15 »	23 711 199	26 743 503
At and above 20 »	20 813 581	23 665 696
At and above 30 »	14 378 646	17 793 908
At and above 40 »	10 597 002	12 471 423
At and above 50 »	6 522 193	7 881 660
At and above 60 »	3 276 407	4 171 266
At and above 70 »	1 152 730	1 605 898
At and above 80 »	224 959	328 829
At and above 90 »	25 389	33 854
Centenarians generally.	2 819	3 206

PERIODIC DEATHS.

(*See chapter XV.*)

First minimum of the relative quantity of deaths, referred to one million of annual births; which minimum takes place at 13 completed years, for the male sex, and at 15 for the female. .	3539·499	3125·348
Maximum of their relative quantity; occuring at 67 completed years for the male, and at 70 completed years for the female sex.	12835·779	13172·970

SPECIFIC INTENSITY OF LIFE.

(*See chapter XVI.*)

At the birth; being the quantity of those out of which *one* fails to complete a first year of age.	4·8705	5·5680
Its maximum referable to 13 completed years, for the males, and 14 for the females.	168·3791	200·4973
Its first minimum, occuring at 87 completed years for both sexes; after which the intensity increases to the 94th, and then declines at each subseqent year.	4·7489	4·5955

	Males.	Females.
Its comparison for both sexes at similar ages; or the proportions of superior intensity attending either sex, with reference to those ages, only, at which such superiority — during the intervening periods — alternately rises to a maximum or falls to a minimum, until it is assumed by the other sex :		
Proportions of the Females' superiority, at the birth		1·1432
— at 4 completed years . .		1·0529
— at 26 »		1.4278
— at 43 »		1·0364
— at 69 »		1·2178
— at 81 »		1·0025
Proportions of the Males' superiority.	1·0192	at 82 comp. years.
—	1·0489	at 85 »
—	1·0193	at 89 »
—	1·0827	at 105, 106 and 107.
—	1·0999	at 117, 118 and 119.
—	1·1172	at 129, 130 and 131.
—	1·1349	at 141, 142 and 143.

COLLECTIVE INTENSITY OF LIFE.

(*See chap. XII.*)

At the birth, and then being identical with the Absolute intensity.	33·4583	36·9583
Its maximum, referable to the 5th completed year and all superior ages, for both sexes.	46·6557	49·4248
Its first minimum, referable for both sexes to the 85th and all superior years. . .	4·4560	4·2605
Its measure of years, referable to the probably oldest individual including any possibly older; that probable age being 128 years for a male, and 126 for a female.	2·5920	2·3358
Its measure referable to two joint lives, at the birth.	16·6574	19·5862
Its measure at the birth, with reference to either of those lives aventually surviving the other.	50·2592	54·3304

	Males.	Females.
EQUATION OF LIFE.		
(See chapter XIII.)		
At the birth, the probabilities being then equal, of attaining, or not, the age of	31·883	39·671
Its maximum, referable for both sexes to the 4th completed year of age.	50·965	53·860
Its first minimum, referable for both sexes to the 86th completed year.	2·956	2·856
Its measure of years referable to the probably oldest individual, then having completed 128 years, if a male, and 126 years if a female.	1·827	1·675
Its measure referable to two joint-lives, at their birth	2·188	2·997
Its measure then referable to the eventual survivor of those two lives. . . .	51·978	56·858
YEARS OF AGE.		
At which the Specific intensity of life equalizes with the Absolute intensity referred to the population at large. . .	55	55
At which the Equation of life ceases to exceed the measure of its Collective intensity.	45	48
The utmost probably attainable by one individual only; —		
Amongst one million born in any year.	128	126
Amongst those born during ten years.	134	131
Amongst those born during one hundred years.	139	136
Amongst those born during a thousand years..	143	140
At which the surviving females become more numerous than the males, although the births of the latter sex are understood to exceed those of the former; — First, supposing 21 male births to 20 female.	»	4 to 5
— Secondly, supposing 17 male births to 16 female.	»	17 to 18
At which the surviving males recommence being more numerous than the females;		

	Males.	Females.
—First, supposing equal quantities born of each sex.	109 to 110 years.	
— Secondly, supposing 21 male births to 20 female.	107 to 108 years.	
— Thirdly, supposing 17 male births to 16 female, as experienced in France of late years.	106 to 107 years.	
At which any quantity of individuals born are reduced, by the deaths :—		
To one-half.	31·883	39·671
To one-third.	54·227	58·687
To one-fourth.	62·010	65·562
To one-fifth.	66·014	69·395
To one-sixth.	68·615	71·927
To one-eighth.	71·962	75·138
To one-tenth.	74·128	77·145
To one-twenty-fifth part. . .	80·725	82·897
To one-hundredth part. . . .	87·365	88·817
To one-thousandth part. . . .	98·163	99·231
At which any quantity of couples simultaneously born would be so reducible, by the death of any one of each two joint-lives : —		
To one-half.	2.188	2·997
To one-third.	18·103	27·339
To one-fourth.	31·884	39·672
To one-fifth.	39·432	46·540
To one-tenth.	56·007	60·190
To one-hundredth part. . . .	74·136	77·155
To one-thousandth part. . .	82·026	83·996
To a single surviving couple.	101 years.	102 years.

249. The above with other corresponding statements, all referred to each year of age, to each sex, and to Joint as well as to Single lives of each discriminated class, — together with the valuations, similarly referred, of contingencies variously described in our next chapter, — form numerous sets of Tables that convey information on important points concerning social life.

CHAPTER XXVIII.

Of applying the Law of Mortality, towards reducing contingent or reversionary sums to a present value.

250. Among the useful purposes to which the law of mortality is applicable, a principal one, of daily recurrence, is that of ascertaining the present value of life-annuities and of reversionary property. The only means of such ascertainment, with a desirable correctness, are derived from a combination of the probabilities of life to be deduced from that law, with the rated interest of money; the latter being a necessary element of computation. And when proceeding on this, the importance of exclusively applying an appropriate modification of the general law of mortality, according to the class and sex of the considered lives, must now be fully understood.

251. Several branches of those results are susceptible of being tabulated by anticipation; and taking joint-lives into view, the tabulations may embrace a vast extent. On this matter, much labour has already been bestowed.

252. The celebrated Euler computed the values of single lives, from Kersseboom's tables of mortality, at *five per cent.* interest; as also Mr. de St-Cyran, from the same tables, at various rates of interest. Mr. Deparcieux likewise computed the values of single lives according to his own tables referred to the class of tontine-nominees; as also Mr. de Florencourt, from the same

tables he corrected. Mr. Dupré de St-Maur computed other tables of values, subsequently inserted in Buffon's work. After them, Mr. Milne supplied complete tables of the values of life-annuities, both on single and on joint-lives, computed according to various rates of interest and to the law he constructed from experience on the mortality of the town of Carlisle; which law has been eminently serviceable to science, at a time when the Northampton law was too indiscriminately and often very injudiciously applied. Subsequently, Mr. Davies published further elaborate tables of valued life-annuities and reversions, computed in the same manner, and according to various rates of interest, combined with the law of mortality he concluded from the experience of the "*Equitable*" life-insurance office. The late Mr. Mazeres and the late Dr. Price had previously supplied analogous tables; the former, according to the law deduced from Deparcieux's observations on select classes of lives in France; and the latter, according to his law concluded from the Northampton experience, as also to the law he concluded from Mr. Wargentin's observations on the mortality in Sweden. Other sets of tables, falling under a similar description, have lately been published by Mr. Finlaison; their computation being from a law of mortality the discussion of which has been the matter of our XXth chapter. And lastly, the writer of these pages has considerably advanced his tabulated valuations of life-annuities, of reversions, etc., under the respective combinations of distinct rates of interest with each of the *ten* modifications here set forth of the law of mortality: but the publication of those extensive tables must be postponed, until leisure shall have been found for their completion, if then it may be reconciled with other considerations.

253. Meanwhile it may be proper to state the following principles and methods, upon which such computations are

generally to be proceeded with; as also to point out some means of securing their accuracy, with all possibly economy of time and labour.

254. Retaining for the symbols x and y their preceding significations, — the former, that of any year of age completed by the considered individual,—and the latter, that of any quantity of survivors at such age, out of a given quantity of births, according to the decrement referable to the appropriate law of mortality; let r further signify a fractional quantity, equal to one year's interest in a single instalment, supposing *unity* to represent the principal sum; and let also x signify a term of forthcoming years, to the expiration of which will be referred any sum then receivable or payable, when the question is of reducing such future sum to a present equivalent. Then $\frac{1}{(1+r)^x}$ shall express a present value of the sum certainly forthcoming at the expiry of the term signified by X, that sum represented by *unity* discountable for that term at compound-interest according to its ratio r, at the same time as $-\mathrm{X} \lambda (1+r)$ is the logarithm of that value, expressible only by a fractional quantity; and $u_x = \frac{y_{x+x}}{y_x (1+r)^x}$ shall likewise express, by a still smaller quantity, the present value of a future and contingent sum also represented by *unity* and available at the expiry of the term X, but conditionally on the assigned life actually of the age x being still extant at the further age $x + \mathrm{X}$. That general expression u_x, the logarithm of which is $\lambda y_{x+x} - \lambda y_x - \mathrm{X} \lambda (1+r)$, shall be the basis on which to rest the computation of any value hereafter signified by v_x, being that of the annuity depending on a single life.

255. Having admitted X generally to represent all successive

numbers of years, beyond that of the individual's present age x; if the corresponding values represented by u be accordingly computed, we shall have a series u_x, correctly expressing present values of the contingent *unity* incoming at the expiration of every succeeding year, until any term at which the corresponding value becomes so reduced as no longer to be of consideration; $v = \Sigma\, u_x$, the sum of partial values u_x, shall then express the total value or *Principal*, by a quantity of *years' purchase* of such annuity, or of the income in a single payment at the expiration of each further year of the considered life: understanding, however, that no ultimate claim of income is to be grounded on any period of days elapsing between the last revolved year and the failure of such life.

256. The method of computing the value of an annuity made to depend on the joint continuance of two lives is perfectly analogous with the preceding. Supposing those lives of the same class, sex and age, a series U_x will be formed of successively partial values $U = \frac{\gamma^2_{x+x}}{\gamma^2_x(1+r)}$; whence $V = \Sigma\, U_x$ shall be the value of such an annuity, also expressed by a quantity of years' purchase, with the same understanding as above.

257. Supposing again those lives to be of different ages, though of similar class and sex: if then the ages are respectively signified by x and by x', the preceding formula will be converted into $U = \frac{\gamma_{x+x} \times \gamma_{x'+x}}{\gamma_x \times \gamma_{x'} \times (1+r)^x}$; whence $V = \Sigma\, U_x$ as before. But in case of the lives being of different sexes, or of different classes, it will be necessary to apply the appropriate modifications of the law of mortality; multiplying the quantity $\frac{\gamma_{x+x}}{\gamma_x}$ which the one modification may represent, by its

corresponding quantity $\frac{\jmath_{x'+x}}{\jmath_{x'}}$ according to the other, and dividing the product by $(1+r)^x$; whence the process stated in the 255th paragraph shall equally yield a series U_x, the summation of which $V = \Sigma\, U_x$, exhibiting the present value of the annuity on joint-life; always with the understanding aforesaid.

258. When the question is of tabulating, by anticipation, the values either of single or of joint lives, according to successive years of age, and to any given rate of interest, a great economy of time and of mental labour, as also a security against incidental errors, will result from the following mode of proceeding.

259. Having stated in one column all logarithms of the successive quantities u_x, with reference either to any earliest age signified by x, or to the earliest two ages signified by x and by x' in the case of joint lives, those logarithms being *positive* quantities, in expressing which, all the *negative* indices shall be omitted; every succeeding column, referring to ages more advanced, will be formed by the one immediately preceding, exclusively of its first term, and adding to each of its subsequent terms an equal quantity, being the arithmetic complement of that first term of the series. The motive is obvious. Each quantity, either u or U, being produced by the probability that a single life aged x years,—or else two joint-lives as described, — shall endure another year, multiplied by the discounted value of *unity* for one year; it follows, that when such first year is expired the mere *probability* has become a *certainty*, as also that the discounted sum has recovered an integral value, as regards either the life aged x having then attained the age $x+1$, or as regards the joint-lives both of which have in

the same manner advanced another year; whence the logarithm of the probability, and that of the discounted value, shall have respectively risen to o, from being negative quantities referred to the year of age immediately preceding; and all other logarithms in the column $\lambda\, u_x$ shall increase by a similar quantity, to form the column $\lambda\, u_{x+1}$. When thus proceeding, errors will be guarded against, by observing, as a natural consequence, that the successive, quantities $\lambda\, u_{x+1}$, $\lambda\, u_{x+2}$, $\lambda\, u_{x+3}$, $\lambda\, u_{x+4}$ ..... $\lambda\, u_{x+n}$, must be respectively equal to the corresponding quantities $\lambda\, u_x - \lambda\, u_x$, $\lambda\, u_x - \lambda\, u_x$, $\lambda\, u_x - \lambda\, u_x$, $\lambda\, u_x - \lambda\, u_x$ ..... $\lambda\, u_{x+n-1} - \lambda\, u_x$, in the same order of succession; whence no incidental error could escape detection. And further the chances of error will be diminished, as also a considerable saving of time will be obtained, by avoiding to appropriate in the logarithms more figures than strictly necessary. *Five* are sufficient for the purpose of all desirable accuracy, which then admits *four* decimal figures to express the most elevated among the fractional quantities u_x; and it would be a mere delusion to imagine that a nearer approach to absolute correctness, in a matter resting entirely on probabilities and approximations, could be obtainable through the introduction of any greater number of decimal figures in the expressed valuations of annuities by quantities of years' purchase. The writer derived great economy of time from using Lalande's table of logarithms thus limited, and carefully transcribed within the smallest possible space. Errors may however arise on converting the $\lambda\, u_x$ into their corresponding quantities u_x, by the tables of logarithms, although with ordinary attention they should but seldom occur when having only *four* figures to set down; as also further errors on summing up $v = \Sigma\, u_x$. But a

ready method of detecting all such errors will be to note the successive differences $v_x \pm v_{x+1}$, $v_{x+1} \pm v_{x+2}$, $v_{x+2} \pm v_{x+3}$, etc., throughout the whole series of computed values; and to remark where the regular progression of those differences may be materially disturbed, thus pointing out any specific quantity v_x, or series u_x, involving probable error. All that is here mentioned, referably to u and to v, equally applies to U and to V regarding annuities on joint-life.

260. The present value, or *Principal*, of an annuity contingent on the longest of any two lives, — which implies its being payable until both lives shall have dropt, — is immediately determinable from a previous ascertainment of the respective values of three equal annuities, two of which contingent on each of those lives singly considered, and the third on their joint-continuance. Supposing the values of the single lives respectively to be v and v', as also V to be the value of their joint continuance, the value of the longest life shall obviously be, in all cases, $v + v' - V$, or the sum of the first two values abating the third, or value of the eventually shortest life; which necessarily follows from the latter's ultimately proving identical with the one or with the other of the two, whose contingencies were separately valued.

261. When stating the above rules, the life-annuities of different descriptions have been exclusively considered as accruing at the expiration of each revolved year, and as terminating with the last of those years preceding the failure of the life on which such income depended; but as other conditions may attach to the grant of any life-annuity, it is necessary further to state the modifications of value consequent on each particular condition,

differing from those first supposed and always assumed when the values are tabulated by anticipation.

262. In case of an annuity stipulated to accrue at the commencement — instead of the expiration — of every succeeding year, either of the valuations, computed as before, are to be increased by *unity* or a whole year's purchase; the only difference then consisting in the first year's anticipated income, which indeed is nothing else than an abatement on the principal sum or purchase price.

263. There are two other cases, both independent of each other, as also of the preceding; but the solution of questions involved by those cases requires previously to ascertain another quantity, which we may generally signify by t. That quantity, — either t_v, t_V, or $t_{v+v'-V}$, — expresses a *term certain* of years, during which, and by an equitable composition, the annuity of whatever description might be continued, instead of being made to depend on the uncertain duration of life. By consulting the elementary works that state invariable relations between these *five* quantities, — the *annuity*, — its *cumulated amount* at the expiry of any given term, — its value or the *principal*, — the *ratio* of interest, — and the *term* of years of the annuitys' continuance; and in which works it is further demonstrated, that any three of those quantities being stated, the other two become ascertainable; it will be found that the relative term t, according to the respectively predetermined values, is either $t_v = \frac{-\lambda\,(1 - rv)}{\lambda\,(1 + r)}$, $t_V = \frac{-\lambda\,(1 - rV)}{\lambda\,(1 + r)}$, or $t_{v+v'-V} = \frac{-\lambda\,(1 - r\,[v + v' - V])}{\lambda\,(1 + r)}$.

264. Reverting to the two cases mentioned in the first

clause of the preceding paragraph : if the annuity continued payable, in due proportion, for any intervening period between the last revolved year and the demise of the understood life or lives, the value, predetermined without that condition, would in this case admit an increase equal to a half-year's income discounted at compound-interest, with reference to the term t computed according to the above direction; and if the annuity accrued by *half-yearly* or by *quarterly* instalments, in corresponding proportions, instead of accruing by single and annual instalments, the increased value would then, and according to either of those proportions, be $\frac{(1+\frac{r}{2})^{2t}-1}{(1+r)^t-1}$, or $\frac{(1+\frac{r}{4})^{4t}-1}{(1+r)^t-1}$.

265. As those cases of exception, to the general rule for valuing life-annuities, are perfectly independant of each other, they admit such combinations as to require the computations of increase, above the simple and tabulated values, to be governed by the respective analogics; observing always, that the fractional quantity signified by r is understood invariable, when performing different functions in the original and in the supplementary computations. Hence, and supposing anticipated accretions of only the half-yearly or the quarterly instalments, the increase of the annuity's value would be no more than a fourth or an eighth part of a years' income discounted for the term t, if notwithstanding such anticipation the annuity continued proportionally payable after the last revolved half-year or quarter, until the demise; whilst, on the other hand, cumulated proportions of the increased value should be consequent on a combination of the two cases stated in the preceding paragraph, or on a combination of either with the condition of anticipated instalments; and the latter condition alone, if the instalments

were half-yearly or quarterly, would merely add a corresponding proportion to any predetermined value of the annuity.

266. As regards the present value of any reversionary property, available on the failure of a single life, — on that of either the one or the other of two lives jointly considered, — or else on the failure of both lives, — the ascertainment of such values entirely depends on that of the annuities contingent on those lives as respectively described; excluding the consideration of any one amongst the extraordinary conditions discussed in the 261st and subsequent paragraphs.

267. Now admitting a to signify the reversionary sum, or the value of any other reversionary property; and further admitting b, B, and $b + b' - B$, respectively to signify the corresponding and present values of such reversions, after failure of a single life valued v, — after failure of any two lives the joint-continuance of which valued V, — or after failure of both those lives the longest of which valued $v + v' - V$; there is, with reference to all cases, the following determinations of those present values:

$$b = \frac{a - arv}{1 + \frac{r}{2}}, \quad B = \frac{a - arV}{1 + \frac{r}{2}}, \quad \text{and} \quad b + b' - B = \frac{a - ar(v + v') - arV}{1 + \frac{r}{2}}.$$

268. If the reversion valued B were conditional on the first failing, of the two lives, being one selected preferably to the other; the value of such conditional reversion would be, — proportionally with the amount of unconditional valuation, — as the fractional quantity expressing the probability of the selected life's surviving the other, — to *unity* or the sum of their reciprocal probabilities

of survivorship. Mr. Morgan's rule *, for computing those probabilities, is however without application in the case of two lives differing in sex or in class, and thence requiring a reference to distinct modifications of the law of mortality.

269. Having thus ascertained the equivalent of any reversionary property, it is easy further to determine an annual sum substitutable for that equivalent and depending on the contingencies of life in the presupposed cases, of single, of joint, or of longest life; which annual sum is usually denominated *Premium of Insurance*. Such premium being nothing else than an annuity, into which the principal sum is converted by mutual agreement, and considering that it is usually discharged by anticipation of each year in a single payment; it shall then be, either $\frac{b}{v+1}$, $\frac{B}{V+1}$, or $\frac{b+b'-B}{v+v'-V+1}$, according to the specific case. But it must be understood, that any premium of life-insurance computed on those grounds, — however equitable, — leaves entirely out of consideration the charges of management, requisite profit, and liabilities necessarily incurred by public institutions, when transacting business of that nature.

270. It is immediately consequent on what has just been stated, that the title to property, denominated *Policy of Insurance on Life*, possesses a value increasing with the advance of time since the contract was entered into. At any posterior period, the real value of the reversion, whether that value were b, B, or $b+b'-B$, will be more or less superior

(*) Mr. Morgan has computed the probabilities of survivorship, according to the Sweden mortality-tables; as also Mr. Milne, according to his tables for Carlisle.

to what it was originally; whilst the annuity or premium, charged upon that original value, will represent a smaller capital, at which it should be redeemable. The property in a Policy may therefore at all times be equitably purchased at the then present value of the reversion, according to the ages of the life or lives on which it depends; abating the present value, also, of the life-annuity as then describable. This simple rule applies to all possible cases; there existing no adequate motive for excluding from the benefit of life-insurance, either joint-lives, or a survivor's life. It is of no small importance for the public, at large, to be facilitated in ascertaining the fair value of such titles of property; a due information respecting which may render the unpretending individual less dependant on arbitrary dealing. Some offices of life-insurance are understood to notify, at the time of contracting, the gradually increasing valuations from year to year, at which they are willing to purchase the policies originating with themselves: a very laudable regulation, which all offices of that description ought to adopt. It is but seldom that contingent property of any kind, when thrown on the market, may obtain its full value; and a life-annuity in particular has, from special fitness, its greatest appreciable value when in the nominee's possession.

271. This chapter is confined to stating those applications of the law of mortality which relate to results susceptible of tabulation for occasional use. There are numerous other objects of application, the appropriate rules for most of which are to be found in various publications, chiefly those of Mr. Morgan. The circumscribed purpose of the present work further renders unnecessary that those statements should embrace the joint consideration of any more than two lives, the valuation of contingencies depending on which might equally be called for.

CHAPTER XXIX.

Of Institutions founded on an application of the Law of Mortality; and in particular, of an Institution for Assuring, at the time of Marriage, Endowments to the issue therefrom.

272. The conversion of property exposed to peril or involved in doubt, into other possessing the character of certainty, is at all times attended with advantage, when obtainable by an equitable compromise of the unfavourable chances attaching to the former. The reality of that advantage will not be destroyed, though profit should devolve to the parties neutralizing the risk or causes of uncertainty, unless such profit were exorbitant; and the beneficial results of promoting all provident dispositions, as also of affording the utmost facilities to render profitable the savings of income, are unquestionable. Those objects are in progress of fulfilment, through the instrumentality of numerous public Institutions and private associations, induced by the advance of general knowledge; some of which Institutions, being formed on the principle of a mutual assurance, which under wholesome administration admits the lowest standard of sacrifice by the assured parties, may be entitled to preference.

273. The associations for life-insurance hitherto stand prominent amongst all others. By *Insurance of life* is understood the contract for a sum reversible, when shall fail either any single life, the joint-continuance of any two or more lives, or else a last-surviving life of

several jointly considered; which reversionable sum is represented by an equivalent at the time of contracting, when the latter may be either discharged in a single payment, or be converted into an annuity under the denomination of *premium*, payable during the life or lives thus said to be insured. Such insurance may further take place against the only chance of life's dropping within a stated period, as also other modes of accommodation may be introduced; the particulars of all which are here unnecessary to be recalled. Amongst all provident transactions, this is one of the most important, viewed as a resource for millions of persons respectably situated, but whose periodic incomes shall in all probability terminate with their lives; as it resolves into certainty the pecuniary results to be expected from life's profitable employment, whilst limited to a probable duration according to age, to sex, or to class, and neutralizing the chances of that duration's eventual abridgment or protraction.

274. Excepting only the Savings-banks and the associations for insurance against fire, those institutions are generally founded upon an application of the *Law of Mortality;* and it is a great desideratum, that appropriate modifications of that law should at length be substituted for the Northampton tables, too indiscriminately applied in most cases. Those tables exhibiting human life under a most unfavourable aspect, inasmuch as its Absolute intensity is there represented as scarcely exceeding *twenty-five* years, may indeed answer the purpose of *security*, when applied to the computation of premiums chargeable on life-insurance; but then the mark is so widely overshot, that those associations, encumbered with exorbitant profits thence arising, though not originally contemplated, become obnoxious to restitutions in diversified proportions, depending on arbitrary rules, and the worst feature of all which consists in a mode of dealing in utter darkness; whilst

the sound principle, to be proceeded upon in transactions of that description, should be in the first instance to concede terms as favourable for the public as may consist with perfect safety to the general concern. A positive increase, in whatsoever proportion of the reversible sum insured,—that increase becoming a certainty,—would at all times be better appreciated than the prospect of a *bonus* extending to even the double of that proportion, but involved in uncertainty and made to depend on (perhaps) capricious rules of apportionment. On the other hand, the tables now used for computing the life-annuities to be granted by the Exchequer are objectionable on other grounds stated in our XXth chapter.

275. It is further to be remarked, that property become the subject of an insurance is incapable of bearing taxation, for the benefit of the revenue; it being not less absurd than it is oppressive, to tax either provident economy,—which cannot be too much encouraged,—or direful misfortune, as in the case of property destroyed by conflagration.

276. All provident institutions, in England, labour under a special inconvenience, one single glance at which may here be sufficient for the present. Their accumulating capitals are unavoidably sunk, at every risk, in that overwhelming gulph, the FUNDED DEBT; yielding only a scanty rate of interest, towards the utmost reduction of which all imaginable artifices are constantly practised, and the best talents in the country are enlisted. In this respect two questions arise, which we shall merely state, leaving their solution to the operation of TIME. — *First*, is the National Debt, from its origin, and considering the parties exclusively benefited through its having been incurred fairly chargeable on the labour and industry of the nation, either in perpetuity as regards the *interest* of that debt,

or in any shape as regards the *principal*, under a supposition that its redemption were seriously intended; or rather, is it not exclusively chargeable on the property actually existing, of whatsoever description, an assessment upon which might ultimately be for the greater advantage of all classes, not excepting even the reluctant contributors, as also revive the country from its comparatively paralyzed state? — And *Secondly*, is a very low rate of interest, in the investment of money, truly beneficial to the community at large; or is it beneficial only to speculators, and to those who aim at the greatest concentration of property; to the detriment of others living by their personal exertions, the only source whence the country derives its powers called forth in the hour of need?

277. All reversionary expectations, depending on the chances of life and of survivorship, — however remote, uncertain, or complicated, — are nevertheless convertible into a present value, through applying the Law of Mortality; but if this application be made without judicious discrimination of the appropriate modifications of that law, considering the sex and class to which it is referable, the results of computation to that effect must differ so much from the truth as to defeat every purpose of distributive justice. Such conversions may occasionally prove an invaluable resource for persons peculiarly circumstanced. In our state of ultra-civilization, involving a most unequal distribution of the social advantages amongst a numerous population, Institutions resting on positive science, — directed on principles of strict equity, — and above all, affording reciprocal guarantees, — should if possible extend to accommodating the public in respect to all its demands.

278. It is from those considerations, that the writer of

these pages has employed many years in maturing the Plan of an Institution, on the economic principle of mutual assurance, for providing at the time of marriage, and in behalf of the children to be born thereof, sums payable on their attaining any agreed year of age; varying the contributions according to the wife's age at marriage, and supplying optional modes of their discharge. The average of births in expectation, at each specific age of marriage being contracted; — the proportions, to each other, of all births male and female; — the proportions of individuals, belonging to either sex, who, amongst any quantity of births, attain the respective ages at which the endowments may be rendered available; — an average period, computed from the time of marriage, and to which all births may be referred; — lastly, the ratio of interest, according to which any accumulation of capital may safely be assumed, — are requisite elements from which the principal tables have been computed, towards equitably regulating all transactions of the above description; and it is seen by the foregoing chapters, that those elements are susceptible of determination with sufficient accuracy. The general object of that Concern is to guard large families against the vicissitudes of fortune, and females particularly against a precarious dependance; as also to relieve the solicitude of parents contemplating a numerous offspring, the original contract providing for each child in whatever number. The beneficent provision will then be obtained at less cost than through a transaction of life-insurance, and possess the advantage of not requiring the previous death of a parent. The moral tendency of this proposed Institution, together with the permanent benefits it is intended to confer, cannot fail at length to be appreciated; and from those benefits extending to all classes, the highest will find an

equal inducement to join in the PROSPECTIVE-ENDOWMENT-ASSOCIATION (*).

(*) *It would not be inconsistent with the author's views to devolve that concern on* FOUR, *or more, amongst the leading Associations in the British metropolis, for the Insurance of Lives; in which case, his continued assistance to be liberally afforded, and the terms of such cession to be commensurate with just claims to which he is liable. The present opportunity is therefore taken of giving notice, that proposals to the above-mentioned effect, or for honourable co-operation with him, in the alternative of opening an exclusive concern as described, shall be respectfully met.*

CHAPTER XXX.

Of the Law of Mortality differently represented by various authors.

279. In many parts of this book, it has been remarked on the objectionable results of preceding attempts at ascertaining the Law of Mortality, whence the expedieney of stating those results in a shape favourable to their comparison; which will bring out, in a clear point of view, the discrepancies, contradictions, disproportions, and other irregularities of those results. This statement shall be of two parts: — *First*, a Synopsis of the DECREMENT OF LIFE, according to the different representations it has received, and consequent on which are the corresponding expressions of life's Absolute intensity: — *Secondly*, a Synopsis of Life's SPECIFIC INTENSITY at each year of age; being likewise consequent on those varied representations of the Decrement, and deduced according to the principle established in the 51st paragraph.

280. Such of those Mortality-tables as may be worth commemorating are *twenty-five* in number; of which follows a review in successive order; commencing with the most elevated, and ending with the most reduced measure of life's average duration or Absolute intensity, as rendered apparent by the respective decrements, and deduced according to the general rule set forth in the 62d paragraph.

Years of Abs. intensity.

I. Mr. FINLAISON's tables, computed from his observations on the mortality amongst FEMALES, being tontine-nominees and life-annuitants of the government in England and Ireland, at various periods . . . . . 49·3621

II. The same author's tables referred to the MALE sex, of the above-stated class. . . . . 43·6767

N. B.—See, in chapter XXth, the remarks arising from an investigation of Mr. Finlaison's tables.

III. Mr. BABBAGE's tables, deduced from data supplied by an experience of the "*Equitable*" life-insurance office; not distinguishing the sexes, and admitting as regards the first ten years of life Mr. Milne's results from the observations at Carlisle. . . . . 39·3627

IV. Mr. DAVIES's tables, also deduced from the "*Equitable*" experience above-mentioned; without distinction of sex, and supplying the results there omitted for the first ten years. . . . . 38·7288

N. B. — See the remark in paragraph 19th, respecting the deductions from the assured-lives experience, and applicable to those results N°. III and IV.

V. Mr. MILNE's tables, computed from Dr. Heysham's observations during the *nine* years to 1787 inclusive, on the mortality of both sexes in the town of Carlisle. . . . . 38·7213

N. B. — See the remarks on those tables, in the 31st paragraph.

VI. The same author's tables, computed from observations supplied by Mr. Nicander on the mortality amongst the FEMALE population of Sweden and Finland; which observations embrace a period of 20 years, ending with 1795. . . . . 37·5424

VII. The same author's tables referred to the indiscriminate population of both sexes in Sweden and Finland, and deduced from Mr. Nicander's above-menioned data; further admitting 1021 male births to 979 female. . . . . 36·1154

VIII. Dr. PRICE's tables computed from Mr. Wargentin's observations on the mortality amongst the FEMALE population in Sweden; which observations embrace a period of 20 years, to 1775 inclusive. . . . . 35·7020

Years of Abs. intensity

IX. Mr. Deparcieux's tables, deduced from observations concluded in the year 1742, on select lives of both sexes in France, being Tontine-nominees entered in the years 1689 and 1696, as also of individuals in monastic retirement, those last data referred to various periods between the years 1607 and 1745; further remarking, that the results for the first three years are supplied by Mr. de Florencourt and stated to be from Kersseboom's results. . . . . 34·8955

X. Mr. Milne's tables, computed from the data supplied by Mr. Nicander, respecting the Male population of Sweden and Finland, as related in N°. VI. . . . . 34·7416

XI. Mr. Kersseboom's tables, deduced from experience amongst the state-annuitants of both sexes, in Holland; according to a register of their mortality, embracing a period of 135 years, to 17.. inclusive. . . . . 34·4702

XII. Dr. Price's tables, deduced from M. Wargentin's observations on the mortality of both sexes in Sweden, during 20 years, to 1775 inclusive. . . . . 34·4217

N. B. — That author having proceeded on the erroneous supposition of births in equal quantities for both sexes; the tables here related are a rectification of his own, on the admission of 1021 male births to 979 female, as in N°. VII.

XIII. Mr. Rickman's tables, computed from observations during the 18 years that terminate with 1830, on the mortality amongst Females, in the county of Essex, in England . . . . . 34·1473

XIV. The same author's tables, referred to the indiscriminate population of both sexes in Essex, from the above-related observations. . . . . 33·9697

XV. The same author's tables, referred to the Male sex in particular, and deduced from the said observations on the mortality in the county of Essex. . . . . 33·7721

N. B. — A rectification of the decrement, in each of the last three cases, should increase the absolnte intensity of life by half a year; consequently to Mr. R's having taken departure from a quantity of the living at various fractional parts of a first year of age, instead of proceeding from a supposed quantity of simultaneous births, being greater than the former; respecting which distinction of quantities, see the definitions in chapter V, as also see in the 34th paragraph some further remarks on Mr. R's tables.

Years of Abs. intensity.

XVI. Dr. Price's tables referred to the Male population of Sweden, and deduced from Mr. Wargentin's observations related in No. VIII. . . . . 33·1939

XVII. Mr. Duvillard's tables, computed from his observations on the mortality of both sexes in France, previously to the year 1790, but which observations were confined to the towns; further remarking that the small-pox's influence on the rates of mortality, as respectively affecting each year of age, has been abstracted in those computations. . . . . 32·2557

XVIII. Mr. Sussmilch's tables, deduced from observations on the mortality amongst the population of a part of the Prussian dominions, without distinction of sex, and combining the experience of three periods of ten years each to 1774 inclusive. 30·6922

XIX. Mr. Duvillard's tables of the mortality in the towns of France, without distinction of sex, and deduced from his observations related in No. XVII, without the abstraction there mentioned. 28·7632

XX. Dr. Halley's tables, computed from observations continued during one hundred years from 1633, on the mortality at Breslaw (Silesia), without distinction of sex . . . . . 27·4518

XXI. Mr. Milne's tables, computed from observations supplied by Mr. Mourgue, on the mortality amongst Females in the town of Montpellier (France); and which observations embrace 21 years, ending with 1792. . . . . 27·3639

XXII. The same author's tables, also deduced from the Montpellier observations, but indistinctly referred to both sexes, admitting the births in the proportion of 33 males to 31 females. 25·3055

XXIII. Dr. Price's tables, deduced from a register of mortality in the town of Northampton, during the 46 years that terminate with 1788; without distinction of sex. . . . . 25·1824

XXIV. Mr. Milne's tables, computed from the Montpellier observations related in No. XXI; but exclusively referred to the Male population of that town. . . . . 23·3723

XXV. Mr. Simpson's tables referred to the population of London, without distinction of sex; and computed from the returns of mortality during three periods of ten years each, respectively terminating with the years 1737, 1768, and 1780. . 18·9351

DECREMENT OF LIFE,

OR THE RELATIVE QUANTITIES OF INDIVIDUALS ATTAINING EACH SUCCESSIVE YEAR OF AGE, TO THAT OF ONE HUNDRED;

AS VARIOUSLY REPRESENTED BY TWENTY-FIVE STATEMENTS OF THE LAW OF MORTALITY, MOSTLY BY DIFFERENT AUTHORS, AND ADMITTING THE BIRTHS IN EQUAL QUANTITIES.

COMPLETED YEAR OF AGE	No 1. FINLAISON: Annuitants, Females.	No 2. FINLAISON: Annuitants, Males.	No 3. BABBAGE: Assurables.	No 4. DAVIES: Assurables.	No 5. MILNE: Population of Carlisle.	No 6. NICANDER: Sweden, Females.	No 7. NICANDER: Population of Sweden.	No 8. WARGENTIN: Sweden, Females.	No 9. DEPARCIEUX: Select lives in France.	No 10. NICANDER: Sweden, Males.	No 11. KERSSEBOOM: Annuitants in Holland.	No 12. WARGENTIN: Population of Sweden.	No 13. BICKMAN: Essex, Females.	No 14. BICKMAN: Population of Essex.	No 15. BICKMAN: Essex, Males.	No 16. WARGENTIN: Sweden, Males.	No 17. DUVILLARD: Towns in France,—Small-pox influence abstracted.	No 18. SUSSMILCH: Population of Brandenburgh	No 19. DUVILLARD: The towns in France.	No 20. HALLEY: Population of Breslaw.	No 21. MOURGUE: Montpellier, Females.	No 22. MOURGUE: Population of Montpellier.	No 23. PRICE: Population of Northampton.	No 24. MOURGUE: Montpellier, Males.	No 25. SIMPSON: Population of London.
0	1·0000 000	1·0000 000	1·0000	1·0000	1·0000	1·0000	1·0000	1·0000	1·0000	1·0000	1·0000	1·0000 00	1·0000	1·0000	1·0000	1·0000	1·0000 000	1·0000	1·0000 000	1·0000 00	1·0000	1·0000 00	1·0000	1·0000	1·0000
1	8711 809	8827 334	8461	8461	8461	8099	7985	7910	7450	7876	8036	7802 80	8161	8006	7857	7700	7842 279	7923	7675 247	7942 20	7669	7365 21	7425	7080	6809
2	8590 071	8574 483	7779	7779	7779	7534	7444	7392	7088	7333	7679	7293 88	7684	7518	7359	7200	7094 430	7192	6718 341	6790 58	6700	6363 27	6252	6047	5774
3	8484 627	8548 303	7274	7274	7274	7230	7134	7062	6823	7023	7357	6950 62	7369	7199	7016	6863	6749 479	6795	6246 684	6337 87	6021	57,6 58	5821	5631	5036
4	8391 483	8455 312	6998	6998	6998	6964	6911	6792	6618	6799	7093	6705 72	7164	6994	6830	6625	6558 719	6524	5987 134	6036 07	5699	5232 83	5533	4982	4676
5	8302 732	8060 778	6797	6797	6797	6864	6747	6657	6468	6634	6886	6563 07	7000	6841	6688	6473	6440 122	6294	5831 509	5813 69	5122	4860 58	5364	4615	4433
6	8227 842	7990 804	6676	6676	6676	6720	6599	6537	6345	6483	6764	6440 51	6893	6732	6577	6348	6359 114	6096	5730 250	5638 96	4908	4646 94	5206	4402	4283
7	8163 034	7932 258	6594	6594	6594	6613	6490	6432	6243	6371	6643	6355 51	6796	6634	6479	6243	6298 775	5950	5658 379	5496 00	4787	4518 79	5086	4267	4169
8	8108 655	7880 476	6536	6536	6536	6538	6412	6347	6154	6190	6521	6247 97	6712	6544	6383	6153	6249 746	5846	5602 446	5400 69	4711	4438 73	4991	4153	4068
9	8062 245	7832 877	6493	6493	6493	6481	6353	6277	6073	6230	6557	6175 41	6669	6473	6313	6078	6206 500	5762	5556 864	5321 27	4652	4390 92	4923	4142	4018
10	8022 477	7787 164	6460	6460	6460	6431	6303	6217	6004	6180	6391	6112 86	6575	6411	6253	6013	6165 650	5710	5511 216	5249 79	4620	4358 21	4871	4112	3964
11	7987 424	7748 322	6435	6435	6431	6385	6257	6165	5946	6134	6329	6059 33	6510	6349	6194	5958	6125 093	5668	5468 883	5186 25	4592	4334 54	4827	4093	3912
12	7955 889	7700 854	6409	6409	6363	6360	6215	6119	5897	6091	6271	6013 84	6448	6288	6135	5913	6083 335	5626	5426 301	5130 66	4566	4312 90	4784	4075	3861
13	7918 852	7659 708	6381	6383	6368	6303	6174	6079	5854	6030	6214	5971 28	6388	6233	6087	5868	6030 193	5565	5382 550	5083 01	4542	4292 09	4741	4058	3810
14	7881 054	7619 428	6351	6356	6355	6266	6136	6044	5815	6011	6164	5933 73	6317	6172	6032	5828	5994 618	5543	5337 105	5035 35	4518	4271 67	4698	4040	3763
15	7838 952	7577 865	6320	6326	6300	6229	6098	6009	5778	5973	6114	5896 18	6251	6114	5982	5788	5946 573	5501	5289 693	4987 70	4493	4250 44	4655	4022	3718
16	7783 179	7532 780	6288	6294	6261	6192	6061	5974	5740	5934	6064	5859 13	6176	6048	5925	5749	5895 964	5459	5240 203	4940 05	4468	4227 54	4612	4002	3673
17	7726 688	7481 098	6255	6260	6219	6155	6023	5934	5699	5836	6014	5819 64	6092	5977	5866	5710	5842 786	5418	5188 627	4892 39	4441	4202 16	4567	3978	3626
18	7664 683	7421 542	6221	6224	6176	6117	5985	5894	5655	5857	5964	5780 15	6009	5903	5800	5671	5787 093	5376	5135 022	4844 74	4410	4171 40	4517	3947	3579
19	7600 537	7352 394	6186	6185	6133	6079	5945	5852	5608	5816	5900	5737 13	5912	5817	5725	5627	5728 980	5334	5079 490	4797 09	4376	4135 66	4463	3910	3531
20	7534 839	7274 887	6150	6144	6090	6039	5903	5809	5558	5773	5836	5693 63	5820	5730	5644	5583	5668 569	5192	5022 159	4749 43	4340	4097 48	4405	3870	3483
21	7470 889	7190 120	6113	6103	6047	5998	5839	5766	5506	5716	5771	5647 06	5727	5643	5563	5533	5605 999	5240	4963 170	4701 78	4301	4057 25	4343	3828	3435
22	7407 223	7093 356	6075	6062	6005	5956	5814	5723	5453	5677	5714	5600 48	5634	5557	5481	5483	5551 421	5188	4902 676	4654 13	4261	4015 80	4229	3785	3383
23	7343 672	6994 223	6035	6019	5963	5912	5766	5680	5399	5626	5657	5553 91	5529	5462	5394	5433	5474 996	5136	4840 825	4598 53	4219	3973 55	4215	3763	3330
24	7280 340	6895 242	5993	5976	5921	5867	5717	5636	5344	5573	5593	5504 29	5426	5371	5315	5378	5406 833	5084	4777 770	4550 88	4175	3930 50	4150	3700	3275
25	7217 145	6797 645	5949	5931	5879	5821	5667	5591	5258	5519	5514	5454 18	5324	5280	5235	5323	5337 250	5031	4713 660	4503 23	4131	3887 06	4086	3658	3219
26	7154 481	6702 606	5903	5885	5836	5772	5615	5546	5231	5464	5429	5404 08	5226	5195	5162	5268	5266 258	4969	4668 634	4447 63	4086	3863 22	4021	3615	3162
27	7091 637	6615 559	5855	5838	5793	5722	5562	5496	5173	5408	5336	5351 53	5115	5112	5095	5213	5194 054	4906	4582 822	4392 03	4060	3798 55	3957	3572	3106
28	7028 457	6530 715	5805	5788	5748	5671	5508	5444	5116	5352	5250	5298 00	5030	5029	5023	5158	5120 818	4843	4516 346	4336 44	3993	3753 49	3893	3529	3049
29	6964 884	6447 667	5734	5735	5698	5619	5458	5389	5060	5294	5104	5243 00	4942	4951	4955	5103	5046 663	4781	4449 316	4280 84	3946	3708 43	3828	3486	2986
30	6900 810	6366 071	5702	5681	5642	5565	5397	5324	5005	5255	5079	5188 50	4863	4882	4894	5047	4971 732	4718	4381 832	4217 31	3898	3662 97	3764	3442	2923
31	6837 163	6285 700	5649	5626	5585	5508	5339	5274	4951	5175	4993	5127 99	4784	4812	4833	4988	4896 141	4636	4313 978	4153 77	3849	3617 10	3700	3393	2859
32	6772 808	6206 242	5595	5570	5528	5449	5281	5214	4897	5116	4907	5067 99	4706	4742	4773	4928	4819 996	4593	4245 828	4090 23	3800	3570 86	3635	3356	2794
33	6707 468	6128 280	5540	5511	5472	5390	5222	5149	4844	5056	4821	5005 55	4625	4673	4715	4868	4743 385	4530	4177 440	4026 69	3751	3524 60	3571	3312	2730
34	6641 060	6051 918	5483	5451	5417	5332	5163	5084	4792	4996	4750	4963 10	4560	4609	4632	4808	4666 381	4468	4108 859	3963 16	3701	3478 34	3506	3269	2665
35	6573 575	5976 871	5424	5392	5362	5275	5104	5019	4740	4936	4679	4830 65	4494	4548	4597	4748	4589 040	4405	4050 116	3891 68	3652	3432 50	3442	3227	2600
36	6503 465	5902 578	5364	5331	5307	5218	5045	4939	4688	4877	4607	4820 65	4420	4475	4525	4688	4511 399	4332	3971 226	3820 20	3602	3386 65	3378	3184	2535
37	6432 901	5828 140	5303	5270	5251	5160	4986	4903	4637	4817	4536	4762 61	4338	4399	4455	4628	4433 178	4230	3902 191	3768 72	3553	3340 83	3313	3142	2670
38	6362 224	5753 425	5241	5206	5194	5103	4927	4847	4587	4757	4464	4704 57	4267	4334	4395	4568	4355 282	4186	3833 001	3677 24	3504	3294 99	3249	3099	2404
39	6291 591	5677 847	5170	5145	5136	5045	4868	4791	4538	4697	4393	4646 53	4193	4264	4330	4508	4276 799	4115	3765 631	3605 76	3453	3248 75	3185	3057	2336
40	6221 105	5602 015	5117	5079	5075	4983	4805	4733	4490	4635	4321	4587 50	4122	4199	4269	4448	4197 995	4010	3694 042	3534 28	3403	3202 09	3120	3013	2264
41	6151 371	5526 266	5055	5015	5009	4914	4736	4668	4441	4565	4257	4522 51	4052	4133	4208	4383	4118 829	3967	3624 185	3462 80	3353	3155 43	3055	2970	2194
42	6081 708	5452 564	4993	4952	4940	4845	4666	4593	4392	4494	4193	4449 04	3982	4067	4146	4311	4032 239	3894	3553 999	3391 32	3303	3106 67	2989	2923	2121
43	6012 191	5378 865	4931	4888	4869	4775	4596	4517	4342	4422	4129	4371 00	3906	3995	4079	4231	3959 156	3830	3483 415	3311 90	3252	3056 23	2922	2872	2048
44	5942 983	5306 057	4869	4822	4798	4707	4526	4461	4291	4351	4064	4292 93	3846	3940	4030	4151	3878 495	3747	3412 351	3232 47	3202	3005 09	2855	2818	1978
45	5874 030	5234 014	4806	4754	4727	4638	4455	4366	4239	4278	4000	4215 41	3784	3876	3965	4071	3797 166	3674	3340 722	3153 05	3 52	2951 11	2788	2762	1908
46	5805 746	5162 448	4742	4686	4657	4570	4382	4294	4186	4302	3929	4139 32	3710	3801	3888	3991	3715 064	3601	3268 433	3073 63	3102	2897 29	2721	2705	1840
47	5737 805	5093 363	4675	4618	4588	4503	4309	4227	4132	4123	3857	4065 68	3646	3737	3823	3911	3632 085	3528	3195 387	2994 21	3051	2842 63	2654	2646	1771
48	5670 042	5023 451	4603	4547	4521	4435	4236	4162	4077	4015	3786	3993 03	3577	3671	3759	3831	3548 117	3455	3121 483	2914 79	3001	2787 55	2587	2587	1702
49	5602 408	4952 114	4532	4475	4458	4367	4163	4097	4021	3967	3700	3920 37	3508	3597	3681	3751	3463 048	3382	3046 619	2835 36	2950	2731 65	2520	2526	1639
50	5534 900	4877 910	4455	4400	4397	4296	4087	4027	3964	3885	3621	3842 71	3442	3526	3607	3666	3376 765	3309	2970 695	2748 00	2899	2675 32	2452	2465	1577
51	5468 501	4799 446	4375	4321	4338	4222	4007	3952	3905	3801	3536	3757 50	3375	3455	3532	3571	3289 158	3225	2893 611	2660 64	2846	2618 20	2383	2404	1515
52	5401 832	4712 447	4293	4236	4276	4145	3925	3872	3843	3714	3443	3669 84	3308	3384	3457	3476	3200 123	3142	2815 274	2573 27	2791	2559 46	2312	2342	1453
53	5334 592	4619 716	4208	4148	4211	4067	3842	3787	3777	3626	3357	3579 74	3231	3309	3384	3381	3109 561	3068	2735 597	2485 91	2734	2499 10	2242	2279	1393
54	5265 817	4520 420	4120	4055	4143	3988	3757	3702	3707	3536	3271	3489 63	3171	3244	3314	3286	3017 387	2965	2654 504	2398 54	2674	2437 13	2172	2215	1336
55	5194 957	4415 155	4030	3961	4073	3907	3671	3617	3631	3445	3186	3399 54	3106	3177	3245	3191	2923 527	2871	2571 919	2319 12	2612	2373 51	2101	2150	1280
56	5120 399	4304 770	3937	3866	4000	3824	3584	3532	3550	3353	3100	3309 42	3027	3090	3150	3096	2827 923	2766	2487 821	2239 70	2548	2307 83	2031	2082	1225
57	5043 146	4189 245	3841	3768	3924	3736	3492	3447	3465	3258	3007	3219 32	2952	3006	3057	3001	2730 533	2682	2402 144	2160 28	2483	2239 67	1961	2011	1169
58	4962 388	4070 398	3743	3668	3842	3646	3398	3357	3377	3161	2914	3124 21	2885	2933	2978	2901	2631 344	2557	2314 884	2080 86	2417	2169 88	1890	1938	1118
59	4878 173	3949 880	3643	3566	3749	3552	3302	3267	3286	3063	2821	3029 11	2816	2859	2899	2801	2530 564	2443	2226 048	2001 43	2349	2099 25	1820	1865	1068
60	4790 613	3828 144	3542	3422	3643	3455	3204	3167	3191	2964	2729	2929 11	2736	2774	2808	2701	2427 628	2283	2135 668	1922 01	2280	2027 41	1749	1790	1014
61	4701 717	3707 731	3440	3357	4521	3347	3098	3057	3092	2858	2636	2821 66	2656	2688	2716	2596	2323 203	2218	2043 802	1842 59	2209	1953 93	1679	1714	962
62	4609 205	3588 657	3337	3253	3395	3232	2983	2939	2990	2764	2543	2707 74	2576	2602	2624	2486	2217 192	2098	1950 540	1763 17	2138	1880 05	1609	1638	912
63	4512 015	3469 557	3234	3146	3268	3110	2862	2819	2883	2623	2450	2590 30	2487	2511	2551	2371	2109 733	1993	1856 005	1683 75	2065	1805 78	1539	1562	863
64	4409 301	3346 330	3130	3037	3143	2983	2736	2699	2778	2490	2350	2472 85	2389	2411	2428	2356	2001 004	1888	1760 352	1604 32	1992	1731 10	1470	1486	813
65	4300 432	3218 997	3024	2926	3018	2851	2608	2579	2669	2375	2250	2335 40	2301	2317	2328	2341	1891 224	1754	1663 775	1524 90	1918	1656 03	1401	1410	763
66	4185 632	3087 900	2918	2812	2894	2714	2475	2459	2559	2246	2150	2237 95	2204	2212	2215	2026	1780 659	1639	1566 507	1445 48	1844	1581 37	1332	1335	715
67	4063 635	2946 196	2811	2695	2771	2573	2337	2339	2448	2111	2050	2120 51	2101	2102	2098	1911	1669 617	1524	1468 819	1366 05	1769	1507 14	1264	1262	667
68	3935 258	2801 283	2704	2578	2648	2426	2195	2219	2336	1973	1950	2000 51	2005	2002	1994	1791	1558 432	1409	1371 024	1286 64	1695	1433 32	1193	1187	618
69	3801 503	2653 666	2596	2458	2525	2275	2050	2099	2223	1884	1850	1877 95	1907	1905	1898	1666	1447 563	1292	1273 473	1207 21	1621	1359 95	1126	1114	574
70	3660 852	2503 329	2487	2335	2401	2121	1903	1979	2109	1693	1750	1755 40	1807	1799	1786	1541	1337 399	1189	1176 556	1127 79	1547	1286 97	1058	1043	530
71	3509 204	2350 310	2378	2212	2277	1966	1761	1849	1993	1565	1650	1627 96	1707	1693	1674	1416	1228 440	1075	1080 701	1040 43	1472	1214 86	989	973	489
72	3350 211	2195 927	2269	2087	2145	1809	1618	1709	1874	1435	1550	1495 62	1606	1586	1562	1291	1121 210	971	986 367	955 06	1397	1143 61	920	905	448
73	3184 222	2043 408	2159	1963	1997	1650	1475	1559	1749	1307	1450	1360 93	1500	1472	1441	1171	1016 260	886	894 039	865 70	1322	1073 19	853	839	408
74	3009 854	1895 790	2059	1835	1894	1494	1335	1399	1617	1182	1350	1221 35	1380	1361	1328	1051	914 171	761	804 228	778 33	1247	1003 61	783	775	373
75	2819 129	1752 128	1938	1708	1675	1345	1199	1249	1479	1061	1250	1091 77	1283	1252	1218	961	815 534	668	717 453	698 91	1172	935 01	714	712	339
76	2648 552	1612 228	1827	1583	1515	1200	1070	1109	1337	944	1143	969 64	1163	1132	1097	836	720 947	585	634 242	619 49	1098	866 99	645	650	305
77	2460 598	1484 134	1715	1458	1359	1034	947	979	1198	833	1036	854 95	1054	1019	981	736	631 001	511	555 113	540 07	1023	800 76	579	592	272
78	2265 378	1354 652	1600	1336	1213	937	831	859	1064	730	929	750 26	963	900	856	656	546 262	449	480 366	460 65	950	735 78	517	534	239
79	2066 976	1221 918	1481	1213	1084	819	724	769	936	633	821	633 03	836	792	763	561	467 766	385	411 070	389 17	877	671 63	458	479	213
80	1869 269	1089 387	1337	1090	953	712	624	649	812	539	714	563 24	733	700	654	481	394 492	334	347 048	325 63	804	609 17	403	427	170
81	1674 427	938 082	1219	968	837	615	533	554	697	454	621	478 44	651	609	563	406	328 351	283	288 862	270 04	731	547 96	348	376	148
82	1492 007	828 664	1069	847	725	521	449	464	590	380	536	398 66	559	518	472	336	269 172	240	236 800	222 38	660	488 40	297	328	127
83	1325 685	706 429	923	729	623	431	372	379	492	315	457	323 87	472	435	393	271	217 184	198	191 065	182 67	589	430 93	248	283	108
84	1174 803	591 807	783	616	529	350	304	299	404	259	393	234 08	409	370	326	211	172 699	167	151 753	150 90	519	375 12	201	240	89
85	1038 102	483 501	651	509	445	280	243	224	327	207	321	191 84	310	276	238	161	135 104	136	118 856	119 13	450	320 98	160	200	78
86	912 010	383 801	527	411	367	220	191	169	261	163	257	144 50	250	219	185	121	104 853	115	92 243	87 36	382	269 32	124	163	61
87	793 338	291 483	413	325	296	175	150	129	206	126	200	109 61	201	173	142	91	81 448	91	71 633	63 56	317	220 54	95	130	68
88	659 713	211 236	315	252	232	140	119	99	159	98	150	83 68	157	135	110	69	64 451	73	56 700	39 71	254	173 40	71	98	36
89	571 447	145 834	235	193	181	111	94	76	117	77	107	63 75	123	102	78	52	55 263	63	46 857	23 83	194	130 35	53	70	29
90	465 210	96 400	170	148	142	87	73	58	80	59	71	47 79	100	83	62	38	43 536	52	38 300	7 94	143	92 64	39	46	22
91	362 796	60 050	120	111	105	67	56	43	50	45	50	34 32	77	64	47	26	35 164	42	30 933	»	111	69 99	29	32	18
92	267 246	36 991	84	82	75	51	42	31	28	33	36	23 85	54	45	32	17	28 035	47	24 683	»	86	53 87	21	24	14
93	184 966	21 381	56	57	56	38	31	21	14	14	21	15 38	39	33	23	10	22 032	31	19 382	»	68	42 22	14	19	10
94	120 564	11 566	35	36	40	28	22	13	6	11	14	8 60	29	24	15	4	17 044	21	14 994	»	53	32 97	8	15	8
95	73 301	5 796	20	20	30	19	15	7	3		7	3 94	24	19	11	1	12 058		11 400	»	41	25 73	3	11	5
96	42 337	2 689	10	9	23	12	10	3	2	7	4	1 50	18	14	7	»	9 664	»	8 502	»	32	20 10	1	9	»
97	21 422	1 008	4	2	18	6	5	1	1	2	4	50	14	10	4	»	7 056	»	6 207	»	25	15 69	»	7	»
98	9 212	252	1	»	14	3	3	»	»	1	3	»	10	7	2	»	5 029	»	4 424	»	19	12 07	»	6	»
99	3 234	»	»	»	11	1	1	»	»	»	1	»	7	5	2	»	3 491	»	3 071	»	14	8 85	»	4	»
100	996	»	»	»	9	»	»	»	»	»	»	»	4	3	1	»	2 351	»	2 068	»	11	6 42	»	2	»

(*Second Appendix to Chapter XXX[th].*)

SPECIFIC INTENSITIES OF LIFE,

Or the **RATES OF MORTALITY** referred to each interval of age; as resulting from **TWENTY-FIVE** different statements of the **LAW**, by various authors.

Completed years of age.	No 1. FINLAISON: Annuitants, Females.	No 2. FINLAISON: Annuitants, Males.	No 3. BABBAGE: Assurables.	No 4. DAVIES: Assurables.	No 5. MILNE: Population of Carlisle.
0	7·763	6·794	6·498	6·498	6·498
1	71·561	55·789	12·406	12·406	12·406
2	81·466	66·368	15·404	15·404	15·404
3	91·091	80·088	26·355	26·355	26·355
4	94·549	96·332	34·816	34·816	34·816
5	110·861	115·227	56·174	56·174	56·174
6	126·961	136·491	81·415	81·415	81·415
7	150·080	153·184	113·690	113·690	113·690
8	174·767	165·555	152·000	152·000	152·000
9	202·716	171·347	196·758	196·758	196·758
10	228·861	177·623	258·400	258·400	222·759
11	237·957	182·309	247·500	257·400	207·452
12	227·211	187·168	228·893	237·408	200·000
13	209·501	190·165	212·700	236·408	192·970
14	187·161	183·305	204·871	211·867	181·000
15	145·771	168·237	197·500	197·687	161·538
16	133·101	145·756	190·545	185·118	149·071
17	124·612	125·549	183·971	173·889	144·628
18	119·119	107·374	177·743	159·590	143·628
19	116·071	94·860	171·833	150·854	142·628
20	117·971	85·821	166·216	149·854	141·628
21	117·162	74·306	160·868	148·854	143·976
22	116·553	71·554	151·875	140·977	142·976
23	115·958	70·665	143·690	139·977	141·976
24	115·202	70·652	136·205	132·800	140·976
25	115·172	71·525	129·326	128·935	136·721
26	113·845	76·999	122·979	125·213	135·721
27	112·242	77·974	117·100	116·760	126·733
28	110·509	78·639	113·824	109·208	114·960
29	108·748	79·019	110·654	106·204	101·750
30	108·429	79·209	107·585	103·291	98·982
31	106·229	79·108	104·611	100·464	97·982
32	103.662	79·606	101·727	94·407	98·714
33	100·987	80·254	97·193	91·850	99·491
34	98·423	80·641	92·932	92·390	98·491
35	93·765	80·449	90·400	88·393	97·491
36	92·157	79·295	87·934	87·393	94·768
37	91·018	78·007	85·532	82·344	92·123
38	90·075	76·095	84·532	82·635	89·552
39	89·259	74·904	83·532	80·359	84·197
40	89·212	73·955	82·532	79·359	76·894
41	88·301	74·222	81·532	79·603	72·594
42	87·488	73·985	80·532	77·375	69·577
43	86·842	73·887	79·532	74·061	68·577
44	86·214	73·640	77·286	70·912	67·577
45	86·025	73·137	75·094	69·912	67·529
46	85·451	74·727	70·776	68·912	67·493
47	84·674	72·854	66·786	65·042	68·478
48	83·836	70·417	63·082	63·153	71·762
49	82·988	66·737	58·857	59·667	73·082
50	83·410	62·145	55·687	55·696	74·525
51	81·977	55·185	53·354	50·835	69·968
52	80·229	50·819	50·506	48·136	65·784
53	77·666	46·525	47·818	44·602	61·926
54	74·311	42·943	45·778	43·138	59·186
55	69·864	39·998	43·333	41·695	55·795
56	66·112	37·263	41·010	39·449	52·632
57	62·449	35·249	39·194	37·680	47·854
58	58·925	33·774	37·430	35·961	41·312
59	55·642	32·446	36·069	34·288	35·368
60	53·890	31·792	34·725	32·971	29·861
61	50·823	31·138	33·398	32·279	27·944
62	47·425	30·131	32·398	30·402	26·732
63	43·928	28·156	31·096	28·862	26·144
64	40·501	26·280	29·528	27·360	25·144
65	37·460	24·554	28·528	25·667	24·339
66	34·310	21·791	27·271	24·241	23·528
67	31·654	20·331	26·271	22·847	22·528
68	29·422	18·977	25·037	21·483	21·528
69	27·031	17·651	23·817	19·984	20·363
70	24·137	16·360	22·817	18·984	19·363
71	22·071	15·223	21·817	17·696	16·993
72	20·138	14·402	20·627	16·831	14·678
73	18·261	13·838	19·627	15·336	12·801
74	16·664	13·196	18·459	14·449	11·090
75	15·659	12·524	17·459	13·664	10·469
76	14·091	12·586	16·312	12·664	9·712
77	12·604	11·462	14·913	11·951	9·308
78	11·418	10·206	13·445	10·862	9·189
79	10·456	9·220	11·944	9·862	8·445
80	9·593	8·297	9·833	8·934	8·216
81	9·181	7·403	8·127	8·000	7·473
82	8·969	6·779	7·322	7·178	7·108
83	8·786	6·163	6·593	6·451	6·628
84	8·600	5·464	5·932	5·757	6·298
85	8·227	4·850	5·250	5·194	5·705
86	7·685	4·157	4·623	4·779	5·169
87	7·044	3·632	4·214	4·452	4·625
88	6·228	3·231	3·937	4·271	4·549
89	5·380	2·949	3·615	4·289	4·641
90	4·543	2·652	3·400	4·000	3·838
91	3·797	2·604	3·333	3·828	3·500
92	3·248	2·370	3·000	3·280	3·571
93	2·872	2·174	2·667	2·714	3·857
94	2·562	2·008	2·333	2·250	4·000
95	2·358	1·866	2·000	1·818	4·286
96	2·024	1·600	1·667	1·286	4·600
97	1·754	1·333	1·333	1·000	4·500
98	1·538	1·000	1·000	.	4·667
99	1·333	.	.	.	5·500
100	1·000	.	.	.	.

Completed years of age.	No 6. NICANDER: Sweden, Females.	No 7. NICANDER: Population of Sweden.	No 8. WARGENTIN: Sweden, Females.	No 9. DEPARCIEUX: Select lives in France.	No 10. NICANDER: Sweden, Males.
0	5·260	4·963	4·785	5·922	4·708
1	14·861	14·678	15·270	20·580	14·505
2	24·849	24·238	21·120	26·747	23·655
3	32·511	31·991	28·168	33·283	31·353
4	43·110	42·140	50·311	44·120	41·206
5	47·667	45·588	55·475	52·585	43·934
6	62·804	60·541	62·257	62·206	57·884
7	88·173	83·205	75·671	70·146	78·654
8	114·702	108·678	90·671	75·975	104·833
9	129·620	127·060	104·617	88·014	124·633
10	139·804	137·022	119·558	103·517	134·348
11	152·024	148·976	134·022	121·347	142·651
12	158·575	151·585	152·975	137·140	148·561
13	170·351	162·474	173·686	150·103	155·128
14	169·351	161·474	172·686	157·162	158·184
15	168·351	164·811	171·686	152·053	153·154
16	167·351	159·500	149·350	140·000	156·158
17	161·974	158·500	148·350	129·523	151·180
18	160·974	149·625	140·333	120·319	142·854
19	151·975	141·548	136·093	112·160	135·256
20	147·293	134·159	135·093	106·885	122·830
21	142·810	130·200	134·093	103·887	116·857
22	135·364	121·125	133·093	100·981	111·314
23	131·378	117·673	129·091	98·164	106·151
24	127·543	114·340	125·244	95·429	103·204
25	118·796	108·981	124·244	92·772	100·345
26	115·440	105·943	110·920	90·190	97·571
27	112·196	103·000	105·692	90·754	96·571
28	109·058	100·145	98·982	91·357	92·276
29	104·056	97·375	97·982	92·000	89·729
30	97·632	93·052	88·900	92·685	87·250
31	93·356	92·052	67·900	91·685	87·712
32	92·356	89·508	80·215	92·396	85·267
33	92·931	88·508	79·215	93·154	84·267
34	93·544	87·508	78·215	92·154	83·267
35	92·544	86·508	83·650	91·154	83·661
36	69·966	85·508	88·554	91·922	61·283
37	90·526	84·508	87·554	92·739	80·283
38	87·983	83·508	86·554	93·612	79·283
39	81·371	77·270	82·603	94·542	75·758
40	72·217	69·638	72·815	91·633	66·214
41	71·217	67·657	62·240	90·633	64·296
42	69·214	66·657	60·434	87·840	62·417
43	70·221	65·657	59·434	85·137	62·282
44	63·217	63·746	59·213	62·519	59·603
45	68·206	60·973	60·639	79·981	56·289
46	68·209	60·027	64·090	77·518	53·190
47	66·221	59·027	65·031	75·127	52·859
48	65·221	58·027	64·031	72·804	51·859
49	61·507	54·776	58·529	70·544	48·378
50	58·054	5 ·087	53·693	67·186	46·250
51	54·831	48·866	49·400	62·984	43·690
52	53·141	47·289	45·553	58·227	42·205
53	51·481	45·200	44·553	53·957	40·289
54	49·235	43·686	43·553	48·776	38·857
55	47·072	42·195	42·553	44·827	37·446
56	43·455	38·957	41·553	41·765	35·295
57	41·511	37·149	38·300	39·375	33·588
58	38·787	35·396	37·300	37·110	32·255
59	36·619	33·694	32·670	34·589	30·939
60	31·991	30·226	28·791	32·232	27·962
61	29·104	26·939	25·907	30·314	25·070
62	26·492	24·653	24·492	28·476	22·678
63	24·488	22·714	23·492	26·963	21·325
64	22·598	21·375	22·492	25·486	20·000
65	20·810	19·609	21·492	24·264	18·411
66	19·248	17·935	20·492	23·054	16·637
67	17·503	16·458	19·492	21·857	15·297
68	16·066	15·138	18·492	20·673	14·194
69	14·773	14·138	17·492	19·500	13·483
70	13·684	13·229	15·223	18·181	12·767
71	12·522	12·315	13·207	16·748	12·038
72	11·377	11·315	11·393	14·992	11·211
73	10·577	10·536	9·744	13·250	10·456
74	9·894	9·816	9·327	11·717	9·769
75	9·392	9·295	8·921	10·415	9·068
76	8·824	8·699	8·531	9·619	8·582
77	8·378	8·164	8·158	8·940	8·010
78	7·941	7·766	7·809	8·312	7·526
79	7·654	7·240	7·490	7·548	6·734
80	7·340	6·857	6·832	7·061	6·341
81	6·543	6·345	6·156	6·514	6·135
82	5·789	5·831	5·459	6·020	5·846
83	5·321	5·471	4·737	5·591	5·625
84	5·000	4·984	3·987	5·247	4·981
85	4·667	4·673	4·073	4·955	4·705
86	4·889	4·659	4·225	4·745	4·405
87	5·000	4·839	4·300	4·383	4·500
88	4·828	4·760	4·304	3·786	4·667
89	4·625	4·476	4·222	3·162	4·278
90	4·350	4·294	3·867	2·667	4·214
91	4·187	4·000	3·583	2·273	3·750
92	3·923	3·818	3·100	2·000	3·667
93	3·800	3·444	2·625	1·750	3·429
94	3·111	3·143	2·167	2·000	2·833
95	1·583	.	.	3·000	2·750
96	2·000	.	.	2·000	2.333
97	2·000	.	.	.	2·000
98	.	.	.	.	2·000
99	.	.	.	.	.
100	.	.	.	.	.

Completed years of age.	No 11. KERSSEBOOM: Annuitants in Holland.	No 12. WARGENTIN: Population of Sweden.	No 13. RICKMAN: Essex, Females.	No 14. RICKMAN: Population of Essex.	No 15. RICKMAN: Essex, Males.
0	5·092	4·551	5·438	5·015	4·667
1	22·510	15·332	17·107	16·406	15·777
2	23·848	21·249	24·381	23·567	22·783
3	27·867	28·381	35·946	35·117	34·157
4	34·266	47·008	43·683	45·712	48·099
5	56·443	53·550	65·421	62·761	60·252
6	55·901	61·338	71·062	68·694	67·112
7	54·451	72·373	80·905	73·711	67·489
8	101·891	86·108	91·945	92·169	91·186
9	100·891	98·728	105·138	104·403	105·217
10	99·891	114·195	102·719	103·403	105·983
11	109·121	133·201	101·719	104·082	104·983
12	110·018	141·303	105·672	114·327	127·812
13	124·280	159·022	93·897	102·180	110·673
14	123·280	158·022	95·712	101·180	120·640
15	122·280	159·141	83·347	92·636	104·947
16	121·280	148·370	73·524	85·183	100·424
17	120·280	147·370	73·398	80·770	88·879
18	93·187	134·360	61·948	68·640	77·333
19	92·187	131·886	64·261	66·862	70·679
20	89·785	122·260	62·581	65·862	69·679
21	101·246	121·234	61·581	65·616	67·841
22	100·246	120·259	53·657	58·495	63·000
23	88·391	111·929	53·680	60·002	68·279
24	70·797	109·844	53·196	59·002	66·437
25	64·871	108·866	54·327	62·118	71·712
26	58·376	102·837	51·743	62·590	77·045
27	62·046	99·973	53·947	61·590	70·764
28	61·046	96·327	57·159	64·474	73·868
29	60·753	96·202	62·557	71·754	81·230
30	59·056	85·744	61·557	69·743	80·230
31	58·058	85·466	61·333	68·743	80·550
32	57·058	81·166	58·099	68·725	82·293
33	67·901	80·153	71·112	73·016	74·841
34	66·901	79·153	69·091	75·557	84·582
35	64·986	81·344	60·730	62·301	63·847
36	64·887	83·057	53·902	58·682	64·643
37	63·000	82·057	61·099	67·677	74·250
38	62·873	81·043	57·662	61·914	67·615
39	61·014	78·728	59·056	65·700	70·984
40	67·515	70·588	58·889	63·621	69·984
41	66·515	61·556	57·889	62·621	67·871
42	65·515	57·010	52·395	56·466	61·881
43	63·523	56·003	65·100	72·636	83·245
44	63·500	55·364	62·032	61·562	62·000
45	56·338	55·400	51·135	51·680	51·494
46	54·569	56·210	57·969	59·391	59·815
47	54·324	55·963	52·841	56·621	59·733
48	44·023	54·955	51·841	49·608	48·191
49	46·835	50·481	53·152	50·662	49·743
50	42·600	45·097	51·373	49·662	48·093
51	38·022	42·864	50·373	46·662	47·093
52	40·035	40·731	42·935	45·120	47·356
53	39·035	39·726	53·850	50·908	48·343
54	38·482	38·735	48·785	48·418	48·029
55	37·047	37·722	39·316	36·517	34·158
56	33·333	36·731	40·360	36·786	33·870
57	32·333	33·648	40·060	41·176	38·696
58	31·333	32·852	41·812	39·635	37·696
59	30·663	30·291	35·200	33·635	31·857
60	29·344	27·260	34·200	32·255	30·522
61	28·344	24·769	33·200	31·255	29·522
62	27·344	23·056	28·944	28·593	28·215
63	24·500	22·054	25·378	25·110	24·573
64	23·500	21·054	27·148	25·649	24·280
65	22·500	20·054	23·722	22·067	20·602
66	21·500	19·056	21·398	20·109	18·932
67	20·500	17·671	21·885	21·020	20·173
68	19·500	16·323	20·459	20·639	20·771
69	18·500	15·324	19·070	17·972	16·946
70	17·500	13·774	18·070	16·972	15·946
71	16·500	12·301	16·901	15·822	14·946
72	15·500	11·104	15·151	13·912	12·909
73	14·500	9·750	13·636	13·261	12·752
74	13·500	9·425	12·991	12·486	12·073
75	11·682	8·939	10·692	10·433	10·066
76	10·682	8·454	10·670	10·016	9·457
77	9·682	8·166	9·496	8·563	7·724
78	8·602	7·716	8·813	8·333	7·835
79	7·673	7·273	8·989	8·609	8·187
80	7·677	6·642	8·076	7·692	7·187
81	7·306	5·997	7·076	6·692	6·187
82	6·785	5·330	6·425	6·241	5·975
83	7·140	4·641	7·492	6·692	5·866
84	5·458	4·082	4·131	3·936	3·705
85	5·016	4·052	5·167	4·842	4·491
86	4·509	4·142	5·102	4·761	4·302
87	4·000	4·227	4·568	4·553	4·437
88	3·488	4·199	4·617	4·091	3·437
89	2·972	3·994	5·348	5·368	4·875
90	3·381	3·548	4·348	4·366	4·133
91	3·571	3·278	3·348	3·368	3·133
92	2·400	2·816	3·600	3·750	3·556
93	3·000	2·203	3·900	3·667	2·875
94	2·000	1·883	5·800	4·800	3·750
95	.	1·615	4·000	3·800	2·750
96	.	1·500	4·500	3·500	2·333
97	.	.	3·500	3·333	2·000
98	.	.	3·333	3·500	.
99	.	.	2·333	2·500	.
100	.	.	.	3·000	.

Completed years of age.	No 16. WARGENTIN: Sweden, Males.	No 17. DUVILLARD: Towns in France, — Small-pox influence abstracted.	No 18. SUSSMILCH: Population of Braodenburgh	No 19. DUVILLARD: The towns in France.	No 20. HALLEY: Population of Breslaw.
0	4·348	4·635	4·815	4·302	4·860
1	15·400	10·486	10·839	8·021	6·897
2	21·365	20·566	18·116	14·244	15·000
3	28·596	35·382	25·074	24·067	21·489
4	44·153	55·303	28·365	38·472	27·143
5	51·784	79·500	31·788	57·590	33·272
6	60·457	105·390	41·754	79·730	39·444
7	69·367	128·470	57·212	101·164	57·664
8	82·040	144·514	69·595	117·743	68·002
9	93·508	151·934	110·808	127·265	74·444
10	109·327	152·024	135·952	130·184	82·622
11	132·400	147·387	134·952	128·435	93·295
12	131·400	140·361	137·219	124·027	107·674
13	146·700	132·533	132·976	118·441	106·651
14	145·700	124·771	131·976	112·569	105·674
15	148·410	117·500	130·976	106·884	104·674
16	147·410	110·873	133·146	101·602	103·374
17	146·410	104·914	129·003	96·794	102·674
18	128·886	99·583	128·003	92·470	101·673
19	127·886	94·833	127·003	88·599	100·673
20	111·660	90·596	101·769	85·137	99·673
21	110·660	86·810	100·769	82·041	98·673
22	109·660	83·424	99·769	79·268	83·707
23	98·782	80·381	98·769	76·771	96·506
24	97·782	77·648	95·925	74·525	95·506
25	96·782	75·161	81·145	72·490	80·993
26	95·782	72·946	78·873	70·635	79·993
27	94·782	70·913	77·873	68·939	78·993
28	93·782	69·056	78·113	67·378	77·993
29	91·125	67·351	75·889	65·931	67·373
30	85·542	65·771	76·097	64·577	66·373
31	63·133	64·300	73·905	63·301	65·373
32	82·133	62·915	72·905	62·084	64·373
33	81·133	61·599	73·065	60·913	63·373
34	80·133	60·335	70·921	59·771	55·444
35	79·133	59·106	60·342	58·646	54·444
36	78·133	57·897	59·342	57·525	53·444
37	77·133	56·697	58·342	56·398	52·444
38	76·133	55·493	57·342	55·254	51·444
39	75·133	54·271	56·342	54·084	50·444
40	68·431	53·028	55·342	52·880	49·444
41	60·875	51·751	54·342	51·637	48·444
42	53·887	50·438	52·622	50·351	42·701
43	52·887	49·084	52·329	49·018	41·701
44	51·687	47·689	51·329	47·639	40·701
45	50·887	46·249	50·329	46·213	39·701
46	49·887	44·771	49·329	44·745	38·701
47	48·887	43·256	48·329	43·237	37·701
48	47·887	41·709	47·329	41·695	36·701
49	44·129	40·136	46·329	40·127	32·456
50	38·589	38·544	39·393	38·538	31·456
51	37·589	36·942	38·855	36·936	30·456
52	36·569	35·336	37·405	35·334	29·456
53	35·589	33·736	32·882	33·734	28·456
54	34·589	32·148	31·543	32·147	30·201
55	33·589	30·579	27·343	30·579	29·201
56	32·597	29·037	26·596	29·037	28·201
57	30·010	27·529	25·352	27·529	27·201
58	29·010	26·058	22·430	26·058	26·201
59	28·010	24·630	21·243	24·630	25·201
60	25·724	23·248	20·243	23·248	24·201
61	23·600	21·915	19·243	21·915	23·201
62	21·617	20·633	16·243	20·633	22·201
63	20·617	19·404	17·243	19·404	21·201
64	19·617	18·227	16·386	18·227	20·201
65	18·617	17·106	15·352	17·106	19·201
66	17·617	16·036	14·252	16·036	18·201
67	15·925	15·019	13·252	15·019	17·201
68	14·328	14·054	12·252	14·054	16·201
69	13·328	13·140	11·351	13·140	15·201
70	12·328	12·274	11·238	12·274	12·909
71	11·328	11·456	10·337	11·456	11·909
72	10·758	10·683	9·248	10·683	10·909
73	9·758	9·955	8·327	9·955	9·909
74	9·555	9·268	8·106	9·268	9·800
75	8·962	8·622	8·048	8·622	8·800
76	6·360	8·015	7·905	8·015	7·800
77	8·178	7·446	8·244	7·446	6·800
78	7·600	6·915	7·127	6·915	6·444
79	7·012	6·421	7·423	6·421	6·125
80	6·413	5·964	6·423	5·964	5·857
81	5·800	5·548	6·714	5·548	5·667
82	5·169	5·178	5·714	5·178	5·600
83	4·517	4·860	6·387	4·860	5·750
84	4·220	4·613	5·387	4·613	4·750
85	4·025	4·466	6·476	4·466	3·750
86	4·033	4·480	5·476	4·480	3·667
87	4·136	4·792	4·476	4·792	2·667
88	4·059	5·760	7·300	5·760	2·500
89	3·714	5·476	5·727	5·476	1·500
90	3·167	5·200	5·200	5·200	.
91	2·889	4·932	.	4·932	.
92	2·429	4·670	3·816	4·670	.
93	1·667	4·417	.	4·417	.
94	1·333	4·172	3·100	4·172	.
95	1·000	3·934	.	3·934	.
96	.	3·705	.	3·705	.
97	.	3·461	.	3·481	.
98	.	3·270	.	3·270	.
99	.	3·062	.	3·062	.
100	.	.	.	.	.

Completed years of age.	No 21. MOURGUE: Montpellier, Females.	No 22. MOURGUE: Population of Montpellier.	No 23. PRICE: Population of Northampton.	No 24. MOURGUE: Montpellier, Males.	No 25. SIMPSON: Population of London.
0	4·290	3·795	3·883	3·425	3·134
1	7·914	7·351	6·330	6·854	5·513
2	9·867	9·840	14·506	9·817	10·361
3	11·534	11·817	20·212	12·096	13·989
4	14·586	14·057	32·740	13·575	19·243
5	23·935	22·751	33·949	21·667	29·553
6	40·562	36·262	43·383	32·607	37·570
7	62·987	56·443	53·537	50·798	50·229
8	85·655	92·841	73·397	102·024	60·088
9	129·333	134·238	94·673	138·067	74·407
10	165·000	184·124	110·705	216·421	76·231
11	176·615	200·302	112·256	227·389	75·231
12	190·250	207·251	111·256	239·706	77·200
13	189·250	210·190	110·256	225·444	81·064
14	180·720	201·209	109·256	224·444	83·622
15	179·720	185·609	108·256	201·100	82·622
16	165·481	166·570	102·489	166·750	78·149
17	143·258	136·611	91·340	128·323	77·149
18	129·706	116·715	83·648	106·676	74·562
19	121·555	108·320	76·948	97·750	73·562
20	111·282	101·851	71·048	92·141	72·562
21	107·525	97·883	67·859	89·023	66·058
22	101·452	95·049	66·859	90·119	63·830
23	95·886	92·301	64·846	87·047	60·545
24	94·886	90·481	64·844	88·095	58·482
25	91·800	88·665	62·862	85·070	56·474
26	88·826	86·036	62·828	84·070	56·464
27	85·957	84·300	61·828	83·070	54·491
28	84·957	83·300	59·892	82·070	48·397
29	82·208	81·576	59·813	79·227	47·397
30	79·551	79·855	58·813	80·047	45·672
31	78·551	78·224	56·923	79·047	43·985
32	77·551	77·191	56·797	76·273	43·656
33	75·020	76·191	54·938	77·023	42·000
34	75·531	75·880	54·781	77·833	41·000
35	73·040	74·864	53·781	75·047	40·000
36	73·510	73·912	51·969	75·810	39·000
37	72·510	72·880	51·766	73·070	37·424
38	68·706	71·256	50·766	73·786	35·353
39	69·060	69·626	49·000	69·477	32·444
40	68·060	68·626	48·000	70·070	32·343
41	67·060	64·714	46·288	63·191	30·055
42	64·765	61·591	44·612	57·314	29·055
43	65·040	58·616	43·612	57·185	29·257
44	64·040	56·702	42·612	50·321	28·257
45	63·040	54·833	41·612	48·456	28·059
46	60·824	53·006	40·612	45·847	26·667
47	61·020	51·609	39·612	44·847	25·667
48	58·848	49·867	38·612	42·410	27·016
49	57·848	48·494	37·059	41·410	26·435
50	54·698	46·837	35·536	40·410	25·435
51	51·745	44·573	33·563	38·774	24·435
52	48·965	42·403	33·029	37·175	24·217
53	45·567	40·328	32·029	35·609	24·439
54	43·129	38·308	30·592	34·077	23·857
55	40·813	36·137	30·014	31·041	23·273
56	39·200	33·859	29·014	29·324	21·675
57	37·621	32·092	27·620	27·547	22·922
58	35·544	30·722	27·000	26·547	22·360
59	34·043	29·221	25·634	24·867	19·778
60	32·113	27·591	24·986	23·553	19·500
61	31·113	26·447	23·986	22·553	19·240
62	29·288	25·314	22·986	21·553	18·612
63	28·288	24·180	22·304	20·553	17·260
64	26·919	23·060	21·304	19·553	16·260
65	25·919	22·181	20·304	18·800	15·896
66	24·587	21·304	19·588	18·288	14·896
67	23·905	20·416	18·319	16·827	13·612
68	22·905	19·533	17·319	16·260	14·045
69	21·905	18·637	16·559	15·690	13·045
70	20·627	17·828	15·333	14·900	12·927
71	19·627	17·051	14·333	14·309	11·927
72	18·627	16·240	13·529	13·712	11·200
73	17·627	15·424	12·348	13·109	11·657
74	16·627	14·630	11·348	12·302	10·971
75	15·838	13·746	10·348	11·484	9·971
76	14·640	13·091	9·773	11·207	9·242
77	14·014	12·323	9·339	10·207	8·242
78	13·014	11·470	8·763	9·709	9·192
79	12·014	10·753	8·327	9·212	4·953
80	11·014	9·952	7·327	8·373	7·727
81	10·296	9·200	6·824	7·833	7·048
82	9·296	8·498	6·061	7·289	6·700
83	8·414	7·721	5·277	6·581	5·700
84	7·522	6·929	4·902	6·000	8·091
85	6·618	6·213	4·444	5·405	4·588
86	5·877	5·521	4·276	4·939	4·692
87	5·032	4·678	3·958	4·063	4·000
88	4·233	4·028	3·944	3·500	5·143
89	3·804	3·457	3·786	2·917	4·143
90	4·469	4·090	3·900	3·286	5·500
91	4·440	4·342	3·625	4·000	4·500
92	4·778	4·831	3·000	4·800	3·500
93	4·533	4·564	2·333	4·750	5·000
94	4·417	4·554	1·600	3·750	2·667
95	4·556	4·570	1·500	5·500	.
96	4·571	4·556	.	4·500	.
97	4·167	4·334	.	7·000	.
98	3·800	3·748	.	3·000	.
99	4·667	3·642	.	2·000	.
100	.	.	.	.	.

TABLES,

THAT EXHIBIT THE RELATIONS BETWEEN CAPITAL AND INCOME, AND THAT SOLVE ALL QUESTIONS DEPENDING ON THE OPERATION OF COMPOUND-INTEREST.

THE TABLES hereafter, which formed part of the volume entitled "DOCTRINE OF COMPOUND-INTEREST," are thought proper to be now reproduced, considering their extensive and perpetual utility; after having destroyed the remainder of that volume, with the exception only of a very few copies. The practical purpose of those tables merely requires that their arrangement and application should be clearly explained.

On the first appearance thereof, a great number amongst men of business lapsed into a singular mistake. As the express stipulation of Compound-interest in reciprocal contracts is by law forbidden, they conceived at a first glance that they could have nothing to do with a book thus described; forgetting that a multitude of transactions, in which they are daily concerned, —such as when valuing terminable annuities comparatively with those in perpetuity, and in many other instances, —necessarily involve, as a matter of course, the consideration of compound-interest; whatever the letter of the law may expressly provide on this subject.

We have here to understand that Capital accumulates in more elevated proportions, not only when the rate of interest is superior, but also when its instalments embrace only short periods, such as the half-yearly, or else the quarterly,

substituted for an annual periodicity; whence the necessity, on tabulating the various relations, either between an original and an improved capital, or between the capital and the income produced by it, to refer each set of computed results, to every distinct consideration of that income. Therefore the results for practical application, so as immediately to solve without error any propounded question, are here separately classed; with distinct reference, *first* to specific rates of interest, from that of *three* to that of *six per centum per annum*, as also proceeding by successive differences of *one-quarter per cent.*; and *secondly*, to the special intervals of accretion, whether *Annually*, *Half-yearly*, or *Quarterly*.

In every one of those cases, distinctly, there are *six* series of results, the enumeration of which follows; they being sufficient towards the solution of all questions that may arise of this nature, whenever the income of invested capital is regular and not contingent, but a matter of certainty.

A *first* class of questions relates to the IMPROVED PRINCIPAL; and one column of the tables accordingly states the gradual accumulation, at compound-interest, of each *unit* in any originally invested capital.

The counterpart of those respective statements is given in another column, solving a *second* class of questions, or that of the DISCOUNTED PRINCIPAL; being the *present value*, expressed by a decimal fraction, of each *unit* in any sum certainly forthcoming at a future period referred to.

A *third* class of questions relates to the CUMULATED ANNUITY; respecting which there is a column that indicates the gradually increasing capital, formed by a periodic accession of further income, in addition to its preceding instalments, and each time improved collectively with such capital.

The counterpart of this third class constitutes a *fourth*, of questions concerning the ANNUITY FOR CUMULATION. The latter denomination however involves some obscurity, which will disappear on substituting the more appropriate denomination of REDEMPTION-FUND; and the corresponding statements, in a specific column, shew the fractional part of *unity*, which at each instalment should be appropriated for improvement at compound-interest, so as to produce an entire and requisite capital, here represented by *unity*, at the expiry of any term of years.

A *fifth* class of questions is that of the present VALUE OF THE ANNUITY, to be continued during a specific term of years, but no longer; and the appropriate column, of those tables, expresses all such values by a quantity of years' purchase of the understood income for a whole year, whether this accrued by a single instalment, or by a plurality of instalments.

A *sixth* and last class of questions is the counterpart of the preceding one; and the column thereto answering shall, under the denomination of RATIO OF THE ANNUITY, solve any inquiry concerning the proportion of income produced during a limited time only, by any capital here represented by *unity*, and supposed to be invested in that particular shape.

The tables thus constructed are of *thirteen parts;* each part embraces an extent of *four pages*, referring to a specific rate of interest, and successively to all periods of time not exceeding *one hundred years*. Further each page has *three* subdivisions, comparatively exhibiting the divergent results of annual, of half-yearly, and of quarterly instalments; the rate of interest for one year, as also the considered period of years, being respectively alike in those three cases. Although any rates inferior to *three* or superior

to *six per cent.* are excluded from the tabulation, our intelligent readers will perceive that in all such instances the tables are still available; requiring only to deal with the inferior rates of interest as if they referred to half-yearly instalments, at a double rate per annum; and with the superior rates by supposing them refcrable to a period of two years, whence only half that rate to a single year represented by half-years in the tables.

But the question may occasionally consist of the required term of years, for producing any pre-stated result, under a certain datum of the rated interest. In all cases of this description the tables will immediately point out two proximate periods, the one superior and the other inferior to that which is required, — any difference being then no more than a fraction either of a whole year, of a half-year, or of a quarter; — and then the precise difference must be proportionate with any small quantities in which the two proximate results, announced by the table, may differ between themselves, as also from the previously stated quantity.

Lastly, the thirteen sets of tables are headed by indications of the prices of public stock, funded at 3, at 3 1/2, at 4, and at 5 *per cent. per ann.*, as corresponding with any specified rate of interest. It is always to be considered, that such stated prices are those of the bare stock, exclusive of any portion which may have accrued of the next forthcoming dividend, and which portion is usually understood to be sold with that stock.

The various objects to which all tables of this kind may apply have been so often mentioned and described in other books, that our reverting to those objects, or reproducing special examples of such application, would be useless.

Tables,

SOLVING THE QUESTIONS THAT DEPEND ON

Compound Interest,

ACCRUING EITHER ANNUALLY, HALF-YEARLY, OR QUARTERLY.

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.03.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.015.			RATIO *of* INTEREST: *QUARTERLY*, 0.0075.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
0¼	....	....	....	....	....	....	1.0075 000	0.2500 000	0.2481 39
½	....	....	....	1.0150 000	0.5000 000	0.4926 11	1.0150 563	0.5018 750	0.4944 31
¾	....	....	....	....	....	....	1.0226 692	0.7556 391	0.7388 89
1	1.0300 000	1.0000 000	0.9708 74	1.0302 250	1.0075 000	0.9779 42	1.0303 392	1.0113 064	0.9815 28
1¼	....	....	....	....	....	....	1.0380 667	1.2688 912	1.2223 60
½	....	....	....	1.0456 784	1.5226 125	1.4561 00	1.0458 522	1.5284 078	1.4613 99
¾	....	....	....	....	....	....	1.0536 961	1.7898 709	1.6986 59
2	1.0609 000	2.0300 000	1.9134 70	1.0613 636	2.0454 517	1.9271 92	1.0615 988	2.0532 949	1.9341 53
2¼	....	....	....	....	....	....	1.0695 608	2.3186 946	2.1678 94
½	....	....	....	1.0772 840	2.5761 335	2.3913 23	1.0775 825	2.5860 848	2.3998 95
¾	....	....	....	....	....	....	1.0856 644	2.8554 805	2.6301 69
3	1.0927 270	3.0909 000	2.828 612	1.0934 433	3.1147 755	2.8485 94	1.0938 069	3.1268 966	2.8587 28
3¼	....	....	....	....	....	....	1.1020 104	3.4003 483	3.0855 86
½	....	....	....	1.1098 449	3.6614 971	3.2991 07	1.1102 755	3.6758 509	3.3107 56
¾	....	....	....	....	....	....	1.1186 026	3.9534 198	3.5342 49
4	1.1255 088	4.1836 270	3.717 098	1.1264 926	4.2164 196	3.7429 63	1.1269 922	4.2330 721	3.7560 78
4¼	....	....	....	....	....	....	1.1354 446	4.5148 185	3.9762 56
½	....	....	....	1.1433 900	4.7796 658	4.1802 59	1.1439 604	4.7986 796	4.1947 95
¾	....	....	....	....	....	....	1.1525 401	5.0846 697	4.4117 07
5	1.1592 741	5.3091 358	4.579 707	1.1605 409	5.3513 627	4.6110 93	1.1611 841	5.3728 047	4.6270 05
5¼	....	....	....	....	....	....	1.1698 930	5.6631 008	4.8407 00
½	....	....	....	1.1779 489	5.9316 312	5.0355 59	1.1786 672	5.9555 740	5.0523 04
¾	....	....	....	....	....	....	1.1875 072	6.2502 408	5.2633 29
6	1.1940 523	6.4684 099	5.417 191	1.1956 182	6.5206 057	5.4537 53	1.1964 135	6.5471 176	5.4722 86
6¼	....	....	....	....	....	....	1.2053 866	6.8462 210	5.6796 89
½	....	....	....	1.2135 524	7.1184 148	5.8657 66	1.2144 270	7.1475 677	5.8855 47
¾	....	....	....	....	....	....	1.2235 352	7.4511 744	6.0898 73
7	1.2298 739	7.6624 622	6.230 283	1.2317 557	7.7251 910	6.2716 91	1.2327 117	7.7570 583	6.2926 78
7¼	....	....	....	....	....	....	1.2419 571	8.0652 362	6.4939 73
½	....	....	....	1.2502 321	8.3410 689	6.6716 17	1.2512 718	8.3757 255	6.6937 70
¾	....	....	....	....	....	....	1.2606 563	8.6885 434	6.8920 79
8	1.2667 701	8.8923 360	7.019 692	1.2689 855	8.9661 849	7.0656 32	1.2701 112	9.0037 075	7.0889 13
8¼	....	....	....	....	....	....	1.2796 371	9.3212 353	7.2842 80
½	....	....	....	1.2880 203	9.6006 777	7.4538 25	1.2892 343	9.6411 446	7.4781 94
¾	....	....	....	....	....	....	1.2989 036	9.9634 532	7.6706 64
9	1.3047 732	10.159 106	7.786 109	1.3073 406	10.244 688	7.8362 80	1.3086 454	10.288 179	7.8617 01
9¼	....	....	....	....	....	....	1.3184 602	10.615 340	8.0513 16
½	....	....	....	1.3269 567	10.898 358	8.2130 84	1.3283 486	10.944 955	8.2395 20
¾	....	....	....	....	....	....	1.3383 113	11.277 043	8.4263 22
10	1.3439 164	11.463 879	8.530 203	1.3468 550	11.561 832	8.5843 20	1.3483 436	11.611 620	8.6117 35
10¼	....	....	....	....	....	....	1.3584 612	11.948 708	8.7957 66
½	....	....	....	1.3670 578	12.235 261	8.9500 69	1.3686 497	12.288 323	8.9784 28
¾	....	....	....	....	....	....	1.3789 146	12.630 485	9.1597 30
11	1.3842 339	12.807 796	9.252 624	1.3875 637	12.918 790	9.3104 12	1.3892 564	12.975 214	9.3396 83
11¼	....	....	....	....	....	....	1.3996 758	13.322 528	9.5182 95
½	....	....	....	1.4083 772	13.612 572	9.6654 31	1.4101 734	13.672 447	9.6955 78
¾	....	....	....	....	....	....	1.4207 497	14.024 990	9.8715 42
12	1.4257 609	14.192 030	9.954 005	1.4295 028	14.316 760	10.015 20	1.4314 053	14.380 178	10.046 20
12¼	....	....	....	....	....	....	1.4421 409	14.738 029	10.219 55
½	....	....	....	1.4509 454	15.031 512	10.359 81	1.4529 570	15.098 564	10.391 61
¾	....	....	....	....	....	....	1.4638 541	15.461 804	10.562 39
13	1.4685 337	15.617 790	10.634 96	1.4727 095	15.756 984	10.699 32	1.4748 330	15.827 767	10.731 90
13¼	....	....	....	....	....	....	1.4858 943	16.196 475	10.900 15
½	....	....	....	1.4948 002	16.493 339	11.033 81	1.4970 385	16.567 949	11.067 15
¾	....	....	....	....	....	....	1.5082 663	16.942 209	11.232 90
14	1.5125 897	17.086 324	11.296 07	1.5172 222	17.240 739	11.363 36	1.5195 783	17.319 275	11.397 42
14¼	....	....	....	....	....	....	1.5309 751	17.699 170	11.560 72
½	....	....	....	1.5399 805	17.999 350	11.688 04	1.5424 574	18.081 947	11.722 80
¾	....	....	....	....	....	....	1.5540 258	18.467 528	11.883 67
15	1.5579 674	18.598 914	11.937 93	1.5630 802	18.769 341	12.007 92	1.5656 810	18.856 034	12.043 34
15¼	....	....	....	....	....	....	1.5774 236	19.247 455	12.201 83
½	....	....	....	1.5865 264	19.550 881	12.323 07	1.5892 543	19.641 811	12.359 14
¾	....	....	....	....	....	....	1.6011 737	20.039 125	12.515 27
16	1.6047 064	20.156 281	12.561 10	1.6103 243	20.344 144	12.633 57	1.6131 825	20.439 418	12.670 24
17	1.6528 476	21.761 588	13.166 12	1.6589 964	21.966 546	13.240 86	1.6621 252	22.070 840	13.278 69
18	1.7024 331	23.414 435	13.753 52	1.7091 395	23.637 985	13.830 34	1.7125 527	23.751 757	13.869 21
19	1.7535 061	25.116 868	14.323 80	1.7607 983	25.359 943	14.402 53	1.7645 102	25.483 673	14.442 35
20	1.8061 112	26.870 374	14.877 47	1.8140 184	27.133 947	14.957 92	1.8180 440	27.268 133	14.998 61
21	1.8602 946	28.676 486	15.415 02	1.8688 471	28.961 571	15.497 03	1.8732 020	29.106 732	15.538 49
22	1.9161 034	30.536 780	15.936 92	1.9253 330	30.844 434	16.020 31	1.9300 334	31.001 113	16.062 48
23	1.9735 865	32.452 884	16.443 61	1.9835 262	32.784 207	16.528 24	1.9885 891	32.952 969	16.571 03
24	2.0327 941	34.426 470	16.935 51	2.0434 783	34.782 610	17.021 28	2.0489 212	34.964 041	17.064 61
25	2.0937 779	36.459 264	17.413 15	2.1052 424	36.841 414	17.499 85	2.1110 839	37.036 128	17.543 66

Years.	RATIO of INTEREST: ANNUALLY, 0.03.			RATIO of INTEREST: HALF-YEARLY, 0.015.			RATIO of INTEREST: QUARTERLY, 0.0075.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
0	....	....	....	....	....	....	0.9925 558	4.0000 000	4.0300 000
½	....	....	....	0.9852 217	2.0000.000	2.0300 000	0.9851 671	1.9925 745	2.0225 745
¾	....	....	....	....	....	....	0.9778 333	1.3233 831	1.3533 831
1	0.9708 737	1.0000 000	1.0300 000	0.9706 618	0.9925 558	1.0225 558	0.9705 542	0.9888 200	1.0188 200
1¼	....	....	....	....	....	....	0.9633 292	0.7880 896	0.8180 896
1½	....	....	....	0.9563 170	0.6567 659	0.6867 659	0.9561 580	0.6542 756	0.6842 756
1¾	....	....	....	....	....	....	0.9490 402	0.5586 995	0.5886 995
2	0.9425 960	0.4926 108	0.5226 108	0.9421 841	0.4888 895	0.5188 895	0.9419 754	0.4870 221	0.5170 221
2¼	....	....	....	....	....	....	0.9349 632	0.4312 771	0.4612 771
2½	....	....	....	0.9282 603	0.3881 786	0.4181 786	0.9280 031	0.3866 849	0.4166 849
2¾	....	....	....	....	....	....	0.9210 949	0.3502 038	0.3802 038
3	0.9151 417	0.3235 303	0.3535 303	0.9145 421	0.3210 504	0.3510 504	0.9142 381	0.3198 059	0.3498 059
3¼	....	....	....	....	....	....	0.9074 324	0.2940 875	0.3240 875
3½	....	....	....	0.9010 267	0.2731 123	0.3031 123	0.9006 773	0.2720 459	0.3020 459
3¾	....	....	....	....	....	....	0.8939 726	0.2529 456	0.2829 456
4	0.8884 871	0.2390 270	0.2690 270	0.8877 111	0.2371 681	0.2671 681	0.8873 176	0.2362 352	0.2662 352
4¼	....	....	....	....	....	....	0.8807 123	0.2214 928	0.2514 928
4½	....	....	....	0.8745 922	0.2092 196	0.2392 196	0.8741 561	0.2083 907	0.2383 907
4¾	....	....	....	....	....	....	0.8676 487	0.1966 696	0.2266 696
5	0.8626 088	0.1883 546	0.2183 546	0.8616 672	0.1868 683	0.2168 683	0.8611 899	0.1861 225	0.2161 225
5¼	....	....	....	....	....	....	0.8547 790	0.1765 817	0.2065 817
5½	....	....	....	0.8489 332	0.1685 877	0.1985 877	0.8484 159	0.1679 099	0.1979 099
5¾	....	....	....	....	....	....	0.8421 001	0.1599 938	0.1899 938
6	0.8374 843	0.1545 975	0.1845 975	0.8363 874	0.1533 600	0.1833 600	0.8358 313	0.1527 390	0.1827 390
6¼	....	....	....	....	....	....	0.8296 093	0.1460 660	0.1760 660
6½	....	....	....	0.8240 270	0.1404 807	0.1704 807	0.8234 336	0.1399 077	0.1699 077
6¾	....	....	....	....	....	....	0.8173 038	0.1342 071	0.1642 071
7	0.8130 915	0.1305 063	0.1605 063	0.8118 493	0.1294 466	0.1594 466	0.8112 197	0.1289 148	0.1589 148
7¼	....	....	....	....	....	....	0.8051 808	0.1239 889	0.1539 889
7½	....	....	....	0.7998 515	0.1198 886	0.1498 886	0.7991 869	0.1193 926	0.1493 926
7¾	....	....	....	....	....	....	0.7932 376	0.1150 941	0.1450 941
8	0.7894 093	0.1124 564	0.1424 564	0.7880 310	0.1115 302	0.1415 302	0.7873 326	0.1110 653	0.1410 653
8¼	....	....	....	....	....	....	0.7814 715	0.1072 819	0.1372 819
8½	....	....	....	0.7763 853	0.1041 593	0.1341 593	0.7756 542	0.1037 221	0.1337 221
8¾	....	....	....	....	....	....	0.7698 801	0.1003 668	0.1303 668
9	0.7664 167	0.0984 339	0.1284 339	0.7649 116	0.0976 116	0.1276 116	0.7641 490	0.0971 989	0.1271 989
9¼	....	....	....	....	....	....	0.7584 605	0.0942 033	0.1242 033
9½	....	....	....	0.7536 074	0.0917 569	0.1217 569	0.7528 144	0.0913 663	0.1213 663
9¾	....	....	....	....	....	....	0.7472 103	0.0886 758	0.1186 758
10	0.7440 939	0.0872 305	0.1172 305	0.7424 704	0.0864 915	0.1164 915	0.7416 480	0.0861 206	0.1161 206
10¼	....	....	....	....	....	....	0.7361 270	0.0836 911	0.1136 911
10½	....	....	....	0.7314 979	0.0817 310	0.1117 310	0.7306 472	0.0813 781	0.1113 781
10¾	....	....	....	....	....	....	0.7252 081	0.0791 735	0.1091 735
11	0.7224 213	0.0780 774	0.1080 774	0.7206 876	0.0774 066	0.1074 066	0.7198 095	0.0770 700	0.1070 700
11¼	....	....	....	....	....	....	0.7144 511	0.0750 608	0.1050 608
11½	....	....	....	0.7100 371	0.0734 615	0.1034 615	0.7091 326	0.0731 398	0.1031 398
11¾	....	....	....	....	....	....	0.7038 537	0.0713 013	0.1013 013
12	0.7013 798	0.0704 621	0.1004 621	0.6995 439	0.0698 482	0.0998 482	0.6986 141	0.0695 402	0.0995 402
12¼	....	....	....	....	....	....	0.6934 135	0.0678 517	0.0978 517
12½	....	....	....	0.6892 058	0.0665 269	0.0965 269	0.6882 516	0.0662 315	0.0962 315
12¾	....	....	....	....	....	....	0.6831 282	0.0646 755	0.0946 755
13	0.6809 513	0.0640 295	0.0940 295	0.6790 205	0.0634 639	0.0934 639	0.6780 429	0.0631 801	0.0931 801
13¼	....	....	....	....	....	....	0.6729 954	0.0617 418	0.0917 418
13½	....	....	....	0.6689 857	0.0606 305	0.0906 305	0.6679 855	0.0603 575	0.0903 575
13¾	....	....	....	....	....	....	0.6630 129	0.0590 242	0.0890 242
14	0.6611 178	0.0585 263	0.0885 263	0.6590 993	0.0580 022	0.0880 022	0.6580 773	0.0577 391	0.0877 391
14¼	....	....	....	....	....	....	0.6531 785	0.0564 998	0.0864 998
14½	....	....	....	0.6493 589	0.0555 576	0.0855 576	0.6483 161	0.0553 039	0.0853 039
14¾	....	....	....	....	....	....	0.6434 899	0.0541 491	0.0841 491
15	0.6418 620	0.0537 666	0.0837 666	0.6397 624	0.0532 784	0.0832 784	0.6386 997	0.0530 334	0.0830 334
15¼	....	....	....	....	....	....	0.6339 451	0.0519 549	0.0819 549
15½	....	....	....	0.6303 078	0.0511 486	0.0811 486	0.6292 259	0.0509 118	0.0809 118
15¾	....	....	....	....	....	....	0.6245 418	0.0499 024	0.0799 024
16	0.6231 669	0.0496 108	0.0796 108	0.6209 929	0.0491 542	0.0791 542	0.6198 927	0.0489 251	0.0789 251
17	0.6050 164	0.0459 525	0.0759 525	0.6027 741	0.0455 238	0.0755 238	0.6016 394	0.0453 087	0.0753 087
18	0.5873 946	0.0427 087	0.0727 087	0.5850 897	0.0423 048	0.0723 048	0.5839 236	0.0421 021	0.0721 021
19	0.5702 860	0.0398 139	0.0698 139	0.5679 242	0.0394 323	0.0694 323	0.5667 295	0.0392 408	0.0692 408
20	0.5536 758	0.0372 157	0.0672 157	0.5512 623	0.0368 542	0.0668 542	0.5500 417	0.0366 728	0.0666 728
21	0.5375 493	0.0348 718	0.0648 718	0.5350 893	0.0345 285	0.0645 285	0.5338 452	0.0343 563	0.0643 563
22	0.5218 925	0.0327 474	0.0627 474	0.5193 907	0.0324 208	0.0624 208	0.5181 257	0.0322 569	0.0622 569
23	0.5066 918	0.0308 139	0.0608 139	0.5041 527	0.0305 025	0.0605 025	0.5028 691	0.0303 463	0.0603 463
24	0.4919 338	0.0290 474	0.0590 474	0.4893 617	0.0287 500	0.0587 500	0.4880 617	0.0286 008	0.0586 008
25	0.4776 056	0.0274 279	0.0574 279	0.4750 047	0.0271 434	0.0571 434	0.4736 903	0.0270 007	0.0570 007

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.03.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.015.			RATIO *of* INTEREST: *QUARTERLY*, 0.0075.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	2.1565 913	38.553 042	17.876 84	2.1688 734	38.962 446	17.964 37	2.1751 324	39.171 081	18.008 60
27	2.2212 890	40.709 633	18.327 03	2.2344 275	41.147 586	18.415 27	2.2411 242	41.370 806	18.459 85
28	2.2879 277	42.930 922	18.764 11	2.3019 631	43.398 771	18.852 94	2.3091 181	43.637 269	18.897 81
29	2.3565 655	45.218 850	19.188 45	2.3715 400	45.717 999	19.277 77	2.3791 749	45.972 495	19.322 87
30	2.4272 625	47.575 415	19.600 44	2.4432 198	48.107 326	19.690 13	2.4513 571	48.378 570	19.735 42
31	2.5000 803	50.002 678	20.000 43	2.5170 661	50.568 870	20.090 40	2.5257 293	50.857 643	20.135 82
32	2.5750 827	52.502 758	20.388 76	2.5931 444	53.104 314	20.478 93	2.6023 579	53.411 929	20.524 44
33	2.6523 352	55.077 841	20.765 79	2.6715 222	55.717 407	20.856 05	2.6813 113	56.043 710	20.901 61
34	2.7319 053	57.730 176	21.131 84	2.7522 690	58.408 956	21.222 12	2.7626 601	58.755 337	21.267 67
35	2.8138 624	60.462 081	21.487 22	2.8354 563	61.181 876	21.577 44	2.8464 770	61.549 233	21.622 95
36	2.8982 783	63.275 944	21.832 25	2.9211 580	64.038 599	21.922 33	2.9328 368	64.427 803	21.967 77
37	2.9852 267	66.174 222	22.167 24	3.0094 500	66.981 665	22.257 11	3.0218 167	67.393 889	22.302 44
38	3.0747 835	69.159 449	22.492 46	3.1004 106	70.013 686	22.582 07	3.1134 962	70.449 872	22.627 26
39	3.1670 270	72.234 232	22.808 22	3.1941 205	73.137 350	22.897 49	3.2079 571	73.598 570	22.942 51
40	3.2620 378	75.401 259	23.114 77	3.2906 628	76.355 426	23.203 66	3.3052 839	76.842 798	23.248 47
41	3.3598 989	78.663 297	23.412 40	3.3901 231	79.670 769	23.500 85	3.4055 636	80.185 452	23.545 43
42	3.4606 959	82.023 196	23.701 36	3.4925 895	83.086 318	23.789 32	3.5088 856	83.629 520	23.833 64
43	3.5645 168	85.483 892	23.981 90	3.5981 531	86.605 102	24.069 32	3.6153 424	87.178 079	24.113 37
44	3.6714 523	89.048 408	24.254 27	3.7069 072	90.230 241	24.341 11	3.7250 289	90.834 297	24.384 86
45	3.7815 958	92.719 861	24.518 71	3.8189 485	93.964 950	24.604 93	3.8380 433	94.601 443	24.648 35
46	3.8950 437	96.501 457	24.775 45	3.9343 762	97.812 541	24.861 00	3.9544 864	98.482 880	24.904 09
47	4.0118 950	100.39 650	25.024 71	4.0532 927	101.77 642	25.109 57	4.0744 623	102.48 208	25.152 30
48	4.1322 519	104.40 840	25.266 71	4.1758 034	105.86 011	25.350 84	4.1980 782	106.60 261	25.393 19
49	4.2562 194	108.54 065	25.501 66	4.3020 171	110.06 724	25.585 03	4.3254 445	110.84 815	25.627 00
50	4.3839 060	112.79 687	25.729 76	4.4320 456	114.40 152	25.812 35	4.4566 750	115.22 250	25.853 92
51	4.5154 232	117.18 077	25.951 22	4.5660 041	118.86 680	26.033 00	4.5918 869	119.72 956	26.074 15
52	4.6508 859	121.69 620	26.166 24	4.7040 116	123.46 705	26.247 18	4.7312 010	124.37 337	26.287 91
53	4.7904 124	126.34 708	26.374 99	4.8461 904	128.20 635	26.455 08	4.8747 419	129.15 806	26.495 36
54	4.9341 248	131.13 749	26.577 66	4.9926 665	133.08 888	26.656 87	5.0226 376	134.08 792	26.696 72
55	5.0821 486	136.07 162	26.774 43	5.1435 698	138.11 899	26.852 75	5.1750 203	139.16 734	26.892 14
56	5.2346 130	141.15 377	26.965 46	5.2990 342	143.30 114	27.042 88	5.3320 263	144.40 876	27.081 80
57	5.3916 514	146.38 838	27.150 94	5.4591 975	148.63 992	27.227 43	5.4937 956	149.79 319	27.265 88
58	5.5534 010	151.78 003	27.331 01	5.6242 018	154.14 006	27.406 57	5.6604 729	155.34 910	27.444 54
59	5.7200 030	157.33 343	27.505 83	5.7941 933	159.80 644	27.580 44	5.8322 071	161.07 357	27.617 94
60	5.8916 031	163.05 344	27.675 56	5.9693 228	165.64 409	27.749 23	6.0091 516	166.97 172	27.786 24
61	6.0683 512	168.94 504	27.840 36	6.1497 455	171.65 818	27.913 05	6.1914 643	173.04 881	27.949 58
62	6.2504 017	175.01 339	28.000 34	6.3356 216	177.85 405	28.072 07	6.3793 084	179.31 028	28.108 11
63	6.4379 138	181.26 379	28.155 67	6.5271 158	184.23 719	28.226 43	6.5728 514	185.76 171	28.261 97
64	6.6310 512	187.70 171	28.306 48	6.7243 978	190.81 326	28.376 26	6.7722 664	192.40 838	28.411 30
65	6.8299 827	194.33 276	28.452 89	6.9276 428	197.58 809	28.521 69	6.9777 315	199.25 772	28.556 23
66	7.0348 822	201.16 274	28.595 04	7.1370 308	204.56 769	28.662 86	7.1894 302	206.31 434	28.696 90
67	7.2459 286	208.19 762	28.733 05	7.3527 475	211.75 825	28.799 88	7.4075 517	213.58 506	28.833 42
68	7.4633 065	215.44 355	28.867 04	7.5749 843	219.16 614	28.932 88	7.6322 908	221.07 636	28.965 93
69	7.6872 057	222.90 626	28.997 12	7.8039 382	226.79 794	29.061 99	7.8638 484	228.79 495	29.094 52
70	7.9178 219	230.59 406	29.123 42	8.0398 122	234.66 041	29.187 30	8.1024 312	236.74 771	29.219 34
71	8.1553 565	238.51 188	29.246 04	8.2828 156	242.76 052	29.308 94	8.3482 524	244.94 175	29.340 48
72	8.4000 172	246.66 724	29.365 09	8.5331 637	251.10 546	29.427 01	8.6015 316	253.38 439	29.458 05
73	8.6520 177	255.06 726	29.480 67	8.7910 785	259.70 262	29.541 61	8.8624 951	262.08 317	29.572 17
74	8.9115 783	263.71 928	29.592 88	9.0567 889	268.55 963	29.652 85	9.1313 760	271.04 537	29.682 93
75	9.1789 256	272.63 085	29.701 83	9.3305 303	277.68 434	29.760 83	9.4084 146	280.28 049	29.790 41
76	9.4542 934	281.80 978	29.807 60	9.6125 456	287.08 485	29.865 64	9.6938 583	289.79 528	29.894 73
77	9.7379 222	291.26 407	29.910 29	9.9030 848	296.76 949	29.967 38	9.9879 621	299.59 874	29.995 98
78	10.030 060	301.00 200	30.009 99	10.202 406	306.74 685	30.066 13	10.290 989	309.69 963	30.094 26
79	10.330 962	311.03 206	30.106 79	10.510 773	317.02 578	30.161 98	10.603 209	320.10 697	30.189 63
80	10.640 891	321.36 302	30.200 77	10.828 461	327.61 538	30.255 02	10.924 902	330.83 006	30.282 20
81	10.960 117	332.00 391	30.292 01	11.155 752	338.52 505	30.345 34	11.256 354	341.87 848	30.372 04
82	11.288 921	342.96 402	30.380 58	11.492 934	349.76 447	30.433 00	11.597 863	353.26 211	30.459 24
83	11.627 588	354.25 295	30.466 59	11.840 308	361.34 361	30.518 09	11.949 733	364.99 110	30.543 87
84	11.976 416	365.88 053	30.550 09	12.198 181	373.27 272	30.600 69	12.312 278	377.07 594	30.626 00
85	12.335 708	377.85 695	30.631 15	12.566 871	385.56 238	30.680 85	12.685 823	389.52 742	30.705 73
86	12.705 780	390.19 266	30.709 85	12.946 705	398.22 351	30.758 68	13.070 700	402.35 668	30.783 10
87	13.086 953	402.89 844	30.786 27	13.338 019	411.26 731	30.834 21	13.467 255	415.57 516	30.858 20
88	13.479 562	415.98 539	30.860 46	13.741 161	424.70 537	30.907 53	13.875 840	429.19 468	30.931 08
89	13.883 949	429.46 495	30.932 48	14.156 488	438.54 959	30.978 70	14.296 822	443.22 741	31.001 81
90	14.300 467	443.34 890	31.002 41	14.584 367	452.81 225	31.047 78	14.730 576	457.68 587	31.070 47
91	14.729 481	457.64 937	31.070 30	15.025 180	467.50 600	31.114 84	15.177 490	472 58 300	31.137 10
92	15.171 365	472.37 885	31.136 21	15.479 316	482.64 387	31.179 92	15.637 963	487.93 209	31.201 77
93	15.626 506	487.55 021	31.200 21	15.947 178	498.23 928	31.243 10	16.112 406	503.74 686	31.264 53
94	16.095 302	503.17 672	31.262 33	16.429 182	514.30 606	31.304 42	16.601 243	520.04 144	31.325 45
95	16.578 161	519.27 202	31.322 65	16.925 754	530.85 846	31.363 95	17.104 912	536.83 039	31.384 58
96	17.075 506	535.85 018	31.381 22	17.437 335	547.91 116	31.421 73	17.623 861	554.12 869	31.441 96
97	17.587 771	552.92 569	31.438 08	17.964 378	565.47 927	31.477 81	18.158 554	571.95 185	31.497 65
98	18.115 404	570.51 346	31.493 28	18.507 351	583.57 838	31.532 25	18.709 470	590.31 567	31.551 70
99	18.658 866	588.62 886	31.546 87	19.066 736	600.22 245	31.585 09	19.277 100	609.23 668	31.604 16
100	19.218 632	607.28 773	31.598 91	19.643 028	621.43 428	31.636 38	19.861 952	628.73 173	31.655 08
	Value of Perpetual Ann.		33.333 33	- - - - - - - - -		33.333 33	- - - - - - - - -		33.333 33

Years.	RATIO of INTEREST: ANNUALLY, 0.03.			RATIO of INTEREST: HALF-YEARLY, 0.015.			RATIO of INTEREST: QUARTERLY, 0.0075.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.4636 947	0.0259 383	0.0559 383	0.4610 689	0.0256 657	0.0556 657	0.4597 421	0.0255 290	0.0555 290
27	0.4501 891	0.0245 642	0.0545 642	0.4475 419	0.0243 028	0.0543 028	0.4462 042	0.0241 716	0.0541 716
28	0.4370 768	0.0232 932	0.0532 932	0.4344 118	0.0230 421	0.0530 421	0.4330 658	0.0229 162	0.0529 162
29	0.4243 464	0.0221 147	0.0521 147	0.4216 669	0.0218 732	0.0518 732	0.4203 138	0.0217 521	0.0517 521
30	0.4119 868	0.0210 193	0.0510 193	0.4092 960	0.0207 869	0.0507 869	0.4079 373	0.0206 703	0.0506 703
31	0.3999 871	0.0199 989	0.0499 989	0.3972 879	0.0197 750	0.0497 750	0.3959 253	0.0196 627	0.0496 627
32	0.3883 370	0.0190 466	0.0490 466	0.3856 322	0.0188 307	0.0488 307	0.3842 669	0.0187 224	0.0487 224
33	0.3770 262	0.0181 561	0.0481 561	0.3743 185	0.0179 477	0.0479 477	0.3729 518	0.0178 432	0.0478 432
34	0.3660 449	0.0173 219	0.0473 219	0.3633 366	0.0171 207	0.0471 207	0.3619 700	0.0170 197	0.0470 197
35	0.3553 834	0.0165 393	0.0465 393	0.3526 769	0.0163 447	0.0463 447	0.3513 115	0.0162 472	0.0462 472
36	0.3450 324	0.0158 038	0.0458 038	0.3423 300	0.0156 156	0.0456 156	0.3409 668	0.0155 212	0.0455 212
37	0.3349 829	0.0151 116	0.0451 116	0.3322 866	0.0149 295	0.0449 295	0.3309 268	0.0148 381	0.0448 381
38	0.3252 262	0.0144 593	0.0444 593	0.3225 380	0.0142 829	0.0442 829	0.3211 824	0.0141 945	0.0441 945
39	0.3157 535	0.0138 438	0.0438 438	0.3130 752	0.0136 729	0.0436 729	0.3117 248	0.0135 872	0.0435 872
40	0.3065 568	0.0132 624	0.0432 624	0.3038 902	0.0130 966	0.0430 966	0.3025 459	0.0130 136	0.0430 136
41	0.2976 280	0.0127 124	0.0427 124	0.2949 746	0.0125 517	0.0425 517	0.2936 372	0.0124 711	0.0424 711
42	0.2889 592	0.0121 917	0.0421 917	0.2863 205	0.0120 357	0.0420 357	0.2849 908	0.0119 575	0.0419 575
43	0.2805 429	0.0116 981	0.0416 981	0.2779 204	0.0115 467	0.0415 467	0.2765 990	0.0114 708	0.0414 708
44	0.2723 718	0.0112 298	0.0412 298	0.2697 666	0.0110 828	0.0410 828	0.2684 543	0.0110 091	0.0410 091
45	0.2644 386	0.0107 852	0.0407 852	0.2618 522	0.0106 423	0.0406 423	0.2605 494	0.0105 706	0.0405 706
46	0.2567 365	0.0103 625	0.0403 625	0.2541 699	0.0102 236	0.0402 236	0.2528 773	0.0101 540	0.0401 540
47	0.2492 588	0.0099 605	0.0399 605	0.2467 130	0.0098 255	0.0398 255	0.2454 312	0.0097 578	0.0397 578
48	0.2419 988	0.0095 778	0.0395 778	0.2394 748	0.0094 464	0.0394 464	0.2382 042	0.0093 806	0.0393 806
49	0.2349 503	0.0092 131	0.0392 131	0.2324 491	0.0090 854	0.0390 854	0.2311 901	0.0090 213	0.0390 213
50	0.2281 071	0.0088 655	0.0388 655	0.2256 295	0.0087 411	0.0387 411	0.2243 825	0.0086 789	0.0386 789
51	0.2214 632	0.0085 338	0.0385 338	0.2190 099	0.0084 128	0.0384 128	0.2177 754	0.0083 522	0.0383 522
52	0.2150 128	0.0082 172	0.0382 172	0.2125 845	0.0080 993	0.0380 993	0.2113 628	0.0080 403	0.0380 403
53	0.2087 503	0.0079 147	0.0379 147	0.2063 476	0.0077 999	0.0377 999	0.2051 391	0.0077 425	0.0377 425
54	0.2026 702	0.0076 256	0.0376 256	0.2002 938	0.0075 138	0.0375 138	0.1990 986	0.0074 578	0.0374 578
55	0.1967 672	0.0073 491	0.0373 491	0.1944 175	0.0072 401	0.0372 401	0.1932 360	0.0071 856	0.0371 856
56	0.1910 361	0.0070 845	0.0370 845	0.1887 136	0.0069 783	0.0369 783	0.1875 459	0.0069 252	0.0369 252
57	0.1854 719	0.0068 311	0.0368 311	0.1831 771	0.0067 277	0.0367 277	0.1820 235	0.0066 759	0.0366 759
58	0.1800 698	0.0065 885	0.0365 885	0.1778 030	0.0064 876	0.0364 876	0.1766 637	0.0064 371	0.0364 371
59	0.1748 251	0.0063 559	0.0363 559	0.1725 866	0.0062 576	0.0362 576	0.1714 617	0.0062 083	0.0362 083
60	0.1697 331	0.0061 330	0.0361 330	0.1675 232	0.0060 370	0.0360 370	0.1664 129	0.0059 890	0.0359 890
61	0.1647 894	0.0059 191	0.0359 191	0.1626 084	0.0058 255	0.0358 255	0.1615 127	0.0057 787	0.0357 787
62	0.1599 897	0.0057 138	0.0357 138	0.1578 377	0.0056 226	0.0356 226	0.1567 568	0.0055 769	0.0355 769
63	0.1553 298	0.0055 168	0.0355 168	0.1532 070	0.0054 278	0.0354 278	0.1521 410	0.0053 832	0.0353 832
64	0.1508 057	0.0053 276	0.0353 276	0.1487 122	0.0052 407	0.0352 407	0.1476 610	0.0051 973	0.0351 973
65	0.1464 132	0.0051 458	0.0351 458	0.1443 492	0.0050 610	0.0350 610	0.1433 130	0.0050 186	0.0350 186
66	0.1421 488	0.0049 711	0.0349 711	0.1401 143	0.0048 884	0.0348 884	0.1390 931	0.0048 470	0.0348 470
67	0.1380 085	0.0048 031	0.0348 031	0.1360 036	0.0047 224	0.0347 224	0.1349 974	0.0046 820	0.0346 820
68	0.1339 889	0.0046 416	0.0346 416	0.1320 135	0.0045 627	0.0345 627	0.1310 223	0.0045 233	0.0345 233
69	0.1300 863	0.0044 862	0.0344 862	0.1281 404	0.0044 092	0.0344 092	0.1271 642	0.0043 707	0.0343 707
70	0.1262 973	0.0043 366	0.0343 366	0.1243 810	0.0042 615	0.0342 615	0.1234 198	0.0042 239	0.0342 239
71	0.1226 188	0.0041 927	0.0341 927	0.1207 319	0.0041 193	0.0341 193	0.1197 856	0.0040 826	0.0340 826
72	0.1190 474	0.0040 540	0.0340 540	0.1171 898	0.0039 824	0.0339 824	0.1162 584	0.0039 466	0.0339 466
73	0.1155 800	0.0039 205	0.0339 205	0.1137 517	0.0038 506	0.0338 506	0.1128 350	0.0038 156	0.0338 156
74	0.1122 135	0.0037 919	0.0337 919	0.1104 144	0.0037 236	0.0337 236	0.1095 125	0.0036 894	0.0336 894
75	0.1089 452	0.0036 680	0.0336 680	0.1071 750	0.0036 012	0.0336 012	0.1062 878	0.0035 679	0.0335 679
76	0.1057 720	0.0035 485	0.0335 485	0.1040 307	0.0034 833	0.0334 833	0.1031 581	0.0034 507	0.0334 507
77	0.1026 913	0.0034 333	0.0334 333	0.1009 786	0.0033 696	0.0333 696	0.1001 205	0.0033 378	0.0333 378
78	0.0997 003	0.0033 222	0.0333 222	0.0980 161	0.0032 600	0.0332 600	0.0971 724	0.0032 289	0.0332 289
79	0.0967 964	0.0032 151	0.0332 151	0.0951 405	0.0031 543	0.0331 543	0.0943 111	0.0031 240	0.0331 240
80	0.0939 771	0.0031 117	0.0331 117	0.0923 492	0.0030 524	0.0330 524	0.0915 340	0.0030 227	0.0330 227
81	0.0912 399	0.0030 120	0.0330 120	0.0896 399	0.0029 540	0.0329 540	0.0888 387	0.0029 250	0.0329 250
82	0.0885 824	0.0029 158	0.0329 158	0.0870 100	0.0028 591	0.0328 591	0.0862 228	0.0028 308	0.0328 308
83	0.0860 024	0.0028 228	0.0328 228	0.0844 573	0.0027 674	0.0327 674	0.0836 839	0.0027 398	0.0327 398
84	0.0834 974	0.0027 331	0.0327 331	0.0819 794	0.0026 790	0.0326 790	0.0812 197	0.0026 520	0.0326 520
85	0.0810 655	0.0026 465	0.0326 465	0.0795 743	0.0025 936	0.0325 936	0.0788 282	0.0025 672	0.0325 672
86	0.0787 043	0.0025 628	0.0325 628	0.0772 397	0.0025 112	0.0325 112	0.0765 070	0.0024 854	0.0324 854
87	0.0764 120	0.0024 820	0.0324 820	0.0749 736	0.0024 315	0.0324 315	0.0742 542	0.0024 063	0.0324 063
88	0.0741 864	0.0024 039	0.0324 039	0.0727 741	0.0023 546	0.0323 546	0.0720 677	0.0023 299	0.0323 299
89	0.0720 256	0.0023 285	0.0323 285	0.0706 390	0.0022 802	0.0322 802	0.0699 456	0.0022 562	0.0322 562
90	0.0699 278	0.0022 556	0.0322 556	0.0685 666	0.0022 084	0.0322 084	0.0678 860	0.0021 849	0.0321 849
91	0.0678 911	0.0021 851	0.0321 851	0.0665 549	0.0021 390	0.0321 390	0.0658 870	0.0021 160	0.0321 160
92	0.0659 136	0.0021 169	0.0321 169	0.0646 023	0.0020 719	0.0320 719	0.0639 469	0.0020 495	0.0320 495
93	0.0639 938	0.0020 511	0.0320 511	0.0627 070	0.0020 071	0.0320 071	0.0620 640	0.0019 851	0.0319 851
94	0.0621 299	0.0019 874	0.0319 874	0.0608 673	0.0019 444	0.0319 444	0.0602 365	0.0019 229	0.0319 229
95	0.0603 203	0.0019 258	0.0319 258	0.0590 816	0.0018 837	0.0318 837	0.0584 627	0.0018 628	0.0318 628
96	0.0585 634	0.0018 662	0.0318 662	0.0573 482	0.0018 251	0.0318 251	0.0567 413	0.0018 046	0.0318 046
97	0.0568 577	0.0018 086	0.0318 086	0.0556 657	0.0017 684	0.0317 684	0.0550 705	0.0017 484	0.0317 484
98	0.0552 016	0.0017 528	0.0317 528	0.0540 326	0.0017 136	0.0317 136	0.0534 489	0.0016 940	0.0316 940
99	0.0535 938	0.0016 989	0.0316 989	0.0524 474	0.0016 605	0.0316 605	0.0518 750	0.0016 414	0.0316 414
100	0.0520 328	0.0016 467	0.0316 467	0.0509 086	0.0016 092	0.0316 092	0.0503 475	0.0015 905	0.0315 905
	Ratio of Perpetual Ann.		0.0300 000	- - - - - - - - -		0.0300 000	- - - - - - - - -		0.0300 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0325.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.01625.			RATIO *of* INTEREST: *QUARTERLY*, 0.008125.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
$0\frac{1}{4}$	....	....	....	....	....	....	1.0081 250	0.2500 000	0.2479 85
$0\frac{2}{4}$	....	....	....	1.0162 500	0.5000 000	0.4920 05	1.0163 160	0.5020 313	0.4939 72
$0\frac{3}{4}$	....	....	....	....	....	....	1.0245 736	0.7561 103	0.7379 76
1	1.0325 000	1.0000 000	0.9685 23	1.0327 641	1.0081 250	0.9761 43	1.0328 982	1.0122 536	0.9800 13
$1\frac{1}{4}$	....	....	....	....	....	....	1.0412 905	1.2704 782	1.2201 00
$1\frac{2}{4}$	....	....	....	1.0495 465	1.5245 070	1.4525 39	1.0497 510	1.5308 008	1.4582 51
$1\frac{3}{4}$	....	....	....	....	....	....	1.0582 803	1.7932 386	1.6944 84
2	1.0660 563	2.0325 000	1.9065 60	1.0666 016	2.0492 803	1.9213 18	1.0668 788	2.0578 087	1.9288 12
$2\frac{1}{4}$	....	....	....	....	....	....	1.0755 472	2.3245 284	2.1612 52
$2\frac{2}{4}$	....	....	....	1.0839 339	2.5825 811	2.3826 00	1.0842 860	2.5934 152	2.3918 18
$2\frac{3}{4}$	....	....	....	....	....	....	1.0930 958	2.8644 867	2.6205 27
3	1.1007 031	3.0985 563	2.8150 70	1.1015 478	3.1245 480	2.8365 07	1.1019 772	3.1377 606	2.8473 92
$3\frac{1}{4}$	....	....	....	....	....	....	1.1109 308	3.4132 549	3.0724 28
$3\frac{2}{4}$	....	....	....	1.1194 480	3.6753 219	3.2831 56	1.1199 571	3.6909 876	3.2956 51
$3\frac{3}{4}$	....	....	....	....	....	....	1.1290 567	3.9709 769	3.5170 75
4	1.1364 759	4.1992 593	3.6949 83	1.1376 390	4.2350 459	3.7226 63	1.1382 303	4.2532 411	3.7367 14
$4\frac{1}{4}$	....	....	....	....	....	....	1.1474 785	4.5377 987	3.9545 83
$4\frac{2}{4}$	....	....	....	1.1561 256	4.8038 654	4.1551 42	1.1568 017	4.8246 083	4.1706 96
$4\frac{3}{4}$	....	....	....	....	....	....	1.1662 007	5.1138 687	4.3850 67
5	1.1734 114	5.3357 353	4.5471 99	1.1749 127	5.3819 282	4.5807 05	1.1756 762	5.4054 189	4.5977 11
$5\frac{1}{4}$	....	....	....	....	....	....	1.1852 285	5.6993 379	4.8086 41
$5\frac{2}{4}$	....	....	....	1.1940 050	5.9693 845	4.9994 66	1.1948 535	5.9956 450	5.0178 71
$5\frac{3}{4}$	....	....	....	....	....	....	1.2045 667	6.2943 596	5.2254 14
6	1.2115 473	6.5091 467	5.3725 90	1.2134 076	6.5663 869	5.4115 29	1.2143 538	6.5955 013	5.4312 85
$6\frac{1}{4}$	....	....	....	....	....	....	1.2242 204	6.8990 898	5.6354 96
$6\frac{2}{4}$	....	....	....	1.2331 254	7.1730 907	5.8170 03	1.2341 672	7.2051 449	5.8380 62
$6\frac{3}{4}$	....	....	....	....	....	....	1.2441 948	7.5136 867	6.0389 95
7	1.2509 226	7.7206 939	6.1720 00	1.2531 637	7.7896 534	6.2159 93	1.2543 039	7.8247 354	6.2383 09
$7\frac{1}{4}$	....	....	....	....	....	....	1.2644 051	8.1383 114	6.4360 16
$7\frac{2}{4}$	....	....	....	1.2735 276	8.4162 353	6.6086 04	1.2747 691	8.4544 351	6.6321 30
$7\frac{3}{4}$	....	....	....	....	....	....	1.2851 266	8.7731 274	6.8266 64
8	1.2915 775	8.9716 165	6.9462 47	1.2942 225	9.0529 991	6.9949 36	1.2955 683	9.0944 091	7.0196 29
$8\frac{1}{4}$	....	....	....	....	....	....	1.3060 943	9.4183 012	7.2110 39
$8\frac{2}{4}$	....	....	....	1.3152 536	9.7001 103	7.3750 91	1.3167 068	9.7448 248	7.4009 07
$8\frac{3}{4}$	....	....	....	....	....	....	1.3274 051	10.074 002	7.5892 45
9	1.3335 538	10.263 194	7.6961 23	1.3366 265	10.357 737	7.7491 67	1.3381 902	10.405 853	7.7760 64
$9\frac{1}{4}$	....	....	....	....	....	....	1.3490 630	10.740 400	7.9613 78
$9\frac{2}{4}$	....	....	....	1.3583 466	11.026 050	8.1172 61	1.3600 241	11.077 666	8.1451 98
$9\frac{3}{4}$	....	....	....	....	....	....	1.3710 743	11.417 672	8.3275 37
10	1.3768 943	11.596 748	8.4223 95	1.3804 198	11.705 224	8.4794 70	1.3822 143	11.760 441	8.5084 06
$10\frac{1}{4}$	....	....	....	....	....	....	1.3934 448	12.105 994	8.6878 18
$10\frac{2}{4}$	....	....	....	1.4028 516	12.395 434	8.8358 87	1.4047 666	12.454 356	8.8657 83
$10\frac{3}{4}$	....	....	....	....	....	....	1.4161 803	12.805 547	9.0423 14
11	1.4216 434	12.973 642	9.1258 07	1.4256 479	13.096 859	9.1866 05	1.4276 867	13.159 592	9.2174 23
$11\frac{1}{4}$	....	....	....	....	....	....	1.4392 867	13.516 514	9.3911 20
$11\frac{2}{4}$	....	....	....	1.4488 147	13.809 683	9.5317 14	1.4509 809	13.876 336	9.5034 17
$11\frac{3}{4}$	....	....	....	....	....	....	1.4627 701	14.239 081	9.7343 26
12	1.4678 468	14.395 285	9.8070 77	1.4723 579	14.534 091	9.8713 06	1.4746 551	14.604 773	9.9038 57
$12\frac{1}{4}$	....	....	....	....	....	....	1.4866 367	14.973 437	10.072 02
$12\frac{2}{4}$	....	....	....	1.4962 838	15.270 270	10.205 47	1.4987 156	15.345 096	10.238 83
$12\frac{3}{4}$	....	....	....	....	....	....	1.5108 927	15.719 775	10.404 30
13	1.5155 518	15.863 132	10.466 90	1.5205 984	16.018 412	10.534 28	1.5231 687	16.097 498	10.568 43
$13\frac{1}{4}$	....	....	....	....	....	....	1.5355 444	16.478 291	10.731 24
$13\frac{2}{4}$	....	....	....	1.5453 081	16.778 711	10.857 84	1.5480 207	16.862 177	10.892 73
$13\frac{3}{4}$	....	....	....	....	....	....	1.5605 984	17.249 182	11.052 93
14	1.5648 072	17.378 684	11.105 96	1.5704 194	17.551 365	11.176 23	1.5732 783	17.639 331	11.211 83
$14\frac{1}{4}$	....	....	....	....	....	....	1.5860 612	18.032 651	11.369 46
$14\frac{2}{4}$	....	....	....	1.5959 387	18.336 575	11.489 53	1.5989 479	18.429 166	11.525 81
$14\frac{3}{4}$	....	....	....	....	....	....	1.6119 394	18.828 903	11.680 90
15	1.6156 635	18.943 491	11.724 90	1.6218 727	19.134 544	11.797 81	1.6250 364	19.231 883	11.834 74
$15\frac{1}{4}$	....	....	....	....	....	....	1.6382 398	19.638 147	11.987 35
$15\frac{2}{4}$	....	....	....	1.6482 281	19.945 480	12.101 17	1.6515 505	20.047 707	12.138 72
$15\frac{3}{4}$	....	....	....	....	....	....	1.6649 693	20.460 595	12.288 87
16	1.6681 725	20.559 155	12.324 36	1.6750 118	20.769 594	12.399 67	1.6784 972	20.876 837	12.437 81
17	1.7223 881	22.227 327	12.904 95	1.7298 920	22.458 215	12.982 44	1.7337 168	22.575 901	13.021 68
18	1.7783 658	23.949 715	13.467 26	1.7865 703	24.202 163	13.546 72	1.7907 530	24.330 862	13.586 94
19	1.8361 626	25.728 081	14.011 88	1.8451 056	26.003 249	14.093 09	1.8496 657	26.143 560	14.134 21
20	1.8958 379	27.564 244	14.539 35	1.9055 587	27.863 346	14.622 14	1.9105 164	28.015 890	14.664 04
21	1.9574 527	29.460 082	15.050 21	1.9679 926	29.784 387	15.134 40	1.9733 691	29.949 818	15.177 00
22	2.0210 699	31.417 534	15.545 00	2.0324 720	31.768 370	15.630 41	2.0382 895	31.947 368	15.673 62
23	2.0867 546	33.438 604	16.024 22	2.0990 641	33.817 355	16.110 68	2.1053 456	34.010 634	16.154 42
24	2.1545 742	35.525 359	16.488 34	2.1678 379	35.933 474	16.575 72	2.1746 078	36.141 778	16.619 91
25	2.2245 978	37.679 933	16.937 86	2.2388 651	38.118 926	17.026 00	2.2461 485	38.343 032	17.070 57

Years.	RATIO of INTEREST: ANNUALLY, 0.0325.			RATIO of INTEREST: HALF-YEARLY, 0.01625.			RATIO of INTEREST: QUARTERLY, 0.008125.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
0¼	....	....	....	....	....	....	0.9919 405	4.0000 000	4.0325 000
½	....	....	....	0.9840 102	2.0000.000	2.0325 000	0.9839 459	1.9919 078	2.0244 078
¾	....	....	....	....	....	....	0.9760 158	1.3225 585	1.3550 585
1	0.9685 230	1.0000 000	1.0325 000	0.9682 753	0.9919 405	1.0244 405	0.9681 496	0.9878 947	1.0203 947
1¼	....	....	....	....	....	....	0.9603 468	0.7871 053	0.8196 053
1½	....	....	....	0.9527 925	0.6559 497	0.6884 497	0.9526 069	0.6532 528	0.6857 528
1¾	....	....	....	....	....	....	0.9449 294	0.5576 503	0.5901 503
2	0.9380 368	0.4920 049	0.5245 049	0.9375 572	0.4879 762	0.5204 762	0.9373 136	0.4859 538	0.5184 538
2¼	....	....	....	....	....	....	0.9297 593	0.4301 948	0.4626 948
2½	....	....	....	0.9225 656	0.3872 095	0.4197 095	0.9222 659	0.3855 919	0.4180 919
2¾	....	....	....	....	....	....	0.9148 329	0.3491 027	0.3816 027
3	0.9085 102	0.3227 310	0.3552 310	0.9078 135	0.3200 463	0.3525 463	0.9074 598	0.3186 986	0.3511 986
3¼	....	....	....	....	....	....	0.9001 461	0.2929 755	0.3254 755
3½	....	....	....	0.8932 975	0.2720 850	0.3045 850	0.8928 913	0.2709 302	0.3034 302
3¾	....	....	....	....	....	....	0.8856 951	0.2518 272	0.2843 272
4	0.8799 130	0.2381 373	0.2706 373	0.8790 134	0.2361 250	0.2686 250	0.8785 568	0.2351 148	0.2676 148
4¼	....	....	....	....	....	....	0.8714 760	0.2203 712	0.2528 712
4½	....	....	....	0.8649 579	0.2081 657	0.2406 657	0.8644 523	0.2072 682	0.2397 682
4¾	....	....	....	....	....	....	0.8574 853	0.1955 467	0.2280 467
5	0.8522 161	0.1874 156	0.2199 156	0.8511 271	0.1858 070	0.2183 070	0.8505 744	0.1849 996	0.2174 996
5¼	....	....	....	....	....	....	0.8437 192	0.1754 590	0.2079 590
5½	....	....	....	0.8375 174	0.1675 213	0.2000 213	0.8369 192	0.1667 878	0.1992 878
5¾	....	....	....	....	....	....	0.8301 741	0.1588 724	0.1913 724
6	0.8253 908	0.1536 300	0.1861 300	0.8241 254	0.1522 906	0.1847 906	0.8234 833	0.1516 186	0.1841 186
6¼	....	....	....	....	....	....	0.8168 464	0.1449 467	0.1774 467
6½	....	....	....	0.8109 475	0.1394 099	0.1719 099	0.8102 630	0.1387 898	0.1712 898
6¾	....	....	....	....	....	....	0.8037 327	0.1330 905	0.1655 905
7	0.7994 100	0.1295 220	0.1620 220	0.7979 803	0.1283 753	0.1608 753	0.7972 550	0.1277 999	0.1602 999
7¼	....	....	....	....	....	....	0.7908 295	0.1228 756	0.1553 756
7½	....	....	....	0.7852 205	0.1188 179	0.1513 179	0.7844 558	0.1182 812	0.1507 812
7¾	....	....	....	....	....	....	0.7781 334	0.1139 844	0.1464 844
8	0.7742 470	0.1114 627	0.1439 627	0.7726 647	0.1104 606	0.1429 606	0.7718 620	0.1099 577	0.1424 577
8¼	....	....	....	....	....	....	0.7656 412	0.1061 763	0.1386 763
8½	....	....	....	0.7603 097	0.1030 915	0.1355 915	0.7594 705	0.1026 186	0.1351 186
8¾	....	....	....	....	....	....	0.7533 495	0.0992 654	0.1317 654
9	0.7498 760	0.0974 356	0.1299 356	0.7481 522	0.0965 461	0.1290 461	0.7472 779	0.0960 998	0.1285 998
9¼	....	....	....	....	....	....	0.7412 552	0.0931 064	0.1256 064
9½	....	....	....	0.7361 891	0.0906 942	0.1231 942	0.7352 810	0.0902 718	0.1227 718
9¾	....	....	....	....	....	....	0.7293 551	0.0875 835	0.1200 835
10	0.7262 722	0.0862 311	0.1187 311	0.7244 173	0.0854 319	0.1179 319	0.7234 769	0.0850 309	0.1175 309
10¼	....	....	....	....	....	....	0.7176 459	0.0826 037	0.1151 037
10½	....	....	....	0.7128 337	0.0806 748	0.1131 748	0.7118 620	0.0802 932	0.1127 932
10¾	....	....	....	....	....	....	0.7061 248	0.0780 913	0.1105 913
11	0.7034 113	0.0770 794	0.1095 794	0.7014 355	0.0763 541	0.1088 541	0.7004 339	0.0759 902	0.1084 902
11¼	....	....	....	....	....	....	0.6947 887	0.0739 836	0.1064 836
11½	....	....	....	0.6902 194	0.0724 129	0.1049 129	0.6891 890	0.0720 652	0.1045 652
11¾	....	....	....	....	....	....	0.6836 345	0.0702 293	0.1027 293
12	0.6812 700	0.0694 672	0.1019 672	0.6791 826	0.0688 037	0.1013 037	0.6781 246	0.0684 708	0.1009 708
12¼	....	....	....	....	....	....	0.6726 593	0.0667 849	0.0992 849
12½	....	....	....	0.6683 224	0.0654 867	0.0979 867	0.6672 380	0.0651 674	0.0976 674
12¾	....	....	....	....	....	....	0.6618 604	0.0636 141	0.0961 141
13	0.6598 257	0.0630 393	0.0955 393	0.6576 359	0.0624 281	0.0949 281	0.6565 261	0.0621 215	0.0946 215
13¼	....	....	....	....	....	....	0.6512 349	0.0606 859	0.0931 859
13½	....	....	....	0.6471 202	0.0595 993	0.0920 993	0.6459 863	0.0593 043	0.0918 043
13¾	....	....	....	....	....	....	0.6407 799	0.0579 738	0.0904 738
14	0.6390 564	0.0575 418	0.0900 418	0.6367 726	0.0569 756	0.0894 756	0.6356 155	0.0566 915	0.0891 915
14¼	....	....	....	....	....	....	0.6304 927	0.0554 550	0.0879 550
14½	....	....	....	0.6265 905	0.0545 358	0.0870 358	0.6254 112	0.0542 618	0.0867 618
14¾	....	....	....	....	....	....	0.6203 707	0.0531 098	0.0856 098
15	0.6189 408	0.0527 886	0.0852 886	0.6165 712	0.0522 615	0.0847 615	0.6153 708	0.0519 970	0.0844 970
15¼	....	....	....	....	....	....	0.6104 112	0.0509 213	0.0834 213
15½	....	....	....	0.6067 121	0.0501 367	0.0826 367	0.6054 916	0.0498 810	0.0823 810
15¾	....	....	....	....	....	....	0.6006 116	0.0488 744	0.0813 744
16	0.5994 584	0.0486 401	0.0811 401	0.5970 107	0.0481 473	0.0806 473	0.5957 710	0.0479 000	0.0804 000
17	0.5805 892	0.0449 807	0.0774 897	0.5780 708	0.0445 271	0.0770 271	0.5767 954	0.0442 950	0.0767 950
18	0.5623 140	0.0417 542	0.0742 542	0.5597 317	0.0413 186	0.0738 186	0.5584 243	0.0411 001	0.0736 001
19	0.5446 141	0.0388 680	0.0713 680	0.5419 744	0.0384 567	0.0709 567	0.5406 382	0.0382 503	0.0707 503
20	0.5274 712	0.0362 789	0.0687 789	0.5247 805	0.0358 894	0.0683 894	0.5234 187	0.0356 940	0.0681 940
21	0.5108 680	0.0339 442	0.0664 442	0.5081 320	0.0335 746	0.0660 746	0.5067 476	0.0333 892	0.0658 892
22	0.4947 874	0.0318 294	0.0643 294	0.4920 117	0.0314 779	0.0639 779	0.4906 075	0.0313 015	0.0638 015
23	0.4792 130	0.0299 056	0.0624 056	0.4764 028	0.0295 706	0.0620 706	0.4749 814	0.0294 026	0.0619 026
24	0.4641 288	0.0281 489	0.0606 489	0.4612 891	0.0278 292	0.0603 292	0.4598 530	0.0276 688	0.0601 688
25	0.4495 194	0.0265 393	0.0590 393	0.4466 549	0.0262 337	0.0587 337	0.4452 065	0.0260 804	0.0585 804

Years	RATIO *of* INTEREST: *ANNUALLY*, 0.0325.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.01625.			RATIO *of* INTEREST: *QUARTERLY*, 0.008125.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	2.2968 973	39.904 531	17.373 23	2.3122 194	40.375 981	17.462 00	2.3200 429	40.616 704	17.506 88
27	2.3715 464	42.201 428	17.794 90	2.3879 771	42.706 988	17.884 17	2.3963 682	42.965 176	17.929 29
28	2.4486 217	44.572 975	18.203 29	2.4662 169	45.114 367	18.292 94	2.4752 045	45.390 909	18.338 24
29	2.5282 019	47.021 596	18.598 83	2.5470 202	47.600 622	18.688 75	2.5566 344	47.896 443	18.734 18
30	2.6103 684	49.549 798	18.981 92	2.6304 710	50.168 337	19.072 00	2.6407 432	50.484 406	19.117 50
31	2.6952 054	52.160 167	19.352 95	2.7166 559	52.820 181	19.443 09	2.7276 190	53.157 508	19.488 61
32	2.7827 996	54.855 372	19.712 30	2.8056 646	55.558 909	19.802 41	2.8173 529	55.918 550	19.847 83
33	2.8732 406	57.638 172	20.060 34	2.8975 895	58.387 370	20.150 32	2.9100 388	58.770 426	20.195 75
34	2.9666 209	60.511 412	20.397 42	2.9925 263	61.308 502	20.487 20	3.0057 740	61.716 123	20.532 52
35	3.0630 361	63.478 033	20.723 89	3.0905 737	64.325 343	20.813 40	3.1046 587	64.758 729	20.858 56
36	3.1625 847	66.541 069	21.040 09	3.1918 334	67.441 028	21.129 24	3.2067 965	67.901 431	21.174 22
37	3.2653 687	69.703 054	21.346 33	3.2964 108	70.658 795	21.435 07	3.3122 945	71.147 522	21.479 83
38	3.3714 932	72.969 023	21.642 94	3.4044 146	73.981 989	21.731 19	3.4212 632	74.500 405	21.775 70
39	3.4810 668	76.340 516	21.930 21	3.5159 571	77.414 064	22.017 92	3.5338 167	77.963 591	22.062 15
40	3.5942 014	79.821 583	22.208 43	3.6311 541	80.958 589	22.295 55	3.6500 731	81.540 710	22.339 47
41	3.7110 130	83.415 784	22.477 90	3.7501 255	84.619 246	22.564 38	3.7701 541	85.235 509	22.607 96
42	3.8316 209	87.126 797	22.738 89	3.8729 948	88.399 841	22.824 67	3.8941 855	89.051 862	22.867 90
43	3.9561 486	90.958 418	22.991 66	3.9998 899	92.304 304	23.076 71	4.0222 974	92.993 765	23.119 56
44	4.0847 234	94.914 566	23.236 47	4.1309 425	96.336 693	23.320 75	4.1546 239	97.065 350	23.363 21
45	4.2174 769	98.999 290	23.473 58	4.2662 889	100.50 120	23.557 05	4.2913 037	101.27 088	23.599 09
46	4.3545 449	103.21 677	23.703 23	4.4060 699	104.80 215	23.785 85	4.4324 801	105.61 477	23.827 46
47	4.4960 676	107.57 131	23.925 64	4.5504 306	109.24 402	24.007 40	4.5783 009	110.10 157	24.048 56
48	4.6421 898	112.06 738	24.141 06	4.6995 212	113.83 142	24.221 92	4.7289 189	114.73 597	24.262 62
49	4.7930 610	116.70 957	24.349 69	4.8534 966	118.56 913	24.429 63	4.8844 921	119.52 283	24.469 86
50	4.9488 355	121.50 263	24.551 76	5.0125 169	123.46 206	24.630 75	5.0451 833	124.46 718	24.670 50
51	5.1096 726	126.45 147	24.747 47	5.1767 473	128.51 530	24.825 49	5.2111 610	129.57 418	24.864 74
52	5.2757 370	131.56 114	24.937 02	5.3463 586	133.73 411	25.014 06	5.3825 990	134.84 920	25.052 80
53	5.4471 984	136.83 688	25.120 60	5.5215 270	139.12 391	25.196 63	5.5596 771	140.29 776	25.234 87
54	5.6242 324	142.28 407	25.298 40	5.7024 346	144.69 030	25.373 42	5.7425 807	145.92 556	25.411 14
55	5.8070 200	147.90 831	25.470 60	5.8892 696	150.43 906	25.544 60	5.9315 015	151.73 851	25.581 80
56	5.9957 481	153.71 533	25.637 39	6.0822 261	156.37 619	25.710 36	6.1266 375	157.74 269	25.747 02
57	6.1906 099	159.71 107	25.798 92	6.2815 045	162.50 783	25.870 85	6.3281 931	163.94 440	25.906 98
58	6.3918 047	165.90 168	25.955 37	6.4873 121	168.84 037	26.026 24	6.5363 795	170.35 014	26.061 85
59	6.5995 384	172.29 349	26.106 90	6.6998 628	175.38 039	26.176 71	6.7514 150	176.96 661	26.211 78
60	6.8140 234	178.89 303	26.253 66	6.9193 775	182.13 469	26.322 41	6.9735 246	183.80 076	26.356 93
61	7.0354 791	185.70 705	26.395 79	7.1460 844	189.11 029	26.463 48	7.2029 414	190.85 973	26.497 47
62	7.2641 322	192.74 253	26.533 46	7.3802 192	196.31 444	26.600 08	7.4399 055	198.15 094	26.633 53
63	7.5002 165	200.00 666	26.666 78	7.6220 252	203.75 462	26.732 35	7.6846 653	205.68 201	26.765 25
64	7.7439 736	207.50 688	26.795 92	7.8717 537	211.43 857	26.860 42	7.9374 773	213.46 084	26.892 78
65	7.9956 527	215.25 085	26.920 99	8.1296 643	219.37 429	26.984 42	8.1986 004	221.49 558	27.016 24
66	8.2555 114	223.24 650	27.042 12	8.3960 251	227.57 000	27.104 49	8.4683 261	229.79 465	27.135 78
67	8.5238 155	231.50 202	27.159 43	8.6711 130	236.03 425	27.220 74	8.7469 192	238.36 674	27.251 50
68	8.8008 395	240.02 583	27.273 06	8.9552 139	244.77 581	27.333 33	9.0346 774	247.22 084	27.363 55
69	9.0868 668	248.82 667	27.383 11	9.2486 231	253.80 379	27.442 33	9.3319 025	256.36 623	27.472 02
70	9.3821 900	257.91 354	27.489 70	9.5516 456	263.12 756	27.547 88	9.6389 057	265.81 248	27.577 03
71	9.6871 112	267.29 573	27.592 92	9.8645 963	272.75 681	27.650 07	9.9560 087	275.56 950	27.678 71
72	10.001 942	276.98 284	27.692 90	10.187 801	282.70 155	27.749 03	10.283 544	285.64 751	27.777 14
73	10.327 005	286.98 478	27.789 74	10.521 594	292.97 213	27.844 84	10.621 854	296.05 706	27.872 44
74	10.662 633	297.31 179	27.883 52	10.866 324	303.57 921	27.937 62	10.971 295	306.80 907	27.964 70
75	11.009 169	307.97 442	27.974 36	11.222 349	314.53 383	28.027 45	11.332 231	317.91 480	28.054 03
76	11.366 967	318.98 359	28.062 33	11.590 039	325.84 736	28.114 43	11.705 042	329.38 590	28.140 51
77	11.736 393	330.35 056	28.147 54	11.969 776	337.53 157	28.198 65	12.090 117	341.23 437	28.224 23
78	12.117 826	342.08 695	28.230 06	12.361 954	349.59 860	28.280 20	12.487 861	353.47 263	28.305 29
79	12.511 655	354.20 477	28.309 99	12.766 982	362.06 099	28.359 17	12.898 689	366.11 352	28.383 77
80	12.918 284	366.71 643	28.387 39	13.185 280	374.93 171	28.435 63	13.323 033	379.17 026	28.459 75
81	13.338 128	379.63 471	28.462 37	13.617 284	388.22 412	28.509 66	13.761 338	392.65 655	28.533 31
82	13.771 617	392.97 284	28.534 98	14.063 441	401.95 204	28.581 34	14.214 062	406.58 652	28.604 52
83	14.219 195	406.74 446	28.605 31	14.524 217	416.12 975	28.650 75	14.681 679	420.97 475	28.673 47
84	14.681 319	420.96 365	28.673 42	15.000 089	430.77 197	28.717 96	15.164 681	435.83 634	28.740 23
85	15.158 462	435.64 497	28.739 39	15.491 553	445.89 394	28.783 03	15.663 572	451.18 684	28.804 84
86	15.651 112	450.80 343	28.803 29	15.999 119	461.51 136	28.846 05	16.178 876	467.04 235	28.867 41
87	16.159 773	466.45 455	28.865 17	16.523 315	477.64 047	28.907 06	16.711 133	483.41 948	28.927 98
88	16.684 965	482.61 432	28.925 10	17.064 686	494.29 804	28.966 13	17.260 900	500.33 538	28.986 62
89	17.227 227	499.29 928	28.983 15	17.623 795	511.50 138	29.023 34	17.828 753	517.80 779	29.043 40
90	17.787 112	516.52 651	29.039 37	18.201 222	529.26 836	29.078 73	18.415 288	535.85 501	29.098 37
91	18.365 193	534.31 362	29.093 82	18.797 568	547.61 747	29.132 36	19.021 118	554.49 595	29.151 59
92	18.962 061	552.67 881	29.146 56	19.413 452	566.56 777	29.184 29	19.646 880	573.75 015	29.203 11
93	19.578 328	571.64 088	29.197 63	20.049 516	586.13 896	29.234 57	20.293 225	593.63 770	29.252 99
94	20.214 624	591.21 920	29.247 10	20.706 420	606.35 137	29.283 26	20.960 837	614.17 900	29.301 28
95	20.871 599	611.43 383	29.295 02	21.384 846	627.22 603	29.330 40	21.650 412	635.39 728	29.348 04
96	21.549 926	632.30 543	29.341 42	22.035 501	648.78 463	29.376 04	22.362 672	657.31 299	29.393 30
97	22.250 299	653.85 535	29.386 36	22.809 111	671.04 958	29.420 24	23.098 365	679.94 968	29.437 13
98	22.973 434	676.10 565	29.429 89	23.556 430	694.04 401	29.463 04	23.858 260	703.25 416	29.479 55
99	23.720 070	699.07 909	29.472 05	24.328 235	717.79 184	29.504 48	24.643 155	727.48 170	29.520 63
100	24.490 973	722.79 916	29.512 88	25.125 327	742.31 774	29.544 60	25.453 872	752.42 683	29.560 40
	Value of Perpetual Ann.		30.769 23	- - - - - - - - -		30.769 23	- - - - - - - - -		30.769 23

Years.	RATIO of INTEREST: ANNUALLY, 0.0325.			RATIO of INTEREST: HALF-YEARLY, 0.01625.			RATIO of INTEREST: QUARTERLY, 0.008125.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.4353 699	0.0250 598	0.0575 598	0.4324 849	0.0247 672	0.0572 672	0.4310 265	0.0246 204	0.0571 204
27	0.4216 658	0.0236 959	0.0561 959	0.4187 644	0.0234 154	0.0559 154	0.4172 981	0.0232 747	0.0557 747
28	0.4083 930	0.0224 351	0.0549 351	0.4054 793	0.0221 659	0.0546 659	0.4040 070	0.0220 308	0.0545 308
29	0.3955 380	0.0212 668	0.0537 668	0.3926 156	0.0210 081	0.0535 081	0.3911 392	0.0208 784	0.0533 784
30	0.3830 877	0.0201 817	0.0526 817	0.3801 601	0.0199 329	0.0524 329	0.3786 812	0.0198 081	0.0523 081
31	0.3710 293	0.0191 717	0.0516 717	0.3680 996	0.0189 322	0.0514 322	0.3666 201	0.0188 120	0.0513 120
32	0.3593 504	0.0182 298	0.0507 298	0.3564 218	0.0179 991	0.0504 991	0.3549 431	0.0178 832	0.0503 832
33	0.3480 391	0.0173 496	0.0498 496	0.3451 145	0.0171 270	0.0496 270	0.3436 380	0.0170 154	0.0495 154
34	0.3370 838	0.0165 258	0.0490 258	0.3341 658	0.0163 110	0.0488 110	0.3326 930	0.0162 032	0.0487 032
35	0.3264 735	0.0157 535	0.0482 535	0.3235 645	0.0155 460	0.0480 460	0.3220 966	0.0154 419	0.0479 419
36	0.3161 971	0.0150 283	0.0475 283	0.3132 996	0.0148 278	0.0473 278	0.3118 377	0.0147 272	0.0472 272
37	0.3062 441	0.0143 465	0.0468 465	0.3033 603	0.0141 525	0.0466 525	0.3019 055	0.0140 553	0.0465 553
38	0.2966 045	0.0137 044	0.0462 044	0.2937 362	0.0135 168	0.0460 168	0.2922 897	0.0134 227	0.0459 227
39	0.2872 683	0.0130 992	0.0455 992	0.2844 176	0.0129 176	0.0454 176	0.2829 801	0.0128 265	0.0453 265
40	0.2782 259	0.0125 279	0.0450 279	0.2753 945	0.0123 520	0.0448 520	0.2739 671	0.0122 638	0.0447 638
41	0.2694 682	0.0119 881	0.0444 881	0.2666 577	0.0118 176	0.0443 176	0.2652 411	0.0117 322	0.0442 322
42	0.2609 862	0.0114 775	0.0439 775	0.2581 981	0.0113 122	0.0438 122	0.2567 931	0.0112 294	0.0437 294
43	0.2527 711	0.0109 940	0.0434 940	0.2500 069	0.0108 337	0.0433 337	0.2486 141	0.0107 534	0.0432 534
44	0.2448 146	0.0105 358	0.0430 358	0.2420 755	0.0103 803	0.0428 803	0.2406 957	0.0103 023	0.0428 023
45	0.2371 086	0.0101 011	0.0426 011	0.2343 957	0.0099 501	0.0424 501	0.2330 294	0.0098 745	0.0423 745
46	0.2296 451	0.0096 884	0.0421 884	0.2269 596	0.0095 418	0.0420 418	0.2256 073	0.0094 684	0.0419 684
47	0.2224 166	0.0092 962	0.0417 962	0.2197 594	0.0091 538	0.0416 538	0.2184 216	0.0090 825	0.0415 825
48	0.2154 156	0.0089 231	0.0414 231	0.2127 876	0.0087 849	0.0412 849	0.2114 648	0.0087 157	0.0412 157
49	0.2086 349	0.0085 683	0.0410 683	0.2060 370	0.0084 339	0.0409 339	0.2047 296	0.0083 666	0.0408 666
50	0.2020 677	0.0082 303	0.0407 303	0.1995 006	0.0080 997	0.0405 997	0.1982 088	0.0080 342	0.0405 342
51	0.1957 073	0.0079 082	0.0404 082	0.1931 715	0.0077 812	0.0402 812	0.1918 958	0.0077 176	0.0402 176
52	0.1895 470	0.0076 009	0.0401 009	0.1870 432	0.0074 775	0.0399 775	0.1857 838	0.0074 157	0.0399 157
53	0.1835 806	0.0073 080	0.0398 080	0.1811 093	0.0071 878	0.0396 878	0.1798 665	0.0071 277	0.0396 277
54	0.1778 020	0.0070 282	0.0395 282	0.1753 637	0.0069 113	0.0394 113	0.1741 377	0.0068 528	0.0393 528
55	0.1722 054	0.0067 609	0.0392 609	0.1698 003	0.0066 472	0.0391 472	0.1685 914	0.0065 903	0.0390 903
56	0.1667 849	0.0065 055	0.0390 055	0.1644 135	0.0063 948	0.0388 948	0.1632 216	0.0063 394	0.0388 394
57	0.1615 350	0.0062 613	0.0387 613	0.1591 975	0.0061 535	0.0386 535	0.1580 230	0.0060 996	0.0385 996
58	0.1564 503	0.0060 277	0.0385 277	0.1541 470	0.0059 228	0.0384 228	0.1529 899	0.0058 703	0.0383 703
59	0.1515 257	0.0058 041	0.0383 041	0.1492 568	0.0057 019	0.0382 019	0.1481 171	0.0056 508	0.0381 508
60	0.1467 562	0.0055*899	0.0380 899	0.1445 217	0.0054 904	0.0379 904	0.1433 995	0.0054 407	0.0379 407
61	0.1421 367	0.0053 849	0.0378 849	0.1399 368	0.0052 879	0.0377 879	0.1388 322	0.0052 395	0.0377 395
62	0.1376 627	0.0051 883	0.0376 883	0.1354 973	0.0050 939	0.0375 939	0.1344 103	0.0050 467	0.0375 467
63	0.1333 295	0.0049 998	0.0374 998	0.1311 987	0.0049 079	0.0374 079	0.1301 293	0.0048 619	0.0373 619
64	0.1291 327	0.0048 191	0.0373 191	0.1270 365	0.0047 295	0.0372 295	0.1259 846	0.0046 847	0.0371 847
65	0.1250 680	0.0046 457	0.0371 457	0.1230 063	0.0045 584	0.0370 584	0.1219 719	0.0045 148	0.0370 148
66	0.1211 312	0.0044 794	0.0369 794	0.1191 040	0.0043 943	0.0368 943	0.1180 871	0.0043 517	0.0368 517
67	0.1173 184	0.0043 196	0.0368 196	0.1153 255	0.0042 367	0.0367 367	0.1143 259	0.0041 952	0.0366 952
68	0.1136 255	0.0041 662	0.0366 662	0.1116 668	0.0040 854	0.0365 854	0.1106 846	0.0040 450	0.0365 450
69	0.1100 489	0.0040 189	0.0365 189	0.1081 242	0.0039 401	0.0364 401	0.1071 593	0.0039 007	0.0364 007
70	0.1065 849	0.0038 773	0.0363 773	0.1046 940	0.0038 004	0.0363 004	0.1037 462	0.0037 621	0.0362 621
71	0.1032 300	0.0037 412	0.0362 412	0.1013 726	0.0036 663	0.0361 663	0.1004 418	0.0036 289	0.0361 289
72	0.0999 806	0.0036 103	0.0361 103	0.0981 566	0.0035 373	0.0360 373	0.0972 427	0.0035 008	0.0360 008
73	0.0968 335	0.0034 845	0.0359 845	0.0950 426	0.0034 133	0.0359 133	0.0941 455	0.0033 777	0.0358 777
74	0.0937 855	0.0033 635	0.0358 635	0.0920 274	0.0032 940	0.0357 940	0.0911 469	0.0032 594	0.0357 594
75	0.0908 334	0.0032 470	0.0357 470	0.0891 079	0.0031 793	0.0356 793	0.0882 439	0.0031 455	0.0356 455
76	0.0879 742	0.0031 350	0.0356 350	0.0862 810	0.0030 689	0.0355 689	0.0854 333	0.0030 360	0.0355 360
77	0.0852 051	0.0030 271	0.0355 271	0.0835 437	0.0029 627	0.0354 627	0.0827 122	0.0029 305	0.0354 305
78	0.0825 231	0.0029 232	0.0354 232	0.0808 934	0.0028 604	0.0353 604	0.0800 778	0.0028 291	0.0353 291
79	0.0799 255	0.0028 232	0.0353 232	0.0783 270	0.0027 620	0.0352 620	0.0775 272	0.0027 314	0.0352 314
80	0.0774 097	0.0027 269	0.0352 269	0.0758 421	0.0026 672	0.0351 672	0.0750 580	0.0026 373	0.0351 373
81	0.0749 730	0.0026 341	0.0351 341	0.0734 361	0.0025 758	0.0350 758	0.0726 673	0.0025 468	0.0350 468
82	0.0726 131	0.0025 447	0.0350 447	0.0711 064	0.0024 879	0.0349 879	0.0703 529	0.0024 595	0.0349 595
83	0.0703 275	0.0024 585	0.0349 585	0.0688 505	0.0024 031	0.0349 031	0.0681 121	0.0023 754	0.0348 754
84	0.0681 138	0.0023 755	0.0348 755	0.0666 663	0.0023 214	0.0348 214	0.0659 427	0.0022 944	0.0347 944
85	0.0659 698	0.0022 954	0.0347 954	0.0645 513	0.0022 427	0.0347 427	0.0638 424	0.0022 164	0.0347 164
86	0.0638 932	0.0022 183	0.0347 183	0.0625 034	0.0021 668	0.0346 668	0.0618 090	0.0021 411	0.0346 411
87	0.0618 821	0.0021 438	0.0346 438	0.0605 205	0.0020 936	0.0345 936	0.0598 403	0.0020 686	0.0345 686
88	0.0599 342	0.0020 721	0.0345 721	0.0586 005	0.0020 231	0.0345 231	0.0579 344	0.0019 987	0.0344 987
89	0.0580 476	0.0020 028	0.0345 028	0.0567 415	0.0019 550	0.0344 550	0.0560 892	0.0019 312	0.0344 312
90	0.0562 205	0.0019 360	0.0344 360	0.0549 414	0.0018 894	0.0343 894	0.0543 027	0.0018 662	0.0343 662
91	0.0544 508	0.0018 716	0.0343 716	0.0531 984	0.0018 261	0.0343 261	0.0525 731	0.0018 034	0.0343 034
92	0.0527 369	0.0018 094	0.0343 094	0.0515 107	0.0017 650	0.0342 650	0.0508 987	0.0017 429	0.0342 429
93	0.0510 769	0.0017 493	0.0342 493	0.0498 765	0.0017 061	0.0342 061	0.0492 775	0.0016 845	0.0341 845
94	0.0494 691	0.0016 914	0.0341 914	0.0482 942	0.0016 492	0.0341 492	0.0477 080	0.0016 282	0.0341 282
95	0.0479 120	0.0016 355	0.0341 355	0.0467 621	0.0015 943	0.0340 943	0.0461 885	0.0015 738	0.0340 738
96	0.0464 039	0.0015 815	0.0340 815	0.0452 786	0.0015 413	0.0340 413	0.0447 174	0.0015 214	0.0340 214
97	0.0449 432	0.0015 294	0.0340 294	0.0438 421	0.0014 902	0.0339 902	0.0432 931	0.0014 707	0.0339 707
98	0.0435 285	0.0014 791	0.0339 791	0.0424 513	0.0014 408	0.0339 408	0.0419 142	0.0014 218	0.0339 218
99	0.0421 584	0.0014 304	0.0339 304	0.0411 045	0.0013 932	0.0338 932	0.0405 792	0.0013 746	0.0338 746
100	0.0408 314	0.0013 835	0.0338 835	0.0398 005	0.0013 471	0.0338 471	0.0392 867	0.0013 290	0.0338 290
	Ratio of Perpetual Ann.		0.0325 000	- - - - - - - - - -		0.0325 000	- - - - - - - - -		0.0325 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.035.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.0175.			RATIO *of* INTEREST: *QUARTERLY*, 0.00875.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
$0\frac{1}{4}$	....	....	....	....	....	....	1.0087 500	0.2500 000	0.247 831
$0\frac{1}{2}$	....	....	....	1.0175 000	0.5000 000	0.491 400	1.0175 766	0.5021 875	0.493 513
$0\frac{3}{4}$	....	....	....	....	....	....	1.0264 804	0.7565 816	0.737 064
1	1.0350 000	1.0000 000	0.9661 84	1.0353 063	1.0087 500	0.974 349	1.0354 621	1.0132 017	0.978 502
$1\frac{1}{4}$	....	....	....	....	....	....	1.0445 224	1.2720 672	1.217 846
$1\frac{1}{2}$	....	....	....	1.0534 241	1.5264 031	1.448 992	1.0536 619	1.5331 978	1.455 114
$1\frac{3}{4}$	....	....	....	....	....	....	1.0628 815	1.7966 133	1.690 323
2	1.0712 250	2.0350 000	1.8996 94	1.0718 590	2.0531 152	1.915 471	1.0721 817	2.0623 337	1.923 493
$2\frac{1}{4}$	....	....	....	....	....	....	1.0815 633	2.3303 791	2.154 640
$2\frac{1}{2}$	....	....	....	1.0906 166	2.5890 447	2.373 928	1.0910 269	2.6007 699	2.383 782
$2\frac{3}{4}$	....	....	....	....	....	....	1.1005 734	2.8735 267	2.610 936
3	1.1087 179	3.1062 250	2.801 636	1.1097 024	3.1343 530	2.824 499	1.1102 034	3.1486 700	2.836 120
$3\frac{1}{4}$	....	....	....	....	....	....	1.1199 178	3.4262 209	3.059 350
$3\frac{1}{2}$	....	....	....	1.1291 221	3.6892 042	3.267 321	1.1297 171	3.7062 003	3.280 645
$3\frac{3}{4}$	....	....	....	....	....	....	1.1396 021	3.9836 296	3.500 020
4	1.1475 230	4.2149 429	3.673 080	1.1488 818	4.2537 652	3.702 526	1.1495 737	4.2735 301	3.717 492
$4\frac{1}{4}$	....	....	....	....	....	....	1.1596 324	4.5609 236	3.933 077
$4\frac{1}{2}$	....	....	....	1.1689 872	4.8282 061	4.130 247	1.1697 792	4.8508 317	4.146 793
$4\frac{3}{4}$	....	....	....	....	....	....	1.1800 148	5.1432 765	4.358 655
5	1.1876 863	5.3624 659	4.515 052	1.1894 445	5.4126 997	4.550 611	1.1903 399	5.4332 802	4.568 679
$5\frac{1}{4}$	....	....	....	....	....	....	1.2007 554	5.7358 651	4.776 881
$5\frac{1}{2}$	....	....	....	1.2102 598	6.0074 220	4.963 746	1.2112 620	6.0360 540	4.983 277
$5\frac{3}{4}$	....	....	....	....	....	....	1.2218 605	6.3388 695	5.187 883
6	1.2292 553	6.5501 522	5.328 553	1.2314 393	6.6125 519	5.369 775	1.2325 518	6.6443 346	5.390 715
$6\frac{1}{4}$	....	....	....	....	....	....	1.2433 366	6.9524 726	5.591 786
$6\frac{1}{2}$	....	....	....	1.2529 895	7.2282 715	5.768 821	1.2542 158	7.2633 067	5.791 114
$6\frac{3}{4}$	....	....	....	....	....	....	1.2651 902	7.5768 607	5.988 713
7	1.2722 793	7.7794 075	6.114 544	1.2749 168	7.8547 663	6.161 002	1.2762 606	7.8931 582	6.184 598
$7\frac{1}{4}$	....	....	....	....	....	....	1.2874 279	8.2122 234	6.378 783
$7\frac{1}{2}$	....	....	....	1.2972 279	8.4922 247	6.546 440	1.2986 929	8.5340 804	6.571 285
$7\frac{3}{4}$	....	....	....	....	....	....	1.3100 565	8.8567 536	6.762 116
8	1.3168 090	9.0516 858	6.873 956	1.3199 294	9.1408 386	6.925 249	1.3215 195	9.1862 677	6.951 292
$8\frac{1}{4}$	....	....	....	....	....	....	1.3330 828	9.5166 476	7.138 828
$8\frac{1}{2}$	....	....	....	1.3430 281	9.8008 033	7.297 541	1.3447 472	9.8499 183	7.324 736
$8\frac{3}{4}$	....	....	....	....	....	....	1.3565 138	10.186 105	7.509 032
9	1.3628 974	10.368 496	7.607 636	1.3665 311	10.472 317	7.663 431	1.3683 833	10.525 234	7.691 729
$9\frac{1}{4}$	....	....	....	....	....	....	1.3803 566	10.867 329	7.872 842
$9\frac{1}{2}$	....	....	....	1.3904 454	11.155 583	8.023 028	1.3924 347	11.212 419	8.052 384
$9\frac{3}{4}$	....	....	....	....	....	....	1.4046 186	11.560 527	8.230 368
10	1.4105 988	11.731 393	8.316 605	1.4147 782	11.850 806	8.376 441	1.4169 090	11.911 682	8.406 808
$10\frac{1}{4}$	....	....	....	....	....	....	1.4293 069	12.265 909	8.581 719
$10\frac{1}{2}$	....	....	....	1.4395 363	12.558 195	8.723 775	1.4418 134	12.623 236	8.755 111
$10\frac{3}{4}$	....	....	....	....	....	....	1.4544 292	12.983 689	8.927 000
11	1.4599 697	13.141 992	9.001 552	1.4647 287	13.277 963	9.065 135	1.4671 555	13.347 296	9.097 398
$11\frac{1}{4}$	....	....	....	....	....	....	1.4799 931	13.714 085	9.266 317
$11\frac{1}{2}$	....	....	....	1.4903 615	14.010 327	9.400 623	1.4929 430	14.084 084	9.433 772
$11\frac{3}{4}$	....	....	....	....	....	....	1.5060 063	14.457 319	9.599 774
12	1.5110 687	14.601 962	9.663 333	1.5164 428	14.755 508	9.730 342	1.5191 838	14.833 821	9.764 336
$12\frac{1}{4}$	....	....	....	....	....	....	1.5324 767	15.213 617	9.927 471
$12\frac{1}{2}$	....	....	....	1.5429 805	15.513 730	10.05 439	1.5458 858	15.596 736	10.08 919
$12\frac{3}{4}$	....	....	....	....	....	....	1.5594 123	15.983 207	10.24 951
13	1.5639 561	16.113 030	10.30 274	1.5699 827	16.285 220	10.37 287	1.5730 572	16.373 061	10.40 843
$13\frac{1}{4}$	....	....	....	....	....	....	1.5868 215	16.766 325	10.56 598
$13\frac{1}{2}$	....	....	....	1.5974 574	17.070 211	10.68 586	1.6007 062	17.163 030	10.72 216
$13\frac{3}{4}$	....	....	....	....	....	....	1.6147 123	17.563 207	10.87 699
14	1.6186 945	17.676 986	10.92 052	1.6254 129	17.868 940	10.99 348	1.6288 411	17.966 885	11.03 047
$14\frac{1}{4}$	....	....	....	....	....	....	1.6430 934	18.374 095	11.18 262
$14\frac{1}{2}$	....	....	....	1.6538 576	18.681 646	11.29 580	1.6574 705	18.784 868	11.33 346
$14\frac{3}{4}$	....	....	....	....	....	....	1.6719 734	19.199 236	11.48 298
15	1.6753 488	19.295 681	11.51 741	1.6828 001	19.508 575	11.59 292	1.6866 031	19.617 229	11.63 121
$15\frac{1}{4}$	....	....	....	....	....	....	1.7013 609	20.038 880	11.77 815
$15\frac{1}{2}$	....	....	....	1.7122 491	20.349 975	11.88 494	1.7162 478	20.464 220	11.92 381
$15\frac{3}{4}$	....	....	....	....	....	....	1.7312 650	20.893 282	12.06 822
16	1.7339 860	20.971 030	12.09 411	1.7422 135	21.206 100	12.17 193	1.7464 136	21.326 099	12.21 137
17	1.7946 756	22.705 016	12.65 132	1.8037 245	22.963 558	12.73 119	1.8083 450	23.095 568	12.77 166
18	1.8574 892	24.499 691	13.18 968	1.8674 073	24.783 065	13.27 138	1.8724 726	24.927 786	13.31 277
19	1.9225 013	26.357 181	13.70 984	1.9333 384	26.666 812	13.79 314	1.9388 744	26.824 979	13.83 534
20	1.9897 889	28.279 682	14.21 240	2.0015 973	28.617 067	14.29 712	2.0076 308	28.789 449	14.34 002
21	2.0594 315	30.269 471	14.69 797	2.0722 662	30.636 178	14.78 390	2.0788 258	30.823 585	14.82 740
22	2.1315 116	32.328 902	15.16 712	2.1454 302	32.726 577	15.25 409	2.1525 452	32.929 854	15.29 810
23	2.2061 145	34.460 414	15.62 041	2.2211 773	34.890 780	15.70 824	2.2288 789	35.110 817	15.75 268
24	2.2833 285	36.666 528	16.05 837	2.2995 987	37.131 392	16.14 690	2.3079 195	37.369 121	16.19 170
25	2.3632 450	38.949 857	16.48 151	2.3807 889	39.451 112	16.57 060	2.3897 631	39.707 509	16.61 567

Years.	RATIO of INTEREST: ANNUALLY, 0.035.			RATIO of INTEREST: HALF-YEARLY, 0.0175.			RATIO of INTEREST: QUARTERLY, 0.00875.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
0	....	....	....	....	....	....	0.9913 259	4.0000 000	4.0350 000
½	....	....	....	0.9828 010	2.0000 000	2.0350 000	0.9827 271	1.9912 881	2.0262 881
¼	....	....	....	....	....	....	0.9742 028	1.3217 344	1.3567 344
1	0.9661 836	1.0000 000	1.0350 000	0.9658 978	0.9913 259	1.0263 259	0.9657 525	0.9869 702	1.0219 702
1¼	....	....	....	....	....	....	0.9573 754	0.7861 220	0.8211 220
1½	....	....	....	0.9492 853	0.6551 349	0.6901 349	0.9490 710	0.6522 316	0.6872 316
1¾	....	....	....	....	....	....	0.9408 387	0.5566 028	0.5916 028
2	0.9335 107	0.4914 005	0.5264 005	0.9329 585	0.4870 648	0.5220 648	0.9326 777	0.4848 876	0.5198 876
2¼	....	....	....	....	....	....	0.9245 876	0.4291 148	0.4641 148
2½	....	....	....	0.9169 125	0.3862 428	0.4212 428	0.9165 677	0.3845 015	0.4195 015
2¾	....	....	....	....	....	....	0.9086 172	0.3480 044	0.3830 044
3	0.9019 427	0.3219 342	0.3569 342	0.9011 425	0.3190 451	0.3540 451	0.9007 358	0.3175 944	0.3525 944
3¼	....	....	....	....	....	....	0.8929 227	0.2918 667	0.3268 667
3½	....	....	....	0.8856 438	0.2710 612	0.3060 612	0.8851 774	0.2698 181	0.3048 181
3¾	....	....	....	....	....	....	0.8774 993	0.2507 127	0.2857 127
4	0.8714 422	0.2372 511	0.2722 511	0.8704 116	0.2350 858	0 2700 858	0.8698 878	0.2339 986	0.2689 986
4¼	....	....	....	....	....	....	0.8623 423	0.2192 539	0.2542 539
4½	....	....	....	0.8554 412	0.2071 162	0.2421 162	0.8548 622	0.2061 502	0.2411 502
4¾	....	....	....	....	....	....	0.8474 471	0.1944 286	0.2294 286
5	0.8419 731	0.1864 814	0.2214 814	0.8407 286	0.1847 507	0.2197 507	0.8400 962	0.1838 817	0.2188 817
5¼	....	....	....	....	....	....	0.8328 092	0.1743 416	0.2093 416
5½	....	....	....	0.8262 689	0.1664 607	0.2014 607	0.8255 853	0.1656 712	0.2006 712
5¾	....	....	....	....	....	....	0.8184 241	0.1577 568	0.1927 568
6	0.8135 006	0.1526 682	0.1876 682	0.8120 579	0.1512 276	0.1862 276	0.8113 250	0.1505 042	0.1855 042
6¼	....	....	....	....	....	....	0.3042 874	0.1438 337	0.1788 337
6½	....	....	....	0.7980 913	0.1383 458	0.1733 458	0.7973 110	0.1376 783	0.1726 783
6¾	....	....	....	....	....	....	0.7903 951	0.1319 868	0.1669 868
7	0.7859 910	0.1285 445	0.1635 445	0.7843 649	0.1273 112	0.1623 112	0.7835 391	0.1266 920	0.1616 920
7¼	....	....	....	....	....	....	0.7767 425	0.1217 697	0.1567 697
7½	....	....	....	0.7708 746	0.1177 548	0.1527 548	0.7700 050	0.1171 772	0.1521 772
7¾	....	....	....	....	....	....	0.7633 266	0.1128 827	0.1478 827
8	0.7594 116	0.1104 766	0.1454 766	0.7576 163	0.1093 991	0.1443 991	0.7567 048	0.1088 582	0.1438 582
8¼	....	....	....	....	....	....	0.7501 410	0.1050 790	0.1400 790
8½	....	....	....	0.7445 860	0.1020 325	0.1370 325	0.7436 342	0.1015 237	0.1365 237
8¾	....	....	....	....	....	....	0.7371 839	0.0981 730	0.1331 730
9	0.7337 310	0.0964 460	0.1314 460	0.7317 799	0.0954 899	0.1304 899	0.7307 895	0.0950 098	0.1300 098
9¼	....	....	....	....	....	....	0.7244 505	0.0920 189	0.1270 189
9½	....	....	....	0.7191 940	0.0896 412	0.1246 412	0.7181 666	0.0891 868	0.1241 868
9¾	....	....	....	....	....	....	0.7119 371	0.0865 012	0.1215 012
10	0.7089 188	0.0852 414	0.1202 414	0.7068 246	0.0843 824	0.1193 824	0.7057 617	0.0839 512	0.1189 512
10¼	....	....	....	....	....	....	0.6996 399	0.0815 268	0.1165 268
10½	....	....	....	0.6946 679	0.0796 293	0.1146 293	0.6935 711	0.0792 190	0.1142 190
10¾	....	....	....	....	....	....	0.6875 550	0.0770 197	0.1120 197
11	0.6849 457	0.0760 920	0.1110 920	0.6827 203	0.0753 128	0.1103 128	0.6815 911	0.0749 215	0.1099 215
11¼	....	....	....	....	....	....	0.6756 789	0.0729 177	0.1079 177
11½	....	....	....	0.6709 782	0.0713 759	0.1063 759	0.6698 180	0.0710 021	0.1060 021
11¾	....	....	....	....	....	....	0.6640 079	0.0691 691	0.1041 691
12	0.6617 833	0.0684 839	0.1034 839	0.6594 380	0.0677 713	0.1027 713	0.6582 482	0.0674 135	0.1024 135
12¼	....	....	....	....	....	....	0.6525 386	0.0657 306	0.1007 306
12½	....	....	....	0.6480 963	0.0644 590	0.0994 590	0.6468 784	0.0641 160	0.0991 160
12¾	....	....	....	....	....	....	0.6412 673	0.0625 657	0.0975 657
13	0.6394 042	0.0620 616	0.0970 616	0.6369 497	0.0614 054	0.0964 054	0.6357 049	0.0610 759	0.0960 759
13¼	....	....	....	....	....	....	0.6301 907	0.0596 434	0.0946 434
13½	....	....	....	0.6259 945	0.0585 816	0.0935 816	0.6247 243	0.0582 648	0.0932 648
13¾	....	....	....	....	....	....	0.6193 054	0.0569 372	0.0919 372
14	0.6177 818	0.0565 707	0.0915 707	0.6152 283	0.0559 630	0.0909 630	0.6139 335	0.0556 579	0.0906 579
14¼	....	....	....	....	....	....	0.6086 082	0.0544 245	0.0894 245
14½	....	....	....	0.6046 469	0.0535 285	0.0885 285	0.6033 291	0.0532 343	0.0882 343
14¾	....	....	....	....	....	....	0.5980 957	0.0520 854	0.0870 854
15	0.5968 905	0.0518 251	0.0868 251	0.5942 476	0.0512 595	0.0862 595	0.5929 077	0.0509 756	0.0859 756
15¼	....	....	....	....	....	....	0.5877 648	0.0499 030	0.0849 030
15½	....	....	....	0.5840 271	0.0491 401	0.0841 401	0.5826 665	0.0488 658	0.0838 658
15¾	....	....	....	....	....	....	0.5776 124	0.0478 623	0.0828 623
16	0.5767 059	0.0476 848	0.0826 848	0.5739 824	0.0471 562	0.0821 562	0.5726 021	0.0468 909	0.0818 909
17	0.5572 038	0.0440 431	0.0790 431	0.5544 084	0.0435 473	0.0785 473	0.5529 919	0.0432 983	0.0782 983
18	0.5383 611	0.0408 168	0.0758 168	0.5355 018	0.0403 501	0.0753 501	0.5340 533	0.0401 159	0.0751 159
19	0.5201 557	0.0379 403	0.0729 403	0.5172 400	0.0374 998	0.0724 998	0.5157 632	0.0372 787	0.0722 787
20	0.5025 659	0.0353 611	0.0703 611	0.4996 010	0.0349 442	0.0699 442	0.4980 996	0.0347 349	0.0697 349
21	0.4855 709	0.0330 366	0.0680 366	0.4825 635	0.0326 411	0.0676 411	0.4810 409	0.0324 427	0.0674 427
22	0.4691 506	0.0309 321	0.0659 321	0.4661 070	0.0305 562	0.0655 562	0.4645 664	0.0303 676	0.0653 676
23	0.4532 856	0.0290 188	0.0640 188	0.4502 117	0.0286 609	0.0636 609	0.4486 561	0.0284 812	0.0634 812
24	0.4379 572	0.0272 728	0.0622 728	0.4348 585	0.0269 314	0.0619 314	0.4332 907	0.0267 601	0.0617 601
25	0.4231 470	0.0256 740	0.0606 740	0.4200 288	0.0253 478	0.0603 478	0.4184 516	0.0251 842	0.0601 842

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.035.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.0175.			RATIO *of* INTEREST: *QUARTERLY*, 0.00875.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	2.4459 586	41.313 102	16.89 035	2.4648 457	41.852 742	16.97 986	2.4745 085	42.128 813	17.02 512
27	2.5315 671	43.759 060	17.28 537	2.5518 700	44.339 142	17.37 516	2.5622 598	44.635 991	17.42 056
28	2.6201 720	46.290 627	17.66 702	2.6419 670	46.913 348	17.75 698	2.6531 227	47.232 078	17.80 245
29	2.7118 780	48.910 799	18.03 577	2.7352 450	49.578 427	18.12 577	2.7472 079	49.920 225	18.17 126
30	2.8067 937	51.622 677	18.39 204	2.8318 164	52.337 617	18.48 199	2.8446 296	52.703 704	18.52 744
31	2.9050 315	54.429 471	18.73 628	2.9317 972	55.194 206	18.82 606	2.9455 060	55.585 887	18.87 142
32	3.0067 076	57.334 503	19.06 887	3.0353 079	58.151 653	19.15 841	3.0499 598	58.570 296	19.20 363
33	3.1119 424	60.341 210	19.39 021	3.1424 732	61.213 518	19.47 941	3.1581 177	61.660 505	19.52 445
34	3.2208 603	63.453 152	19.70 068	3.2534 221	64.383 502	19.78 947	3.2701 110	64.860 318	19.83 429
35	3.3335 905	66.674 013	20.00 066	3.3682 882	67.665 381	20.08 895	3.3860 758	68.173 589	20.13 351
36	3.4502 661	70.007 603	20.29 050	3.4872 098	71.063 139	20.37 822	3.5061 530	71.604 373	20.42 249
37	3.5710 254	73.457 869	20.57 053	3.6103 302	74.580 868	20.65 763	3.6304 886	75.156 818	20.70 157
38	3.6960 113	77.028 895	20.84 109	3.7377 974	78.222 787	20.92 751	3.7592 331	78.835 227	20.97 110
39	3.8253 717	80.724 906	21.10 250	3.8697 652	81.993 292	21.18 818	3.8925 431	82.644 088	21.23 139
40	3.9592 597	84.550 278	21.35 507	4.0063 921	85.896 921	21.43 997	4.0305 803	86.588 022	21.48 276
41	4.0978 338	88.509 538	21.59 910	4.1478 428	89.938 361	21.68 317	4.1735 136	90.671 817	21.72 554
42	4.2412 580	92.607 371	21.83 488	4.2942 874	94.122 500	21.91 807	4.3215 148	94.900 430	21.96 000
43	4.3897 020	96.848 629	22.06 269	4.4459 026	98.454 368	22.14 497	4.4747 649	99.279 000	22.18 642
44	4.5433 416	101.23 833	22.28 279	4.6028 708	102.93 917	22.36 412	4.6334 491	103.81 285	22.40 509
45	4.7023 586	105.78 167	22.49 545	4.7653 808	107.58 231	22.57 580	4.7977 610	108.50 746	22.61 627
46	4.8669 411	110.48 403	22.70 092	4.9336 291	112.38 940	22.78 027	4.9678 994	113.36 858	22.82 022
47	5.0372 840	115.35 097	22.89 942	5.1078 165	117.36 376	22.97 776	5.1440 712	118.40 204	23.01 718
48	5.2135 890	120.38 826	23.09 125	5.2881 543	122.51 869	23.16 852	5.3264 905	123.61 403	23.20 740
49	5.3960 646	125.60 185	23.27 657	5.4748 594	127.85 312	23.35 277	5.5153 790	129.01 083	23.39 111
50	5.5849 269	130.99 791	23.45 561	5.6681 561	133.37 589	23.53 074	5.7109 654	134.59 900	23.56 852
51	5.7803 993	136.58 284	23.62 862	5.8682 775	139.09 365	23.70 264	5.9134 881	140.38 538	23.73 986
52	5.9827 133	142.36 324	23.79 577	6.0754 639	145.01 324	23.86 867	6.1231 928	146.37 695	23.90 533
53	6.1921 083	148.34 595	23.95 726	6.2899 664	151.14 190	24.02 905	6.3403 333	152.58 096	24.06 513
54	6.4088 320	154.53 806	24.11 330	6.5120 411	157.48 690	24.18 395	6.5651 747	159.00 501	24.21 946
55	6.6331 412	160.94 689	24.26 405	6.7419 571	164.05 592	24.33 357	6.7979 894	165.65 683	24.36 851
56	6.8653 011	167.58 003	24.40 971	6.9799 907	170.85 688	24.47 810	7.0390 604	172.54 457	24.51 245
57	7.1055 866	174.44 533	24.55 044	7.2264 275	177.89 793	24.61 769	7.2886 798	179.67 658	24.65 146
58	7.3542 822	181.55 092	24.68 643	7.4815 653	185.18 757	24.75 252	7.5471 515	187.06 147	24.78 571
59	7.6116 820	188.90 520	24.81 779	7.7457 111	192.73 461	24.88 275	7.8147 890	194.70 825	24.91 536
60	7.8780 909	196.51 688	24.94 474	8.0191 839	200.54 192	25.00 855	8.0919 177	202.62 622	25.04 057
61	8.1538 241	204.39 497	25.06 737	8.3023 109	208.63 745	25.13 005	8.3788 735	210.82 496	25.16 149
62	8.4392 079	212.54 880	25.18 587	8.5954 349	217.01 245	25.24 741	8.6760 072	219.31 451	25.27 828
63	8.7345 802	220.98 801	25.30 036	8.8989 071	225.68 305	25.36 076	8.9836 750	228.10 501	25.39 106
64	9.0402 905	229.72 259	25.41 097	9.2130 938	234.65 982	25.47 025	9.3022 544	237.20 727	25.49 998
65	9.3567 007	238.76 288	25.51 785	9.5383 738	243.95 354	25.57 601	9.6321 311	246.63 233	25.60 517
66	9.6841 852	248.11 958	25.62 111	9.8751 382	253.57 545	25.67 816	9.9737 067	256.39 162	25.70 675
67	10.023 132	257.80 376	25.72 088	10.223 792	263.53 694	25.77 683	10.327 395	266.49 701	25.80 486
68	10.373 941	267.82 689	25.81 728	10.584 756	273.85 019	25.87 213	10.693 625	276.96 070	25.89 961
69	10.737 029	278.20 084	25.91 041	10.958 463	284.52 751	25.96 418	11.072 843	287.79 552	25.99 111
70	11.112 825	288.93 787	26.00 040	11.345 366	295.58 190	26.05 309	11.465 509	299.01 455	26.07 948
71	11.501 774	300.05 069	26.08 734	11.745 929	307.02 654	26.13 898	11.872 100	310.63 141	26.16 483
72	11.904 336	311.55 246	26.17 135	12.160 633	318.87 477	26.22 193	12.293 109	322.66 026	26.24 725
73	12.320 988	323.45 680	26.25 250	12.589 981	331.14 229	26.30 205	12.729 048	335.11 570	26.32 684
74	12.752 223	335.77 779	26.33 092	13.034 485	343.84 239	26.37 944	13.180 446	348.01 273	26.40 371
75	13.198 550	348.53 001	26.40 669	13.494 684	356.99 098	26.45 420	13.647 852	361.36 723	26.47 796
76	13.660 500	361.72 856	26.47 989	13.971 130	370.60 374	26.52 640	14.131 833	375.19 521	26.54 965
77	14.138 617	375.38 906	26.55 062	14.464 399	384.69 711	26.59 614	14.632 977	389.51 359	26.61 889
78	14.633 469	389.52 768	26.61 896	14.975 083	399.28 812	26.66 350	15.151 892	404.33 976	26.68 576
79	15.145 640	404.16 115	26.68 498	15.503 795	414.39 410	26.72 856	15.689 209	419.69 166	26.75 034
80	15.675 738	419.30 679	26.74 877	16.051 177	430.03 361	26.79 141	16.245 582	435.58 802	26.81 271
81	16.224 388	434.98 252	26.81 041	16.617 883	446.22 521	26.85 211	16.821 683	452.04 806	26.87 294
82	16.792 242	451.20 691	26.86 996	17.204 599	462.98 850	26.91 074	17.418 214	469.09 186	26.93 111
83	17.379 970	467.99 916	26.92 750	17.812 029	480.34 365	26.96 738	18.035 900	486.74 000	26.98 729
84	17.988 269	485.37 913	26.98 309	18.440 904	498.31 159	27.02 208	18.675 490	505.01 394	27.04 154
85	18.617 859	503.36 740	27.03 680	19.091 984	516.91 390	27.07 492	19.337 762	523.93 605	27.09 393
86	19.269 484	521.98 525	27.08 870	19.766 050	536.17 289	27.12 595	20.023 520	543.52 916	27.14 454
87	19.943 916	541.25 474	27.13 884	20.463 917	556.11 194	27.17 524	20.733 596	563.81 698	27.19 340
88	20.641 953	561.19 861	27.18 728	21.186 418	576.75 481	27.22 285	21.468 851	584.82 432	27.24 060
89	21.364 421	581.84 061	27.23 409	21.934 434	598.12 669	27.26 885	22.230 179	606.57 659	27.28 617
90	22.112 176	603.20 503	27.27 932	22.708 856	620.25 306	27.31 327	23.018 508	629.10 025	27.33 019
91	22.886 102	625.31 720	27.32 301	23.510 621	64.316 062	27.35 617	23.834 791	652.42 258	27.37 270
92	23.687 116	648.20 331	27.36 522	24.340 691	666.87 692	27.39 761	24.680 022	676.57 208	27.41 375
93	24.516 165	671.89 042	27.40 602	25.200 071	691.43 060	27.43 764	25.555 226	701.57 789	27.45 340
94	25.374 231	696.40 659	27.44 543	26.089 790	716.85 121	27.47 631	26.461 468	727.47 052	27.49 169
95	26.262 329	721.78 082	27.48 351	27.010 922	743.16 917	27.51 365	27.399 845	754.28 128	27.52 867
96	27.181 510	748.04 315	27.52 029	27.964 577	770.41 650	27.54 973	28.371 502	782.04 288	27.56 438
97	28.132 863	775.22 466	27.55 584	28.951 900	798.62 576	27.58 457	29.377 613	810.78 900	27.59 887
98	29.117 513	803.35 752	27.59 018	29.974 085	827.83 100	27.61 823	30.419 403	840.55 437	27.63 218
99	30.136 626	832.47 503	27.62 337	31.032 357	858.06 733	27.65 073	31.498 138	871.37 540	27.66 434
100	31.191 408	862.61 166	27.65 543	32.127 993	889.37 122	27.68 213	32.615 128	903.28 940	27.69 541
	Value of Perpetual Ann.		28.57 143	- - - - - - - - - -		28.57 143	- - - - - - - - - -		28.57 143

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.035.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.0175.			RATIO *of* INTEREST: *QUARTERLY*, 0.00875.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.4088 377	0.0242 054	0.0592 054	0.4057 049	0.0238 933	0.0588 933	0.4041 207	0.0237 367	0.0587 367
27	0.3950 122	0.0228 524	0.0578 524	0.3918 695	0.0225 534	0.0575 534	0.3902 805	0.0224 034	0.0574 034
28	0.3816 543	0.0216 026	0.0566 026	0.3785 058	0.0213 159	0.0563 159	0.3769 143	0.0211 721	0.0561 721
29	0.3687 482	0.0204 454	0.0554 454	0.3655 980	0.0201 701	0.0551 701	0.3640 059	0.0200 320	0.0550 320
30	0.3562 784	0.0193 713	0.0543 713	0.3531 303	0.0191 067	0.0541 067	0.3515 396	0.0189 740	0.0539 740
31	0.3442 304	0.0183 724	0.0533 724	0.3410 877	0.0181 178	0.0531 178	0.3395 002	0.0179 902	0.0529 902
32	0.3325 897	0.0174 415	0.0524 415	0.3294 559	0.0171 964	0.0521 964	0.3278 732	0.0170 735	0.0520 735
33	0.3213 427	0.0165 724	0.0515 724	0.3182 207	0.0163 363	0.0513 363	0.3166 443	0.0162 178	0.0512 178
34	0.3104 761	0.0157 597	0.0507 597	0.3073 687	0.0155 319	0.0505 319	0.3058 000	0.0154 177	0.0504 177
35	0.2999 769	0.0149 983	0.0499 983	0.2968 867	0.0147 786	0.0497 786	0.2953 271	0.0146 684	0.0496 684
36	0.2898 327	0.0142 842	0.0492 842	0.2867 622	0.0140 720	0.0490 720	0.2852 129	0.0139 656	0.0489 656
37	0.2800 316	0.0136 132	0.0486 132	0.2769 830	0.0134 083	0.0484 083	0.2754 450	0.0133 055	0.0483 055
38	0.2705 620	0.0129 821	0.0479 821	0.2675 372	0.0127 840	0.0477 840	0.2660 117	0.0126 847	0.0476 847
39	0.2614 125	0.0123 878	0.0473 878	0.2584 136	0.0121 961	0.0471 961	0.2569 015	0.0121 001	0.0471 001
40	0.2525 725	0.0118 273	0.0468 273	0.2496 011	0.0116 419	0.0466 419	0.2481 032	0.0115 489	0.0465 489
41	0.2440 314	0.0112 982	0.0462 982	0.2410 892	0.0111 187	0.0461 187	0.2396 063	0.0110 288	0.0460 288
42	0.2357 791	0.0107 983	0.0457 983	0.2328 675	0.0106 245	0.0456 245	0.2314 003	0.0105 374	0.0455 374
43	0.2278 059	0.0103 254	0.0453 254	0.2249 262	0.0101 570	0.0451 570	0.2234 754	0.0100 726	0.0450 726
44	0.2201 023	0.0098 777	0.0448 777	0.2172 557	0.0097 145	0.0447 145	0.2158 219	0.0096 327	0.0446 327
45	0.2126 592	0.0094 534	0.0444 534	0.2098 468	0.0092 952	0.0442 952	0.2084 306	0.0092 160	0.0442 160
46	0.2054 679	0.0090 511	0.0440 511	0.2026 906	0.0088 976	0.0438 976	0.2012 923	0.0088 208	0.0438 208
47	0.1985 196	0.0086 692	0.0436 692	0.1957 784	0.0085 203	0.0435 203	0.1943 985	0.0084 458	0.0434 458
48	0.1918 065	0.0083 065	0.0433 065	0.1891 019	0.0081 620	0.0431 620	0.1877 409	0.0080 897	0.0430 897
49	0.1853 202	0.0079 617	0.0429 617	0.1826 531	0.0078 215	0.0428 215	0.1813 112	0.0077 513	0.0427 513
50	0.1790 534	0.0076 337	0.0426 337	0.1764 242	0.0074 976	0.0424 976	0.1751 018	0.0074 295	0.0424 295
51	0.1729 984	0.0073 216	0.0423 216	0.1704 078	0.0071 894	0.0421 894	0.1691 049	0.0071 232	0.0421 232
52	0.1671 482	0.0070 243	0.0420 243	0.1645 965	0.0068 959	0.0418 959	0.1633 135	0.0068 317	0.0418 317
53	0.1614 959	0.0067 410	0.0417 410	0.1589 834	0.0066 163	0.0416 163	0.1577 204	0.0065 539	0.0415 539
54	0.1560 347	0.0064 709	0.0414 709	0.1535 617	0.0063 497	0.0413 497	0.1523 189	0.0062 891	0.0412 891
55	0.1507 581	0.0062 132	0.0412 132	0.1483 249	0.0060 955	0.0410 955	0.1471 023	0.0060 366	0.0410 366
56	0.1456 600	0.0059 673	0.0409 673	0.1432 667	0.0058 528	0.0408 528	0.1420 644	0.0057 956	0.0407 956
57	0.1407 343	0.0057 325	0.0407 325	0.1383 810	0.0056 212	0.0406 212	0.1371 991	0.0055 656	0.0405 656
58	0.1359 752	0.0055 081	0.0405 081	0.1336 619	0.0053 999	0.0403 999	0.1325 003	0.0053 458	0.0403 458
59	0.1313 770	0.0052 937	0.0402 937	0.1291 037	0.0051 885	0.0401 885	0.1279 625	0.0051 359	0.0401 359
60	0.1269 343	0.0050 886	0.0400 886	0.1247 010	0.0049 863	0.0399 863	0.1235 801	0.0049 352	0.0399 352
61	0.1226 418	0.0048 925	0.0398 925	0.1204 484	0.0047 930	0.0397 930	0.1193 478	0.0047 433	0.0397 433
62	0.1184 945	0.0047 048	0.0397 048	0.1163 408	0.0046 080	0.0396 080	0.1152 604	0.0045 597	0.0395 597
63	0.1144 875	0.0045 251	0.0395 251	0.1123 733	0.0044 310	0.0394 310	0.1113 130	0.0043 839	0.0393 839
64	0.1106 159	0.0043 531	0.0393 531	0.1085 412	0.0042 615	0.0392 615	0.1075 008	0.0042 157	0.0392 157
65	0.1068 753	0.0041 883	0.0391 883	0.1048 397	0.0040 991	0.0390 991	0.1038 192	0.0040 546	0.0390 546
66	0.1032 611	0.0040 303	0.0390 303	0.1012 644	0.0039 436	0.0389 436	0.1002 636	0.0039 003	0.0389 003
67	0.0997 692	0.0038 789	0.0388 789	0.0978 111	0.0037 945	0.0387 945	0.0968 299	0.0037 524	0.0387 524
68	0.0963 954	0.0037 338	0.0387 338	0.0944 755	0.0036 516	0.0386 516	0.0935 137	0.0036 106	0.0386 106
69	0.0931 356	0.0035 945	0.0385 945	0.0912 537	0.0035 146	0.0385 146	0.0903 110	0.0034 747	0.0384 747
70	0.0899 861	0.0034 610	0.0384 610	0.0881 417	0.0033 832	0.0383 832	0.0872 181	0.0033 443	0.0383 443
71	0.0869 431	0.0033 328	0.0383 328	0.0851 359	0.0032 570	0.0382 570	0.0842 311	0.0032 192	0.0382 192
72	0.0840 030	0.0032 097	0.0382 097	0.0822 326	0.0031 360	0.0381 360	0.0813 464	0.0030 992	0.0380 992
73	0.0811 623	0.0030 916	0.0380 916	0.0794 282	0.0030 198	0.0380 198	0.0785 605	0.0029 840	0.0379 840
74	0.0784 177	0.0029 782	0.0379 782	0.0767 196	0.0029 083	0.0379 083	0.0758 700	0.0028 735	0.0378 735
75	0.0757 659	0.0028 692	0.0378 692	0.0741 033	0.0028 012	0.0378 012	0.0732 716	0.0027 673	0.0377 673
76	0.0732 038	0.0027 645	0.0377 645	0.0715 762	0.0026 983	0.0376 983	0.0707 622	0.0026 653	0.0376 653
77	0.0707 283	0.0026 639	0.0376 639	0.0691 353	0.0025 994	0.0375 994	0.0683 388	0.0025 673	0.0375 673
78	0.0683 365	0.0025 672	0.0375 672	0.0667 776	0.0025 045	0.0375 045	0.0659 983	0.0024 732	0.0374 732
79	0.0660 256	0.0024 743	0.0374 743	0.0645 003	0.0024 132	0.0374 132	0.0637 381	0.0023 827	0.0373 827
80	0.0637 929	0.0023 849	0.0373 849	0.0623 007	0.0023 254	0.0373 254	0.0615 552	0.0022 957	0.0372 957
81	0.0616 356	0.0022 989	0.0372 989	0.0601 761	0.0022 410	0.0372 410	0.0594 471	0.0022 122	0.0372 122
82	0.0595 513	0.0022 163	0.0372 163	0.0581 240	0.0021 599	0.0371 599	0.0574 112	0.0021 318	0.0371 318
83	0.0575 375	0.0021 368	0.0371 368	0.0561 418	0.0020 818	0.0370 818	0.0554 450	0.0020 545	0.0370 545
84	0.0555 918	0.0020 602	0.0370 602	0.0542 273	0.0020 068	0.0370 068	0.0535 461	0.0019 801	0.0369 801
85	0.0537 119	0.0019 866	0.0369 866	0.0523 780	0.0019 346	0.0369 346	0.0517 123	0.0019 086	0.0369 086
86	0.0518 955	0.0019 158	0.0369 158	0.0505 918	0.0018 651	0.0368 651	0.0499 413	0.0018 398	0.0368 398
87	0.0501 406	0.0018 476	0.0368 476	0.0488 665	0.0017 982	0.0367 982	0.0482 309	0.0017 736	0.0367 736
88	0.0484 450	0.0017 819	0.0367 819	0.0472 000	0.0017 338	0.0367 338	0 0465 791	0.0017 099	0 0367 099
89	0.0468 068	0.0017 187	0.0367 187	0.0455 904	0.0016 719	0.0366 719	0.0449 839	0.0016 486	0.0366 486
90	0.0452 240	0.0016 578	0.0366 578	0.0440 357	0.0016 122	0.0366 122	0.0434 433	0 0015 896	0.0365 896
91	0.0436 946	0.0015 992	0.0365 992	0.0425 340	0.0015 548	0.0365 548	0.0419 555	0.0015 327	0.0365 327
92	0.0422 170	0.0015 427	0.0365 427	0.0410 835	0.0014 995	0.0364 995	0.0405 186	0.0014 780	0.0364 780
93	0.0407 894	0.0014 883	0.0364 883	0.0396 824	0.0014 463	0.0364 463	0.0391 309	0.0014 254	0.0364 254
94	0.0394 101	0.0014 359	0.0364 359	0.0383 292	0.0013 950	0.0363 950	0.0377 908	0.0013 746	0.0363 746
95	0.0380 774	0.0013 855	0.0363 855	0.0370 221	0.0013 456	0.0363 456	0.0364 966	0.0013 258	0.0363 258
96	0 0367 897	0.0013 368	0.0363 368	0.0357 595	0.0012 980	0.0362 980	0.0352 466	0.0012 787	0.0362 787
97	0.0355 456	0.0012 899	0.0362 899	0.0345 400	0.0012 522	0.0362 522	0.0340 395	0.0012 334	0.0362 334
98	0.0343 436	0.0012 448	0.0362 448	0.0333 622	0.0012 080	0.0362 080	0.0328 738	0.0011 897	0.0361 897
99	0.0331 822	0.0012 012	0.0362 012	0.0322 244	0.0011 654	0.0361 654	0.0317 479	0.0011 476	0.0361 476
100	0.0320 601	0.0011 593	0.0361 593	0.0311 253	0.0011 244	0.0361 244	0.0306 606	0.0011 071	0.0361 071
	Ratio of Perpetual Ann.		0.0350 000	- - - - - - - - - - - -		0.0350 000	- - - - - - - - - - - -		0.0350 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0375.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.01875.			RATIO *of* INTEREST: *QUARTERLY*, 0.009375.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
0	....	....	....	....	....	....	1.0093 750	0.2500 000	0.2476 78
¼	....	....	....	1.0187 500	0.5000 000	0.4907 98	1.0188 379	0.5023 438	0.4930 56
½	....	....	....	....	....	....	1.0283 895	0.7570 532	0.7361 54
¾	....	....	....	....	....	....	1.0380 306	1.0141 506	0.9769 95
1	1.0375 000	1.0000 000	0.9638 55	1.0378 516	1.0093 750	0.9725 62	....	....	....
¼	....	....	....	....	....	....	1.0477 622	1.2736 583	1.2155 99
½	....	....	....	1.0573 113	1.5283 008	1.4454 60	1.0575 850	1.5355 988	1.4519 86
¾	....	....	....	....	....	....	1.0674 998	1.7999 950	1.6361 78
2	1.0764 063	2.0375 000	1.8928 73	1.0771 359	2.0569 564	1.9096 54	1.0775 076	2.0668 700	1.9181 95
¼	....	....	....	....	....	....	1.0876 093	2.3362 469	2.1480 57
½	....	....	....	1.0973 322	2.5955 244	2.3653 04	1.0978 056	2.6081 492	2.3757 84
¾	....	....	....	....	....	....	1.1080 975	2.8826 006	2.6013 96
3	1.1167 715	3.1139 063	2.7833 11	1.1179 071	3.1441 904	2.8125 69	1.1184 859	3.1596 250	2.8249 13
¼	....	....	....	....	....	....	1.1289 717	3.4392 465	3.0463 53
½	....	....	....	1.1388 679	3.7031 440	3.2516 01	1.1395 559	3.7214 894	3.2657 37
¾	....	....	....	....	....	....	1.1502 392	4.0063 784	3.4830 83
4	1.1586 504	4.2306 777	3.6513 84	1.1602 217	4.2725 780	3.6825 53	1.1610 227	4.2939 382	3.6984 10
¼	....	....	....	....	....	....	1.1719 073	4.5841 938	3.9117 38
½	....	....	....	1.1819 758	4.8526 888	4.1055 74	1.1828 939	4.8771 707	4.1230 84
¾	....	....	....	....	....	....	1.1939 835	5.1728 941	4.3324 67
5	1.2020 998	5.3893 281	4.4832 62	1.2041 379	5.4436 767	4.5208 09	1.2051 771	5.4713 900	4.5399 05
¼	....	....	....	....	....	....	1.2164 757	5.7726 843	4.7454 17
½	....	....	....	1.2267 155	6.0457 456	4.9284 01	1.2278 801	6.0768 032	4.9490 20
¾	....	....	....	....	....	....	1.2393 915	6.3837 733	5.1507 32
6	1.2471 785	6.5914 280	5.2850 72	1.2497 164	6.6591 034	5.3284 92	1.2510 108	6.6936 211	5.3505 70
¼	....	....	....	....	....	....	1.2627 390	7.0063 738	5.5485 53
½	....	....	....	1.2731 486	7.2839 616	5.7212 19	1.2745 772	7.3220 586	5.7446 96
¾	....	....	....	....	....	....	1.2865 264	7.6407 029	5.9390 18
7	1.2939 477	7.8386 065	6.0579 00	1.2970 201	7.9205 358	6.1067 18	1.2985 875	7.9623 345	6.1315 35
¼	....	....	....	....	....	....	1.3107 618	8.2869 814	6.3222 63
½	....	....	....	1.3213 392	8.5690 459	6.4851 22	1.3230 502	8.6146 718	6.5112 21
¾	....	....	....	....	....	....	1.3354 538	8.9454 344	6.6984 23
8	1.3424 708	9.1325 542	6.8027 96	1.3461 143	9.2297 155	6.8565 61	1.3479 737	9.2792 978	6.8838 87
¼	....	....	....	....	....	....	1.3606 109	9.6162 912	7.0676 28
½	....	....	....	1.3713 540	9.9027 727	7.2211 65	1.3733 666	9.9564 439	7.2496 62
¾	....	....	....	....	....	....	1.3862 420	10.299 786	7.4300 06
9	1.3928 134	10.475 025	7.5207 67	1.3970 669	10.588 450	7.5790 57	1.3992 380	10.646 346	7.6086 74
¼	....	....	....	....	....	....	1.4123 558	10.996 156	7.7856 84
½	....	....	....	1.4232 619	11.286 983	7.9303 63	1.4255 967	11.349 245	7.9610 49
¾	....	....	....	....	....	....	1.4389 616	11.705 644	8.1347 85
10	1.4450 439	11.867 838	8.2127 87	1.4499 480	11.998 614	8.2752 03	1.4524 519	12.065 384	8.3069 03
¼	....	....	....	....	....	....	1.4660 686	12.428 497	8.4774 32
½	....	....	....	1.4771 346	12.723 588	8.6136 96	1.4798 130	12.795 014	8.6463 72
¾	....	....	....	....	....	....	1.4936 863	13.164 968	8.8137 43
11	1.4992 331	13.312 882	8.8797 95	1.5048 308	13.462 155	8.9459 59	1.5076 896	13.538 389	8.9795 60
¼	....	....	....	....	....	....	1.5218 242	13.915 311	9.1438 37
½	....	....	....	1.5330 464	14.214 571	9.2721 07	1.5360 913	14.295 768	9.3065 87
¾	....	....	....	....	....	....	1.5504 921	14.679 790	9.4678 26
12	1.5554 543	14.812 116	9.5226 94	1.5617 910	14.981 094	9.5922 53	1.5650 280	15.067 413	9.6275 68
¼	....	....	....	....	....	....	1.5797 001	15.458 670	9.7858 26
½	....	....	....	1.5910 746	15.761 989	9.9065 06	1.5945 098	15.853 595	9.9426 14
¾	....	....	....	....	....	....	1.6094 594	16.252 223	10.097 95
13	1.6137 839	16.367 570	10.142 36	1.6209 073	16.557 527	10.214 97	1.6245 470	16.654 587	10.251 83
¼	....	....	....	....	....	....	1.6397 772	17.060 724	10.404 29
½	....	....	....	1.6512 993	17.367 980	10.517 77	1.6551 501	17.470 669	10.555 34
¾	....	....	....	....	....	....	1.6706 671	17.884 456	10.704 98
14	1.6743 008	17.981 354	10.739 62	1.6822 611	18.193 630	10.814 99	1.6863 296	18.302 123	10.853 23
¼	....	....	....	....	....	....	1.7021 389	18.723 705	11.000 10
½	....	....	....	1.7138 035	19.034 761	11.106 73	1.7180 965	19.149 240	11.145 61
¾	....	....	....	....	....	....	1.7342 037	19.578 764	11.289 77
15	1.7370 870	19.655 654	11.315 30	1.7459 373	19.891 662	11.393 11	1.7504 618	20.012 315	11.432 59
¼	....	....	....	....	....	....	1.7668 724	20.449 930	11.574 08
½	....	....	....	1.7786 737	20.764 631	11.674 22	1.7834 368	20.891 649	11.714 26
¾	....	....	....	....	....	....	1.8001 565	21.337 508	11.853 14
16	1.8022 278	21.392 742	11.870 17	1.8120 238	21.653 968	11.950 16	1.8170 330	21.787 547	11.990 73
17	1.8698 113	23.194 969	12.404 98	1.8806 117	23.482 979	12.486 88	1.8861 359	23.630 292	12.528 41
18	1.9399 293	25.064 781	12.920 46	1.9517 958	25.381 222	13.004 03	1.9578 669	25.543 118	13.046 40
19	2.0126 766	27.004 710	13.417 31	2.0256 743	27.351 316	13.502 32	2.0323 259	27.528 690	13.545 41
20	2.0881 520	29.017 387	13.896 20	2.1023 493	29.395 981	13.982 44	2.1095 165	29.589 774	14.026 14
21	2.1664 577	31.105 539	14.357 79	2.1819 265	31.518 040	14.445 05	2.1898 466	31.729 243	14.489 25
22	2.2476 999	33.271 996	14.802 69	2.2645 158	33.720 422	14.890 79	2.2731 279	33.950 077	14.935 40
23	2.3319 886	35.519 696	15.231 51	2.3502 313	36.006 167	15.320 26	2.3595 764	36.255 371	15.365 20
24	2.4194 382	37.851 685	15.644 82	2.4391 912	38.378 432	15.734 08	2.4493 126	38.648 337	15.779 26
25	2.5101 671	40.271 123	16.043 20	2.5315 184	40.840 491	16.132 80	2.5424 616	41.132 309	16.178 14

Years.	RATIO of INTEREST: ANNUALLY, 0.0375.			RATIO of INTEREST: HALF-YEARLY, 0.01875.			RATIO of INTEREST: QUARTERLY, 0.009375.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
½	....	....	....	....	....	....	0.9907 121	4.0000 000	4.0375 000
	....	....	....	0.9815 951	2.0000 000	2.0375 000	0.9815 104	1.9906 687	2.0281 687
	....	....	....	....	....	....	0.9723 942	1.3209 111	1.3584 111
1	0.9638 554	1.0000 000	1.0375 000	0.9635 291	0.9907 121	1.0282 121	0.9633 627	0.9860 469	1.0235 469
	....	....	....	....	....	....	0.9544 151	0.7851 598	0.8226 598
	....	....	....	0.9457 953	0.6543 215	0.6918 215	0.9455 505	0.6512 118	0.6887 118
	....	....	....	....	....	....	0.9367 683	0.5555 571	0.5930 571
2	0.9290 173	0.4907 976	0.5282 976	0.9283 880	0.4861 547	0.5236 547	0.9280 677	0.4838 234	0.5213 234
	....	....	....	....	....	....	0.9194 479	0.4280 369	0.4655 369
	....	....	....	0.9113 011	0.3852 786	0.4227 786	0.9109 081	0.3834 137	0.4209 137
	....	....	....	....	....	....	0.9024 477	0.3469 090	0.3844 090
3	0.8954 384	0.3211 400	0.3586 400	0.8945 286	0.3180 469	0.3555 469	0.8940 658	0.3164 932	0.3539 932
	....	....	....	....	....	....	0.8857 617	0.2907 614	0.3282 614
	....	....	....	0.8780 650	0.2700 408	0.3075 408	0.8775 349	0.2687 096	0.3062 096
	....	....	....	....	....	....	0.8693 844	0.2496 020	0.2871 020
4	0.8630 731	0.2363 687	0.2738 687	0.8619 043	0.2340 508	0.2715 508	0.8613 097	0.2323 865	0.2703 865
	....	....	....	....	....	....	0.8533 099	0.2181 409	0.2556 409
	....	....	....	0.8460 410	0.2060 713	0.2435 713	0.8453 844	0.2050 369	0.2425 369
	....	....	....	....	....	....	0.8375 325	0.1933 154	0.2308 154
5	0.8318 777	0.1855 519	0.2230 519	0.8304 697	0.1836 994	0.2211 994	0.8297 535	0.1827 689	0.2202 689
	....	....	....	....	....	....	0.8220 469	0.1732 296	0.2107 296
	....	....	....	0.8151 850	0.1654 056	0.2029 056	0.8144 118	0.1645 602	0.2020 602
	....	....	....	....	....	....	0.8068 475	0.1566 472	0.1941 472
6	0.8018 098	0.1517 122	0.1892 122	0.8001 816	0.1501 704	0.1876 704	0.7993 530	0.1493 960	0.1868 960
	....	....	....	....	....	....	0.7919 293	0.1427 272	0.1802 272
	....	....	....	0.7854 543	0.1372 879	0.1747 879	0.7845 739	0.1365 736	0.1740 736
	....	....	....	....	....	....	0.7772 868	0.1308 780	0.1683 780
7	0.7728 287	0.1275 737	0.1650 737	0.7709 981	0.1262 541	0.1637 541	0.7700 675	0.1255 913	0.1630 913
	....	....	....	....	....	....	0.7629 151	0.1206 712	0.1581 712
	....	....	....	0.7568 079	0.1166 991	0.1541 991	0.7558 292	0.1160 810	0.1535 810
	....	....	....	....	....	....	0.7488 092	0.1117 889	0.1492 889
8	0.7448 952	0.1094 984	0.1469 984	0.7428 789	0.1083 457	0.1458 457	0.7418 542	0.1077 668	0.1452 668
	....	....	....	....	....	....	0.7349 640	0.1039 902	0.1414 902
	....	....	....	0.7292 063	0.1009 818	0.1384 818	0.7281 376	0.1004 375	0.1379 375
	....	....	....	....	....	....	0.7213 748	0.0970 894	0.1345 894
9	0.7179 713	0.0954 652	0.1329 652	0.7157 853	0.0944 425	0.1319 425	0.7146 747	0.0939 289	0.1314 289
	....	....	....	....	....	....	0.7080 369	0.0909 409	0.1284 409
	....	....	....	0.7026 114	0.0885 976	0.1260 976	0.7014 607	0.0881 116	0.1256 116
	....	....	....	....	....	....	0.6949 455	0.0854 289	0.1229 289
10	0.6920 205	0.0842 614	0.1217 614	0.6896 799	0.0833 430	0.1208 430	0.6884 910	0.0828 817	0.1203 817
	....	....	....	....	....	....	0.6820 963	0.0804 603	0.1179 603
	....	....	....	0.6769 864	0.0785 942	0.1160 942	0.6757 610	0.0781 554	0.1156 554
	....	....	....	....	....	....	0.6694 846	0.0759 592	0.1134 592
11	0.6670 077	0.0751 152	0.1126 152	0.6645 265	0.0742 823	0.1117 823	0.6632 665	0.0738 640	0.1113 640
	....	....	....	....	....	....	0.6571 061	0.0718 633	0.1093 633
	....	....	....	0.6522 960	0.0703 503	0.1078 503	0.6510 030	0.0699 508	0.1074 503
	....	....	....	....	....	....	0.6449 565	0.0681 209	0.1056 209
12	0.6428 990	0.0675 123	0.1050 123	0.6402 905	0.0667 508	0.1042 508	0.6389 662	0.0663 684	0.1038 684
	....	....	....	....	....	....	0.6330 315	0.0646 886	0.1021 886
	....	....	....	0.6285 060	0.0634 438	0.1009 438	0.6271 520	0.0630 772	0.1005 772
	....	....	....	....	....	....	0.6213 271	0.0615 300	0.0990 300
13	0.6196 616	0.0610 964	0.0985 964	0.6169 385	0.0603 955	0.0978 955	0.6155 562	0.0600 435	0.0975 435
	....	....	....	....	....	....	0.6098 390	0.0586 141	0.0961 141
	....	....	....	0.6055 837	0.0575 772	0.0950 772	0.6041 748	0.0572 388	0.0947 388
	....	....	....	....	....	....	0.5985 633	0.0559 145	0.0934 145
14	0.5972 642	0.0556 132	0.0931 132	0.5944 381	0.0549 643	0.0924 643	0.5930 039	0.0546 385	0.0921 385
	....	....	....	....	....	....	0.5874 961	0.0534 082	0.0909 082
	....	....	....	0.5834 974	0.0525 355	0.0900 355	0.5820 395	0.0522 214	0.0897 214
	....	....	....	....	....	....	0.5766 335	0.0510 757	0.0885 757
15	0.5756 764	0.0508 759	0.0883 759	0.5727 582	0.0502 723	0.0877 723	0.5712 778	0.0499 692	0.0874 692
	....	....	....	....	....	....	0.5659 718	0.0488 999	0.0863 999
	....	....	....	0.5622 167	0.0481 588	0.0856 588	0.5607 151	0.0478 660	0.0853 660
	....	....	....	....	....	....	0.5555 072	0.0468 658	0.0843 658
16	0.5548 688	0.0467 448	0.0842 448	0.5518 691	0.0461 809	0.0836 809	0.5503 477	0.0458 978	0.0833 978
17	0.5348 133	0.0431 128	0.0806 128	0.5317 419	0.0425 840	0.0800 840	0.5301 845	0.0423 186	0.0798 186
18	0.5154 827	0.0398 966	0.0773 966	0.5123 487	0.0393 992	0.0768 992	0.5107 599	0.0391 495	0.0766 495
19	0.4968 508	0.0370 306	0.0745 306	0.4936 628	0.0365 613	0.0740 613	0.4920 471	0.0363 257	0.0738 257
20	0.4788 923	0.0344 621	0.0719 621	0.4756 584	0.0340 183	0.0715 183	0.4740 198	0.0337 955	0.0712 955
21	0.4615 829	0.0321 486	0.0696 486	0.4583 106	0.0317 279	0.0692 279	0.4566 529	0.0315 167	0.0690 167
22	0.4448 993	0.0300 553	0.0675 553	0.4415 955	0.0296 556	0.0671 556	0.4399 225	0.0294 550	0.0669 550
23	0.4288 186	0.0281 534	0.0656 534	0.4254 900	0.0277 730	0.0652 730	0.4238 049	0.0275 821	0.0650 821
24	0.4133 191	0.0264 189	0.0639 189	0.4099 720	0.0260 563	0.0635 563	0.4082 778	0.0258 743	0.0633 743
25	0.3983 799	0.0248 317	0.0623 317	0.3950 198	0.0244 855	0.0619 855	0.3933 196	0.0243 118	0.0618 118

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0375.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.01875.			RATIO *of* INTEREST: *QUARTERLY*, 0.009375.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	2.6042 984	42.781 290	16.427 18	2.6273 403	43.395 742	16.516 98	2.6391 531	43.710 748	16.562 41
27	2.7019 596	45.385 588	16.797 29	2.7267 893	46.047 714	16.887 16	2.7395 218	46.387 247	16.932 61
28	2.8032 830	48.087 548	17.154 01	2.8300 025	48.800 066	17.243 82	2.8437 075	49.165 534	17.289 24
29	2.9084 062	50.890 831	17.497 84	2.9371 225	51.656 600	17.587 49	2.9518 556	52.049 482	17.632 80
30	3.0174 714	53.799 237	17.829 24	3.0482 972	54.621 258	17.918 61	3.0641 166	55.043 108	17.963 78
31	3.1306 266	56.816 709	18.148 67	3.1636 800	57.698 133	18.237 66	3.1806 469	58.150 584	18.282 63
32	3.2480 251	59.947 335	18.456 55	3.2834 302	60.891 473	18.545 08	3.3016 090	61.376 239	18.589 80
33	3.3698 260	63.195 360	18 753 30	3.4077 132	64.205 685	18.841 28	3.4271 713	64.724 567	18.885 71
34	3.4961 945	66.565 186	19.039 33	3 5367 005	67.645 346	19.126 68	3.5575 088	68.200 235	19.170 78
35	3.6273 018	70.061 381	19.315 01	3.6705 701	71.215 203	19.401 67	3.6928 032	71.808 085	19.445 41
36	3.7633 256	73.688 682	19.580 73	3 8095 069	74.920 184	19.666 64	3.8332 429	75.553 143	19.709 98
37	3.9044 503	77.452 008	19.836 85	3.9537 027	78.765 405	19.921 94	3.9790 236	79.440 629	19.964 86
38	4.0508 672	81.356 458	20.083 71	4.1033 565	82.756 174	20.167 92	4.1303 484	83.475 958	20.210 39
39	4.2027 747	85 407 326	20.321 65	4.2586 750	86.898 000	20.404 94	4.2874 283	87.664 753	20.446 93
40	4.3603 788	89.610 100	20.550 99	4.4198 725	91.196 600	20.633 31	4.4504 819	92.012 851	20.674 81
41	4.5238 930	93.970 479	20.772 04	4.5871 716	95.657 908	20.853 35	4.6197 366	96.526 310	20.894 33
42	4.6935 389	98.494 372	20.985 10	4.7608 032	100.28 808	21.065 37	4.7954 282	101.21 142	21.105 82
43	4.8695 467	103.18 791	21.190 46	4 9410 070	105.09 352	21.269 66	4.9778 015	106.07 471	21.309 55
44	5.0521 547	108.05 746	21.388 39	5.1280 318	110 08 085	21.466 49	5.1671 105	111.12 295	21.505 82
45	5.2416 105	113.10 961	21.579 17	5.3221 359	115.25 696	21.656 15	5.3636 190	116.36 317	21.694 90
46	5.4381 709	118.35 122	21.763 06	5.5235 870	120.62 899	21.838 89	5.5676 009	121.80 269	21.877 05
47	5.6421 023	123.78 939	21.940 30	5.7326 634	126.20 436	22 014 96	5.7793 404	127.44 908	22.052 51
48	5.8536 811	129.43 150	22.111 13	5.9496 537	131.99 077	22.184 61	5.9991 324	133.31 020	22.221 58
49	6.0731 941	135.28 518	22.275 79	6.1748 574	137.99 620	22.348 08	6.2272 833	139.39 422	22.384 44
50	6.3009 389	141.35 837	22.434 49	6.4085 854	144.22 894	22.505 58	6.4641 110	145.70 963	22.541 33
51	6.5372 241	147.65 931	22.587 46	6.6511 604	150.69 761	22.657 34	6.7099 453	152.26 521	22.692 46
52	6.7823 700	154.19 653	22.734 90	6.9029 172	157.41 112	22.803 56	6.9651 288	159.07 010	22.838 07
53	7.0367 089	160.97 890	22.877 02	7.1642 034	164.37 876	22.944 46	7.2300 172	166.13 379	22.978 34
54	7.3005 855	168.01 561	23.013 99	7.4353 797	171.61 012	23.080 21	7.5049 794	173.46 612	23.113 47
55	7.5743 574	175.31 620	23.146 02	7.7168 204	179.11 521	23.211 01	7.7903 987	181.07 730	23.243 65
56	7.8583 958	182.89 056	23.273 27	8.0089 141	186.90 438	23 337 04	8.0866 726	188.97 794	23.369 06
57	8.1530 857	190.74 895	23.395 92	8.3120 640	194.98 837	23.458 48	8.3942 140	197.17 904	23.489 88
58	8.4588 264	198.90 204	23.514 14	8.6266 886	203.37 836	23.575 48	8.7134 513	205.69 204	23.606 27
59	8.7760 324	207.36 086	23.628 09	8.9532 223	212.08 593	23.688 22	9.0448 295	214.52 879	23.718 39
60	9.1051 336	216.13 690	23.737 92	9.2921 157	221.12 309	23.796 85	9.3888 103	223.70 161	23.826 41
61	9.4465 761	225.24 203	23.843 77	9.6438 368	230.50 232	23.901 52	9.7458 728	233.22 327	23.930 47
62	9.8008 227	234.68 861	23.945 81	10.008 871	240.23 656	24.002 36	10.116 515	243.10 706	24.030 71
63	10.168 354	244.48 943	24.044 15	10.387 723	250.33 927	24.099 53	10.501 252	253.36 673	24.127 29
64	10.549 667	254.65 778	24.138 94	10.780 914	260.82 437	24.193 16	10.900 622	264.01 658	24.220 32
65	10.945 279	265.20 745	24.230 30	11.183 988	271.70 636	24.283 37	11.315 179	275.07 145	24.309 95
66	11.355 727	276.15 273	24.318 37	11.612 509	283.00 025	24.370 29	11.745 503	286.54 675	24.396 30
67	11.781 567	287.50 846	24.403 24	12.052 061	294.72 162	24.454 04	12.192 192	298.45 845	24.479 47
68	12.223 376	299.29 002	24.485 05	12.508 250	306.88 667	24.534 74	12.655 869	310.82 317	24.559 61
69	12.681 752	311.51 340	24.563 91	12.981 707	319.51 219	24.612 49	13.137 180	323.65 813	24.636 80
70	13.157 318	324.19 515	24 639 91	13.473 085	332.61 560	24.687 41	13.636 795	336.98 121	24.711 17
71	13.650 718	337.35 247	24.713 17	13.983 062	346.21 499	24.759 60	14.155 412	350.81 097	24.782 82
72	14.162 620	351.00 319	24.783 78	14.512 343	360.32 914	24.829 15	14.693 751	365.16 669	24.851 84
73	14.693 718	365.16 581	24.851 83	15.061 658	374.97 754	24.896 17	15.252 564	380.06 837	24.918 33
74	15.244 732	379.85 952	24.917 43	15.631 765	390.18 040	24.960 74	15.832 629	395.53 677	24.982 38
75	15.816 410	395.10 426	24.980 65	16.223 452	405.95 871	25.022 95	16.434 754	411.59 344	25.044 09
76	16.409 525	410.92 067	25.041 59	16.837 535	422.33 426	25.082 90	17.059 778	428.26 075	25.103 54
77	17.024 882	427.33 019	25.100 33	17.474 862	439.32 965	25.140 67	17.708 573	445.56 194	25.160 80
78	17.663 315	444.35 507	25.156 95	18.136 313	456.96 834	25.196 32	18.382 041	463.52 109	25.215 98
79	18.325 690	462.01 839	25.211 51	18.822 800	475.27 468	25.249 94	19.081 122	482.16 325	25.269 12
80	19.012 903	480.34 408	25.264 11	19.535 273	494.27 394	25.301 62	19.806 789	501.51 438	25.320 33
81	19.725 887	499.35 698	25.314 81	20.274 713	513.99 236	25.351 40	20.560 054	521.60 145	25.369 65
82	20.465 608	519.08 287	25.363 67	21.042 143	534.45 715	25.399 37	21.341 967	542.45 244	25.417 17
83	21.233 068	539.54 848	25.410 76	21.838 621	555.69 656	25.445 59	22.153 615	564.09 641	25.462 95
84	22.029 308	560.78 154	25.456 16	22.665 247	577.73 992	25.490 12	22.996 132	586.56 351	25.507 05
85	22.855 407	582.81 085	25.499 91	23.523 162	600.61 765	25.533 04	23.870 690	609.88 505	25.549 54
86	23.712 485	605.66 626	25.542 08	24.413 550	624.36 134	25.574 38	24.778 507	634.09 353	25.590 47
87	24.601 703	629.37 874	25.582 73	25.337 641	649.00 377	25.614 21	25.720 850	659 22 267	25.629 89
88	25.524 267	653.98 045	25.621 91	26.296 711	674.57 895	25.652 60	26.699 031	685.30 748	25.667 88
89	26.481 427	679.50 471	25.659 67	27.292 082	701.12 219	25.689 58	27.714 412	712.38 432	25.704 47
90	27.474 480	705.98 614	25.696 07	28.325 131	728.67 014	25.725 22	28.768 409	740.49 091	25.739 73
91	28.504 773	733.46 062	25.731 15	29.397 281	757.26 082	25.759 55	29.862 490	769.66 640	25.773 68
92	29.573 702	761.96 539	25.764 96	30.510 014	786.93 370	25.792 64	30.998 180	799.95 147	25.806 40
93	30.682 716	791.53 909	25.797 56	31.664 865	817.72 974	25.824 52	32.177 061	831.38 829	25.837 92
94	31.833 318	822.22 181	25.828 97	32.863 430	849.69 147	25.855 23	33.400 775	864.02 068	25.868 28
95	33.027 067	854.05 513	25.859 25	34.107 362	882.86 299	25.884 82	34.671 028	897.89 409	25.897 53
96	34.265 582	887.08 220	25.888 43	35.398 379	917.29 011	25.913 34	35.989 590	933.05 574	25.925 71
97	35.550 542	921.34 778	25.916 56	36.738 263	953.02 035	25.940 81	37.358 297	969.55 460	25.952 86
98	36.883 687	956.89 832	25.943 67	38.128 864	990.10 303	25.967 26	38.779 058	1007.4 415	25.979 01
99	38.266 825	993.78 201	25.969 81	39.572 101	1028.5 894	25.992 79	40.253 850	1046.7 693	26.004 20
100	39.701 831	1032.0 488	25.994 99	41.069 967	1068.5 324	26.017 37	41.784 730	1087.5 928	26 028 48
	Value of Perpetual Ann.		26.666 67	- - - - - - - - -		26.666 67	- - - - - - - - -		26.666 67

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0375.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.01875.			RATIO *of* INTEREST: *QUARTERLY*, 0.009375.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.3839 806	0.0233 747	0.0608 747	0.3806 130	0.0230 438	0.0605 438	0.3789 094	0.0228 777	0.0603 777
27	0.3701 017	0.0220 334	0.0595 334	0.3667 317	0.0217 166	0.0592 166	0.3650 272	0.0215 577	0.0590 577
28	0.3567 246	0.0207 954	0.0582 954	0.3533 566	0.0204 918	0.0579 918	0.3516 536	0.0203 395	0.0578 395
29	0.3438 309	0.0196 499	0.0571 499	0.3404 693	0.0193 586	0.0568 586	0.3387 700	0.0192 125	0.0567 125
30	0.3314 033	0.0185 876	0.0560 876	0.3280 520	0.0183 079	0.0558 079	0.3263 584	0.0181 676	0.0556 676
31	0.3194 249	0.0176 005	0.0551 005	0.3160 876	0.0173 316	0.0548 316	0.3144 015	0.0171 967	0.0546 967
32	0.3078 794	0.0166 813	0.0541 813	0.3045 595	0.0164 227	0.0539 227	0.3028 826	0.0162 929	0.0537 929
33	0.2967 512	0.0158 239	0.0533 239	0.2934 519	0.0155 749	0.0530 749	0.2917 858	0.0154 501	0.0529 501
34	0.2860 253	0.0150 229	0.0525 229	0.2827 494	0.0147 830	0.0522 830	0.2810 956	0.0146 627	0.0521 627
35	0.2756 870	0.0142 732	0.0517 732	0.2724 372	0.0140 419	0.0515 419	0.2707 970	0.0139 259	0.0514 259
36	0.2657 224	0.0135 706	0.0510 706	0.2625 011	0.0133 475	0.0508 475	0.2608 757	0.0132 357	0.0507 357
37	0.2561 182	0.0129 112	0.0504 112	0.2529 275	0.0126 959	0.0501 959	0.2513 179	0.0125 880	0.0500 880
38	0.2468 607	0.0122 916	0.0497 916	0.2437 029	0.0120 837	0.0495 837	0.2421 103	0.0119 795	0.0494 795
39	0.2379 380	0.0117 086	0.0492 086	0.2348 148	0.0115 077	0.0490 077	0.2332 401	0.0114 071	0.0489 071
40	0.2293 379	0.0111 595	0.0486 595	0.2262 509	0.0109 653	0.0484 653	0.2246 948	0.0108 680	0.0483 680
41	0.2210 486	0.0106 416	0.0481 416	0.2179 993	0.0104 539	0.0479 539	0.2164 625	0.0103 599	0.0478 599
42	0.2130 589	0.0101 529	0.0476 529	0.2100 486	0.0099 713	0.0474 713	0.2085 320	0.0098 803	0.0473 803
43	0.2053 579	0.0096 911	0.0471 911	0.2023 879	0.0095 153	0.0470 153	0.2008 919	0.0094 273	0.0469 273
44	0.1979 354	0.0092 543	0.0467 543	0.1950 066	0.0090 842	0.0465 842	0.1935 318	0.0089 990	0.0464 990
45	0.1907 811	0.0088 410	0.0463 410	0.1878 945	0.0086 763	0.0461 763	0.1864 413	0.0085 938	0.0460 938
46	0.1838 854	0.0084 494	0.0459 494	0.1810 418	0.0082 899	0.0457 899	0.1796 106	0.0082 100	0.0457 100
47	0.1772 389	0.0080 782	0.0455 782	0.1744 390	0.0079 237	0.0454 237	0.1730 301	0.0078 463	0.0453 463
48	0.1708 327	0.0077 261	0.0452 261	0.1680 770	0.0075 763	0.0450 763	0.1666 908	0.0075 013	0.0450 013
49	0.1646 580	0.0073 918	0.0448 918	0.1619 471	0.0072 466	0.0447 466	0.1605 837	0.0071 739	0.0446 739
50	0.1587 065	0.0070 742	0.0445 742	0.1560 407	0.0069 334	0.0444 334	0.1547 003	0.0068 630	0.0443 630
51	0.1529 701	0.0067 723	0.0442 723	0.1503 497	0.0066 358	0.0441 358	0.1490 325	0.0065 675	0.0440 675
52	0.1474 411	0.0064 852	0.0439 852	0.1448 663	0.0063 528	0.0438 528	0.1435 724	0.0062 865	0.0437 865
53	0.1421 119	0.0062 120	0.0437 120	0.1395 829	0.0060 835	0.0435 835	0.1383 123	0.0060 192	0.0435 192
54	0.1369 753	0.0059 518	0.0434 518	0.1344 921	0.0058 272	0.0433 272	0.1332 449	0.0057 648	0.0432 648
55	0.1320 244	0.0057 040	0.0432 040	0.1295 871	0.0055 830	0.0430 830	0.1283 631	0.0055 225	0.0430 225
56	0.1272 524	0.0054 678	0.0429 678	0.1248 609	0.0053 503	0.0428 503	0.1236 603	0.0052 916	0.0427 916
57	0.1226 529	0.0052 425	0.0427 425	0.1203 071	0.0051 285	0.0426 285	0.1191 297	0.0050 715	0.0425 715
58	0.1182 197	0.0050 276	0.0425 276	0.1159 193	0.0049 169	0.0424 169	0.1147 651	0.0048 616	0.0423 616
59	0.1139 467	0.0048 225	0.0423 225	0.1116 916	0.0047 151	0.0422 151	0.1105 604	0.0046 614	0.0421 614
60	0.1098 282	0.0046 267	0.0421 267	0.1076 181	0.0045 224	0.0420 224	0.1065 098	0.0044 702	0.0419 702
61	0.1058 584	0.0044 397	0.0419 397	0.1036 932	0.0043 384	0.0418 384	0.1026 075	0.0042 877	0.0417 877
62	0.1020 322	0.0042 610	0.0417 610	0.0999 114	0.0041 626	0.0416 626	0.0988 433	0.0041 134	0.0416 134
63	0.0983 443	0.0040 902	0.0415 902	0.0962 675	0.0039 946	0.0414 946	0.0952 267	0.0039 468	0.0414 468
64	0.0947 897	0.0039 268	0.0414 268	0.0927 565	0.0038 340	0.0413 340	0.0917 379	0.0037 876	0.0412 876
65	0.0913 636	0.0037 706	0.0412 706	0.0893 736	0.0036 804	0.0411 804	0.0883 769	0.0036 354	0.0411 354
66	0.0880 613	0.0036 212	0.0411 212	0.0861 140	0.0035 336	0.0410 336	0.0851 390	0.0034 898	0.0409 898
67	0.0848 784	0.0034 782	0.0409 782	0.0829 734	0.0033 930	0.0408 930	0.0820 197	0.0033 506	0.0408 506
68	0.0818 105	0.0033 412	0.0408 412	0.0799 472	0.0032 585	0.0407 585	0.0790 147	0.0032 173	0.0407 173
69	0.0788 535	0.0032 101	0.0407 101	0.0770 315	0.0031 298	0.0406 298	0.0761 198	0.0030 897	0.0405 897
70	0.0760 033	0.0030 846	0.0405 846	0.0742 220	0.0030 065	0.0405 065	0.0733 310	0.0029 675	0.0404 675
71	0.0732 562	0.0029 643	0.0404 643	0.0715 151	0.0028 884	0.0403 884	0.0706 444	0.0028 505	0.0403 505
72	0.0706 084	0.0028 490	0.0403 490	0.0689 069	0.0027 752	0.0402 752	0.0680 561	0.0027 385	0.0402 385
73	0.0680 563	0.0027 385	0.0402 385	0.0663 938	0.0026 668	0.0401 668	0.0655 628	0.0026 311	0.0401 311
74	0.0655 964	0.0026 326	0.0401 326	0.0639 723	0.0025 629	0.0400 629	0.0631 607	0.0025 282	0.0400 282
75	0.0632 255	0.0025 310	0.0400 310	0.0616 392	0.0024 633	0.0399 633	0.0608 467	0.0024 296	0.0399 296
76	0.0609 402	0.0024 336	0.0399 336	0.0593 911	0.0023 678	0.0398 678	0.0586 174	0.0023 350	0.0398 350
77	0.0587 376	0.0023 401	0.0398 401	0.0572 251	0.0022 762	0.0397 762	0.0564 698	0.0022 444	0.0397 444
78	0.0566 145	0.0022 505	0.0397 505	0.0551 380	0.0021 883	0.0396 883	0.0544 009	0.0021 574	0.0396 574
79	0.0545 682	0.0021 644	0.0396 644	0.0531 271	0.0021 040	0.0396 040	0.0524 078	0.0020 740	0.0395 740
80	0.0525 959	0.0020 818	0.0395 818	0.0511 895	0.0020 232	0.0395 232	0.0504 877	0.0019 940	0.0394 940
81	0.0506 948	0.0020 026	0.0395 026	0.0493 225	0.0019 456	0.0394 456	0.0486 380	0.0019 172	0.0394 172
82	0.0488 625	0.0019 265	0.0394 265	0.0475 237	0.0018 711	0.0393 711	0.0468 560	0.0018 435	0.0393 435
83	0.0470 964	0.0018 534	0.0393 534	0.0457 904	0.0017 995	0.0392 995	0.0451 394	0.0017 727	0.0392 727
84	0.0453 941	0.0017 832	0.0392 832	0.0441 204	0.0017 309	0.0392 309	0.0434 856	0.0017 048	0.0392 048
85	0.0437 533	0.0017 158	0.0392 158	0.0425 113	0.0016 650	0.0391 650	0.0418 924	0.0016 397	0.0391 397
86	0.0421 719	0.0016 511	0.0391 511	0.0409 609	0.0016 016	0.0391 016	0.0403 576	0.0015 771	0.0390 771
87	0.0406 476	0.0015 889	0.0390 889	0.0394 670	0.0015 408	0.0390 408	0.0388 790	0.0015 169	0.0390 169
88	0.0391 784	0.0015 291	0.0390 291	0.0380 276	0.0014 824	0.0389 824	0.0374 545	0.0014 592	0.0389 592
89	0.0377 623	0.0014 717	0.0389 717	0.0366 407	0.0014 263	0.0389 263	0.0360 823	0.0014 037	0.0389 037
90	0.0363 974	0.0014 165	0.0389 165	0.0353 043	0.0013 724	0.0388 724	0.0347 603	0.0013 505	0.0388 505
91	0.0350 819	0.0013 634	0.0388 634	0.0340 168	0.0013 205	0.0388 205	0.0334 868	0.0012 993	0.0387 993
92	0.0338 138	0.0013 124	0.0388 124	0.0327 761	0.0012 708	0.0387 708	0.0322 600	0.0012 501	0.0387 501
93	0.0325 916	0.0012 634	0.0387 634	0.0315 807	0.0012 229	0.0387 229	0.0310 780	0.0012 028	0.0387 028
94	0.0314 136	0.0012 162	0.0387 162	0.0304 290	0.0011 769	0.0386 769	0.0299 394	0.0011 574	0.0386 574
95	0.0302 782	0.0011 709	0.0386 709	0.0293 192	0.0011 327	0.0386 327	0.0288 425	0.0011 137	0.0386 137
96	0.0291 838	0.0011 273	0.0386 273	0.0282 499	0.0010 902	0.0385 902	0.0277 853	0.0010 717	0.0385 717
97	0.0281 290	0.0010 854	0.0385 854	0.0272 196	0.0010 493	0.0385 493	0.0267 678	0.0010 314	0.0385 314
98	0.0271 123	0.0010 450	0.0385 450	0.0262 268	0.0010 100	0.0385 100	0.0257 871	0.0009 926	0.0384 926
99	0.0261 323	0.0010 063	0.0385 063	0.0252 703	0.0009 722	0.0384 722	0.0248 423	0.0009 553	0.0384 553
100	0.0251 878	0.0009 689	0.0384 689	0.0243 487	0.0009 359	0.0384 359	0.0239 322	0.0009 195	0.0384 195
	Ratio of Perpetual Ann.		0.0375 000	- - - - - - - - - -		0.0375 000	- - - - - - - - - -		0.0375 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.04.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02.			RATIO *of* INTEREST: *QUARTERLY*, 0.01.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
0	....	....	....	....	....	....	1.0100 000	0.2500 000	0.2475 25
½	....	....	....	1.0200 000	0.5000 000	0.4901 96	1.0201 000	0.5025 000	0.4925 99
1	.... 1.0400 000	.... 1.0000 000	.... 0.9615 38	.... 1.0404 000	.... 1.0100 000	.... 0.9707 80	1.0303 010 1.0406 040	0.7575 250 1.0151 003	0.7352 46 0.9754 91
1½	....	....	....	....	....	....	1.0510 101	1.2752 513	1.2133 58
2	.... 1.0816 000	.... 2.0400 000	.... 1.8860 95	1.0612 080 .... 1.0824 322	1.5302 000 .... 2.0608 040	1.4419 42 .... 1.9038 64	1.0615 202 1.0721 354 1.0828 567	1.5380 038 1.8033 838 2.0714 176	1.4488 69 1.6820 49 1.9129 19
2½	....	....	....	....	....	....	1.0936 853	2.3421 318	2.1415 04
3	.... 1.1248 640	.... 3.1216 000	.... 2.7750 91	1.1040 808 .... 1.1261 624	2.6020 201 .... 3.1540 605	2.3567 30 .... 2.8007 15	1.1046 221 1.1156 683 1.1268 250	2.6155 531 2.8917 087 3.1706 258	2.3678 26 2.5919 07 2.8137 69
3½	....	....	....	....	....	....	1.1380 933	3.4523 320	3.0334 35
4	.... 1.1698 586	.... 4.2464 640	.... 3.6298 95	1.1486 857 .... 1.1716 594	3.7171 417 .... 4.2914 845	3.2359 95 .... 3.6627 41	1.1494 742 1.1609 690 1.1725 786	3.7368 553 4.0242 239 4.3144 661	3.2509 26 3.4662 63 3.6794 68
4½	....	....	....	....	....	....	1.1843 044	4.6076 108	3.8905 63
5	.... 1.2166 529	.... 5.4163 226	.... 4.4518 22	1.1950 926 .... 1.2189 944	4.8773 142 .... 5.4748 605	4.0311 18 .... 4.4912 92	1.1961 475 1.2081 090 1.2201 900	4.9036 869 5.2027 238 5.5047 510	4.0995 67 4.3065 02 4.5113 88
5½	....	....	....	....	....	....	1.2323 919	5.8097 935	4.7142 46
6	.... 1.2653 190	.... 6.6329 755	.... 5.2421 37	1.2433 743 .... 1.2682 418	6.0843 577 .... 6.7060 449	4.8934 24 .... 5.2876 71	1.2447 159 1.2571 630 1.2697 346	6.1178 964 6.4290 755 6.7433 662	4.9150 95 5.1139 55 5.3108 47
6½	....	....	....	....	....	....	1.2824 320	7.0607 998	5.5057 89
7	.... 1.3159 318	.... 7.8982 945	.... 6.0020 55	1.2936 066 .... 1.3194 788	7.3401 658 .... 7.9869 691	5.6741 87 .... 6.0531 24	1.2952 563 1.3082 089 1.3212 910	7.3814 079 7.7052 219 8.0322 742	5.6988 01 5.8899 02 6.0791 11
7½	....	....	....	....	....	....	1.3345 039	8.3625 969	6.2664 46
8	.... 1.3685 691	.... 9.2142 263	.... 6.7327 45	1.3458 683 .... 1.3727 857	8.6467 085 .... 9.3196 426	6.4246 32 .... 6.7888 55	1.3478 489 1.3613 274 1.3749 407	8.6962 229 9.0331 851 9.3735 170	6.4519 27 6.6355 71 6.8173 97
8½	....	....	....	....	....	....	1.3886 901	9.7172 521	6.9974 23
9	.... 1.4233 118	.... 10.582 795	.... 7.4353 32	1.4002 414 .... 1.4282 462	10.006 035 .... 10.706 156	7.1459 36 .... 7.4960 16	1.4025 770 1.4166 028 1.4307 688	10.064 425 10.415 069 10.769 220	7.1756 66 7.3521 45 7.5268 76
9½	....	....	....	....	....	....	1.4450 765	11.126 912	7.6998 77
10	.... 1.4802 443	.... 12.006 107	.... 8.1108 96	1.4568 112 .... 1.4859 474	11.420 279 .... 12.148 685	7.8392 31 .... 8.1757 17	1.4595 272 1.4741 225 1.4888 637	11.488 181 11.853 063 12.221 593	7.8711 66 8.0407 58 8.2086 71
10½	....	....	....	....	....	....	1.5037 524	12.593 809	8.3749 22
11	.... 1.5394 541	.... 13.486 351	.... 8.7604 77	1.5156 663 .... 1.5459 797	12.891 659 .... 13.649 492	8.5056 05 .... 8.8290 24	1.5187 899 1.5339 778 1.5493 176	12.969 747 13.349 445 13.732 939	8.5395 27 8.7025 02 8.8638 63
11½	....	....	....	....	....	....	1.5648 107	14.120 269	9.0236 27
12	.... 1.6010 322	.... 15.025 805	.... 9.3850 74	1.5768 993 .... 1.6084 372	14.422 482 .... 15.210 931	9.1461 02 .... 9.4569 63	1.5804 589 1.5962 634 1.6122 261	14.511 471 14.906 586 15.305 652	9.1818 09 9.3384 25 9.4934 90
12½	....	....	....	....	....	....	1.6283 483	15.708 708	9.6470 20
13	.... 1.6650 735	.... 16.626 838	.... 9.9856 48	1.6406 062 .... 1.6734 181	16.015 150 .... 16.835 453	9.7617 28 .... 10.060 52	1.6446 318 1.6610 781 1.6776 889	16.115 796 16.526 953 16.942 223	9.7990 29 9.9495 34 10.098 55
13½	....	....	....	....	....	....	1.6944 658	17.361 645	10.246 09
14	.... 1.7316 764	.... 18.291 911	.... 10.563 12	1.7068 865 .... 1.7410 242	17.672 162 .... 18.525 605	10.353 45 .... 10.640 64	1.7114 105 1.7285 246 1.7458 098	17.785 262 18.213 114 18.645 245	10.392 17 10.536 80 10.680 00
14½	....	....	....	....	....	....	1.7632 679	19.081 698	10.821 78
15	.... 1.8009 435	.... 20.023 588	.... 11.118 39	1.7758 447 .... 1.8113 616	19.396 117 .... 20.284 040	10.922 19 .... 11.198 23	1.7809 006 1.7987 096 1.8166 967	19.522 515 19.967 740 20.417 417	10.962 16 11.101 15 11.238 76
15½	....	....	....	....	....	....	1.8348 637	20.871 592	11.375 01
16	.... 1.8729 812	.... 21.824 531	.... 11.652 30	1.8475 888 .... 1.8845 406	21.189 720 .... 22.113 515	11.468 85 .... 11.734 17	1.8532 123 1.8717 444 1.8904 619	21.330 308 21.793 611 22.261 547	11.509 91 11.643 48 11.775 72
17	1.9479 005	23.697 512	12.165 67	1.9606 760	24.016 901	12.249 30	1.9672 222	24.180 555	12.291 72
18	2.0258 165	25.645 413	12.659 30	2.0398 873	25.997 184	12.744 42	2.0470 993	26.177 483	12.787 60
19	2.1068 492	27.671 229	13.133 94	2.1222 988	28.057 470	13.220 32	2.1302 198	28.255 494	13.264 12
20	2.1911 231	29.778 079	13.590 33	2.2080 397	30.200 992	13.677 74	2.2167 152	30.417 880	13.722 05
21	2.2787 681	31.969 202	14.029 16	2.2972 445	32.431 112	14.117 39	2.3067 227	32.668 069	14.162 11
22	2.3699 188	34.247 970	14.451 12	2.3900 531	34.751 327	14.539 98	2.4003 849	35.009 623	14.585 00
23	2.4647 155	36.617 889	14.856 84	2.4866 113	37.165 282	14.946 16	2.4978 502	37.446 255	14.991 39
24	2.5633 042	39.082 604	15.246 96	2.5870 704	39.676 760	15.336 56	2.5992 729	39.981 823	15.381 93
25	2.6658 363	41.645 908	15.622 08	2.6915 880	42.289 701	15.711 80	2.7048 138	42.620 346	15.757 22

PERPETUAL STOCK: 3 p.C. 75; 3½ p.C. 87,5; 4 p.C. 100; 5 p.C. 125.

Years.	RATIO of INTEREST: ANNUALLY, 0.04.			RATIO of INTEREST: HALF-YEARLY, 0.02.			RATIO of INTEREST: QUARTERLY, 0.01.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
0¼	....	....	....	....	....	....	0.9900 990	4.0000 000	4.0400 000
0½	....	....	....	0.9803 921	2.0000 000	2.0400 000	0.9802 960	1.9900 497	2.0300 497
0¾	....	....	....	....	....	....	0.9705 901	1.3200 885	1.3600 885
1	0.9615 384	1.0000 000	1.0400 000	0.9611 688	0.9900 990	1.0300 990	0.9609 804	0.9851 244	1.0251 244
1¼	....	....	....	....	....	....	0.9514 657	0.7841 592	0.8241 592
1½	....	....	....	0.9423 223	0.6535 094	0.6935 094	0.9420 453	0.6501 935	0.6901 935
1¾	....	....	....	....	....	....	0.9327 181	0.5545 131	0.5945 131
2	0.9245 562	0.4901 961	0.5301 961	0.9238 453	0.4852 475	0.5252 475	0.9234 832	0.4827 611	0.5227 611
2¼	....	....	....	....	....	....	0.9143 398	0.4269 614	0.4669 614
2½	....	....	....	0.9057 308	0.3843 168	0.4243 168	0.9052 870	0.3823 283	0.4223 283
2¾	....	....	....	....	....	....	0.8963 237	0.3458 163	0.3858 163
3	0.8889 963	0.3203 485	0.3603 485	0.8879 714	0.3170 516	0.3570 516	0.8874 492	0.3153 951	0.3553 951
3¼	....	....	....	....	....	....	0.8786 625	0.2896 593	0.3296 593
3½	....	....	....	0.8705 602	0.2690 239	0.3090 239	0.8699 629	0.2676 047	0.3076 047
3¾	....	....	....	....	....	....	0.8613 494	0.2484 951	0.2884 951
4	0.8548 042	0.2354 900	0.2754 900	0.8534 904	0.2330 196	0.2730 196	0.8528 212	0.2317 784	0.2717 784
4¼	....	....	....	....	....	....	0.8443 775	0.2170 322	0.2570 322
4½	....	....	....	0.8367 553	0.2050 309	0.2450 309	0.8360 173	0.2039 282	0.2439 282
4¾	....	....	....	....	....	....	0.8277 399	0.1922 070	0.2322 070
5	0.8219 271	0.1846 271	0.2246 271	0.8203 483	0.1826 531	0.2226 531	0.8195 444	0.1816 613	0.2216 613
5¼	....	....	....	....	....	....	0.8114 301	0.1721 230	0.2121 230
5½	....	....	....	0.8042 630	0.1643 559	0.2043 559	0.8033 962	0.1634 549	0.2034 549
5¾	....	....	....	....	....	....	0.7954 418	0.1555 434	0.1955 434
6	0.7903 145	0.1507 619	0.1907 619	0.7884 932	0.1491 192	0.1891 192	0.7875 662	0.1482 939	0.1882 939
6¼	....	....	....	....	....	....	0.7797 684	0.1416 270	0.1816 270
6½	....	....	....	0.7730 326	0.1362 367	0.1762 367	0.7720 480	0.1354 755	0.1754 755
6¾	....	....	....	....	....	....	0.7644 039	0.1297 821	0.1697 821
7	0.7599 178	0.1266 096	0.1666 096	0.7578 751	0.1252 040	0.1652 040	0.7568 356	0.1244 977	0.1644 977
7¼	....	....	....	....	....	....	0.7493 422	0.1195 801	0.1595 801
7½	....	....	....	0.7430 147	0.1156 509	0.1556 509	0.7419 229	0.1149 925	0.1549 925
7¾	....	....	....	....	....	....	0.7345 771	0.1107 029	0.1507 029
8	0.7306 902	0.1085 278	0.1485 278	0.7264 458	0.1073 003	0.1473 003	0.7273 041	0.1066 835	0.1466 835
8¼	....	....	....	....	....	....	0.7201 031	0.1029 098	0.1429 098
8½	....	....	....	0.7141 626	0.0999 397	0.1399 397	0.7129 733	0.0993 599	0.1393 599
8¾	....	....	....	....	....	....	0.7059 143	0.0960 147	0.1360 147
9	0.7025 867	0.0944 930	0.1344 930	0.7001 594	0.0934 042	0.1334 042	0.6989 249	0.0928 572	0.1328 572
9¼	....	....	....	....	....	....	0.6920 049	0.0898 722	0.1298 722
9½	....	....	....	0.6864 307	0.0875 635	0.1275 635	0.6851 533	0.0870 460	0.1270 460
9¾	....	....	....	....	....	....	0.6783 697	0.0843 664	0.1243 664
10	0.6755 642	0.0832 909	0.1232 909	0.6729 713	0.0823 134	0.1223 134	0.6716 531	0.0818 224	0.1218 224
10¼	....	....	....	....	....	....	0.6650 031	0.0794 041	0.1194 041
10½	....	....	....	0.6597 758	0.0775 695	0.1175 695	0.6584 189	0.0771 025	0.1171 025
10¾	....	....	....	....	....	....	0.6518 999	0.0749 095	0.1149 095
11	0.6495 810	0.0741 490	0.1141 490	0.6468 390	0.0732 628	0.1132 628	0.6454 454	0.0728 176	0.1128 176
11¼	....	....	....	....	....	....	0.6390 550	0.0708 202	0.1108 202
11½	....	....	....	0.6341 559	0.0693 362	0.1093 362	0.6327 277	0.0689 110	0.1089 110
11¾	....	....	....	....	....	....	0.6264 630	0.0670 799	0.1070 799
12	0.6245 971	0.0665 522	0.1065 522	0.6217 215	0.0657 422	0.1057 422	0.6202 604	0.0653 353	0.1053 353
12¼	....	....	....	....	....	....	0.6141 192	0.0636 590	0.1036 590
12½	....	....	....	0.6095 309	0.0624 409	0.1024 409	0.6080 388	0.0620 509	0.1020 509
12¾	....	....	....	....	....	....	0.6020 187	0.0605 072	0.1005 072
13	0.6005 741	0.0601 437	0.1001 437	0.5975 793	0.0593 985	0.0993 985	0.5960 581	0.0590 241	0.0990 241
13¼	....	....	....	....	....	....	0.5901 565	0.0575 982	0.0975 982
13½	....	....	....	0.5858 621	0.0565 862	0.0965 862	0.5843 134	0.0562 263	0.0962 263
13¾	....	....	....	....	....	....	0.5785 271	0.0549 055	0.0949 055
14	0.5774 751	0.0546 690	0.0946 690	0.5743 745	0.0539 793	0.0939 793	0.5728 001	0.0536 330	0.0936 330
14¼	....	....	....	....	....	....	0.5671 288	0.0524 062	0.0924 062
14½	....	....	....	0.5631 123	0.0515 567	0.0915 567	0.5615 136	0.0512 229	0.0912 229
14¾	....	....	....	....	....	....	0.5559 541	0.0500 808	0.0900 808
15	0.5552 645	0.0499 411	0.0899 411	0.5520 709	0.0492 998	0.0892 998	0.5504 496	0.0489 778	0.0889 778
15¼	....	....	....	....	....	....	0.5449 996	0.0479 120	0.0879 120
15½	....	....	....	0.5412 460	0.0471 927	0.0871 927	0.5396 036	0.0468 817	0.0868 817
15¾	....	....	....	....	....	....	0.5342 692	0.0458 850	0.0858 850
16	0.5339 082	0.0458 200	0.0858 200	0.5306 333	0.0452 212	0.0852 212	0.5289 713	0.0449 205	0.0849 205
17	0.5133 733	0.0421 985	0.0821 985	0.5100 282	0.0416 373	0.0816 373	0.5083 310	0.0413 555	0.0813 555
18	0.4936 281	0.0389 933	0.0789 933	0.4902 232	0.0384 657	0.0784 657	0.4884 961	0.0382 008	0.0782 008
19	0.4746 424	0.0361 386	0.0761 386	0.4711 872	0.0356 411	0.0756 411	0.4694 351	0.0353 913	0.0753 913
20	0.4563 870	0.0335 818	0.0735 818	0.4528 904	0.0331 115	0.0731 115	0.4511 179	0.0328 754	0.0728 754
21	0.4388 336	0.0312 801	0.0712 801	0.4353 041	0.0308 346	0.0708 346	0.4335 155	0.0306 109	0.0706 109
22	0.4219 554	0.0291 988	0.0691 988	0.4184 007	0.0287 759	0.0687 759	0.4165 998	0.0285 636	0.0685 636
23	0.4057 264	0.0273 090	0.0673 090	0.4021 537	0.0269 068	0.0669 068	0.4003 442	0.0267 049	0.0667 049
24	0.3901 215	0.0255 868	0.0655 868	0.3865 376	0.0252 037	0.0652 037	0.3847 229	0.0250 114	0.0650 114
25	0.3751 168	0.0240 120	0.0640 120	0.3715 279	0.0236 464	0.0636 464	0.3697 112	0.0234 630	0.0634 630

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.04.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02.			RATIO *of* INTEREST: *QUARTERLY*, 0.01.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	2.7724 698	44.311 745	15.982 77	2.8003 282	45.008 205	16.072 47	2.8146 401	45.366 003	16.117 87
27	2.8833 686	47.084 214	16.329 59	2.9134 614	47.836 536	16.419 14	2.9289 258	48.223 145	16.464 45
28	2.9987 033	49.967 583	16.663 06	3.0311 653	50.779 132	16.752 35	3.0478 519	51.196 298	16.797 50
29	3.1186 515	52.966 286	16.983 71	3.1536 244	53.840 609	17.072 61	3.1716 069	54.290 173	17.117 56
30	3.2433 975	56.084 938	17.292 03	3.2810 308	57.025 770	17.380 44	3.3003 869	57.509 672	17.425 13
31	3.3731 334	59.328 335	17.588 49	3.4135 844	60.339 611	17.676 32	3.4343 958	60.859 896	17.720 70
32	3.5080 587	62.701 469	17.873 55	3.5514 932	63.787 331	17.960 71	3.5738 461	64.346 152	18.004 74
33	3.6483 811	66.209 527	18.147 65	3.6949 736	67.374 339	18.234 05	3.7189 586	67.973 964	18.277 69
34	3.7943 163	69.857 909	18.411 20	3.8442 505	71.106 263	18.496 78	3.8699 632	71.749 080	18.539 99
35	3.9460 890	73.652 225	18.664 61	3.9995 582	74.988 956	18.749 31	4.0270 992	75.677 480	18.792 06
36	4.1039 326	77.598 314	18.908 28	4.1611 404	79.028 509	18.992 03	4.1906 156	79.765 390	19.034 29
37	4.2680 899	81.702 246	19.142 58	4.3292 504	83.231 261	19.225 33	4.3607 714	84.019 285	19.267 07
38	4.4388 135	85.970 336	19.367 86	4.5041 522	87.603 804	19.449 57	4.5378 362	88.445 905	19.490 77
39	4.6163 660	90.409 150	19.584 48	4.6861 199	92.152 998	19.665 10	4.7220 905	93.052 264	19.705 73
40	4.8010 206	95.025 516	19.792 77	4.8754 392	96.885 979	19.872 26	4.9138 264	97.845 659	19.912 31
41	4.9930 615	99.826 536	19.993 05	5.0724 069	101.81 017	20.071 37	5.1133 474	102.83 369	20.110 83
42	5.1927 839	104.81 960	20.185 63	5.2773 321	106.93 330	20.262 76	5.3209 698	108.02 425	20.301 61
43	5.4004 953	110.01 238	20.370 79	5.4905 364	112.26 341	20.446 71	5.5370 225	113.42 556	20.484 94
44	5.6165 151	115.41 288	20.548 84	5.7123 540	117.80 885	20.623 52	5.7618 478	119.04 620	20.661 12
45	5.8411 757	121.02 939	20.720 04	5.9431 331	123.57 833	20.793 46	5.9958 020	124.89 505	20.830 40
46	6.0748 227	126.87 057	20.884 65	6.1832 357	129.58 089	20.956 81	6.2392 556	130.98 139	20.993 11
47	6.3178 156	132.94 539	21.042 94	6.4330 384	135.82 596	21.113 81	6.4925 944	137.31 486	21.149 46
48	6.5705 282	139.26 321	21.195 13	6.6929 332	142.32 333	21.264 72	6.7562 197	143.90 549	21.299 70
49	6.8333 494	145.83 373	21.341 47	6.9633 277	149.08 319	21.409 77	7.0305 491	150.76 373	21.444 09
50	7.1066 833	152.66 708	21.482 18	7.2446 461	156.11 615	21.549 18	7.3160 178	157.90 045	21.582 84
51	7.3909 507	159.77 377	21.617 49	7.5373 298	163.43 325	21.683 18	7.6130 775	165.32 694	21.716 18
52	7.6865 887	167.16 472	21.747 58	7.8418 379	171 04 595	21.811 97	7.9221 990	173.05 497	21.844 31
53	7.9940 523	174.85 131	21.872 67	8.1586 484	178.96 621	21.935 77	8.2438 720	181.09 680	21.967 44
54	8.3138 143	182.84 536	21.992 96	8.4882 578	187.20 644	22.054 75	8.5786 063	189.46 516	22.085 77
55	8.6463 669	191.15 917	22.108 61	8.8311 834	195.77 959	22.169 12	8.9269 321	198.17 330	22.199 49
56	8.9922 216	199.80 554	22.219 82	9.1879 632	204.69 908	22.279 05	9.2894 014	207.23 503	22.308 77
57	9.3519 105	208.79 776	22.326 75	9.5591 569	213.97 892	22.384 71	9.6665 883	216.66 471	22.413 77
58	9.7259 869	218.14 967	22.429 57	9.9453 469	223.63 367	22.486 26	10.059 091	226.47 726	22.514 69
59	10.115 026	227.87 566	22.528 43	10.347 139	233.67 847	22.583 87	10.467 530	236.68 825	22.611 66
60	10.519 627	237.99 069	22.623 49	10.765 163	244.12 908	22.677 70	10.892 554	247.31 384	22.704 85
61	10.940 413	248.51 031	22.714 89	11.200 076	255.00 190	22.767 87	11.334 835	258.37 088	22.794 41
62	11.378 029	259.45 073	22.802 78	11.652 559	266.31 397	22.854 55	11.795 075	269.87 687	22.880 47
63	11.833 150	270.82 875	22.887 29	12.123 322	278.08 306	22.937 86	12.274 002	281.85 005	22.963 17
64	12.306 476	282.66 190	22.968 55	12.613 105	290.32 762	23.017 94	12.772 376	294.30 939	23.042 65
65	12.798 735	294.96 838	23.046 68	13.122 674	303.06 685	23.094 90	13.290 985	307.27 464	23.119 03
66	13.310 685	307.76 712	23.121 81	13.652 830	316.32 075	23.168 88	13.830 653	320.76 632	23.192 42
67	13.843 112	321.07 780	23.194 05	14.204 404	330.11 011	23.239 98	14.392 233	334.80 582	23.262 95
68	14.396 836	334.92 091	23.263 51	14.778 262	344.45 656	23.308 32	14.976 615	349.41 538	23.330 73
69	14.972 710	349.31 775	23.330 30	15.375 304	359.38 260	23.374 02	15.584 726	364.61 814	23.395 87
70	15.571 618	364.29 046	23.394 51	15.996 466	374.91 166	23.437 15	16.217 528	380.43 820	23.458 46
71	16.194 483	379.86 208	23.456 26	16.642 724	391.06 809	23.497 84	16.876 025	396.90 062	23.518 61
72	16.842 262	396.05 656	23.515 64	17.315 090	407.87 724	23.556 17	17.561 259	414.03 148	23.576 41
73	17.515 953	412.89 882	23.572 73	18.014 619	425.36 548	23.612 24	18.274 317	431.85 791	23.631 96
74	18.216 591	430.41 478	23.627 62	18.742 410	443.56 025	23.666 13	19.016 327	450.40 818	23.685 34
75	18.945 255	448.63 137	23.680 41	19.499 603	462.49 008	23.717 92	19.788 466	469.71 166	23.736 64
76	19.703 065	467.57 662	23.731 16	20.287 387	482.18 468	23.767 71	20.591 957	489.79 893	23.785 93
77	20.491 187	487.27 969	23.779 96	21.106 998	502.67 494	23.815 56	21.428 073	510.70 183	23.833 31
78	21.310 835	507.77 087	23.826 89	21.959 720	523.99 301	23.861 56	22.298 139	532.45 348	23.878 83
79	22.163 268	529.08 171	23.872 01	22.846 893	546.17 233	23.905 76	23.203 533	555.08 832	23.922 58
80	23.049 799	551.24 498	23.915 39	23.769 908	569.24 769	23.948 25	24.145 689	578.64 224	23.964 62
81	23.971 791	574.29 478	23.957 11	24.730 212	593.25 530	23.989 09	25.126 101	603.15 253	24.005 02
82	24.930 663	598.26 657	23.997 22	25.729 312	618.23 281	24.028 35	26.146 322	628.65 804	24.043 84
83	25.927 889	623.19 723	24.035 79	26.768 777	644.21 941	24.066 08	27.207 967	655.19 918	24.081 15
84	26.965 005	649.12 512	24.072 87	27.850 235	671.25 588	24.102 34	28.312 720	682.81 799	24.117 00
85	28.043 605	676.09 012	24.108 53	28.975 385	699.38 462	24.137 20	29.462 330	711.55 824	24.151 46
86	29.165 349	704.13 373	24.142 82	30.145 990	728.64 976	24.170 70	30.658 618	741.46 546	24.184 57
87	30.331 963	733.29 908	24.175 79	31.363 888	759.09 721	24.202 91	31.903 481	772.58 703	24.216 39
88	31.545 242	763.63 104	24.207 49	32.630 989	790.77 473	24.233 86	33.198 891	804.97 227	24.246 95
89	32.807 051	795.17 628	24.237 97	33.949 281	823.73 203	24.263 61	34.546 899	838.67 247	24.276 35
90	34.119 333	827.98 333	24.267 28	35.320 832	858.02 081	24.292 20	35.949 641	873.74 103	24.304 58
91	35.484 107	862.10 267	24.295 46	36.747 794	893.69 485	24.319 68	37.409 341	910.23 352	24.331 72
92	36.903 471	897.58 677	24.322 56	38.232 405	930.81 012	24.346 10	38.928 310	948.20 775	24.357 79
93	38.379 610	934.49 024	24.348 61	39.776 994	969.42 485	24.371 50	40.508 956	987.72 389	24.382 85
94	39.914 794	972.86 985	24.373 67	41.383 984	1009.5 996	24.395 90	42.153 782	1028.8 445	24.406 93
95	41.511 386	1012.7 846	24.397 76	43.055 897	1051.3 974	24.419 36	43.865 394	1071.6 349	24.430 08
96	43.171 841	1054.2 960	24.420 92	44.795 356	1094.8 839	24.441 91	45.646 505	1116.1 626	24.452 31
97	44.898 715	1097.4 679	24.443 19	46.605 088	1140.1 272	24.463 58	47.499 936	1162.4 984	24.473 68
98	46.694 664	1142.3 666	24.464 61	48.487 934	1187.1 983	24.484 41	49.428 624	1210.7 156	24.494 22
99	48.562 450	1189.0 613	24.485 20	50.446 846	1236.1 712	24.504 43	51.435 625	1260.8 906	24.513 95
100	50.504 948	1237.6 237	24.505 00	52.484 899	1287.1 225	24.523 67	53.524 117	1313.1 029	24.532 92
	Value of Perpetual Ann.		25.000 00	- - - - - - - - - -		25.000 00	- - - - - - - - - -		25.000 00

PERPETUAL STOCK: 3 *p.C.* 75; 3½ *p.C.* 87,5; 4 *p.C.* 100; 5 *p.C.* 125.

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.04.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02.			RATIO *of* INTEREST: *QUARTERLY*, 0.01.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.3606 892	0.0225 674	0.0625 674	0.3571 010	0.0222 182	0.0622 182	0.3552 852	0.0220 429	0.0620 429
27	0.3468 166	0.0212 385	0.0612 385	0.3432 343	0.0209 045	0.0609 045	0.3414 221	0.0207 369	0.0607 369
28	0.3334 775	0.0200 130	0.0600 130	0.3299 061	0.0196 931	0.0596 931	0.3280 999	0.0195 326	0.0595 326
29	0.3206 514	0.0188 799	0.0588 799	0.3170 955	0.0185 733	0.0585 733	0.3152 976	0.0184 195	0.0584 195
30	0.3083 187	0.0178 301	0.0578 301	0.3047 823	0.0175 359	0.0575 359	0.3029 948	0.0173 884	0.0573 884
31	0.2964 602	0.0168 554	0.0568 554	0.2929 472	0.0165 729	0.0565 729	0.2911 720	0.0164 312	0.0564 312
32	0.2850 579	0.0159 486	0.0559 486	0.2815 717	0.0156 771	0.0556 771	0.2798 106	0.0155 409	0.0555 409
33	0.2740 942	0.0151 036	0.0551 036	0.2706 379	0.0148 424	0.0548 424	0.2688 925	0.0147 115	0.0547 115
34	0.2635 521	0.0143 148	0.0543 148	0.2601 287	0.0140 635	0.0540 635	0.2584 004	0.0139 375	0.0539 375
35	0.2534 154	0.0135 773	0.0535 773	0.2500 276	0.0133 353	0.0533 353	0.2483 177	0.0132 140	0.0532 140
36	0.2436 687	0.0128 869	0.0528 869	0.2403 187	0.0126 537	0.0526 537	0.2386 284	0.0125 368	0.0525 368
37	0.2342 968	0.0122 396	0.0522 396	0.2309 869	0.0120 147	0.0520 147	0.2293 172	0.0119 020	0.0519 020
38	0.2252 854	0.0116 319	0.0516 319	0.2220 174	0.0114 150	0.0514 150	0.2203 693	0.0113 063	0.0513 063
39	0.2166 206	0.0110 608	0.0510 608	0.2133 962	0.0108 515	0.0508 515	0.2117 706	0.0107 466	0.0507 466
40	0.2082 890	0.0105 235	0.0505 235	0.2051 097	0.0103 214	0.0503 214	0.2035 074	0.0102 202	0.0502 202
41	0.2002 779	0.0100 174	0.0500 174	0.1971 450	0.0098 222	0.0498 222	0.1955 666	0.0097 244	0.0497 244
42	0.1925 749	0.0095 402	0.0495 402	0.1894 897	0.0093 516	0.0493 516	0.1879 357	0.0092 572	0.0492 572
43	0.1851 682	0.0090 899	0.0490 899	0.1821 316	0.0089 076	0.0489 076	0.1806 025	0.0088 164	0.0488 164
44	0.1780 464	0.0086 645	0.0486 645	0.1750 592	0.0084 883	0.0484 883	0.1735 555	0.0084 001	0.0484 001
45	0.1711 984	0.0082 625	0.0482 625	0.1682 614	0.0080 920	0.0480 920	0.1667 834	0.0080 067	0.0480 067
46	0.1646 139	0.0078 820	0.0478 820	0.1617 276	0.0077 172	0.0477 172	0.1602 755	0.0076 347	0.0476 347
47	0.1582 826	0.0075 219	0.0475 219	0.1554 476	0.0073 624	0.0473 624	0.1540 216	0.0072 825	0.0472 825
48	0.1521 948	0.0071 806	0.0471 806	0.1494 113	0.0070 263	0.0470 263	0.1480 118	0.0069 490	0.0469 490
49	0.1463 411	0.0068 571	0.0468 571	0.1436 094	0.0067 077	0.0467 077	0.1422 364	0.0066 329	0.0466 329
50	0.1407 126	0.0065 502	0.0465 502	0.1380 330	0.0064 055	0.0464 055	0.1366 864	0.0063 331	0.0463 331
51	0.1353 006	0.0062 588	0.0462 588	0.1326 730	0.0061 187	0.0461 187	0.1313 529	0.0060 486	0.0460 486
52	0.1300 967	0.0059 821	0.0459 821	0.1275 211	0.0058 464	0.0458 464	0.1262 276	0.0057 785	0.0457 785
53	0.1250 930	0.0057 191	0.0457 191	0.1225 693	0.0055 876	0.0455 876	0.1213 022	0.0055 219	0.0455 219
54	0.1202 817	0.0054 691	0.0454 691	0.1178 098	0.0053 417	0.0453 417	0.1165 690	0.0052 780	0.0452 780
55	0.1156 555	0.0052 312	0.0452 312	0.1132 351	0.0051 078	0.0451 078	0.1120 206	0.0050 461	0.0450 461
56	0.1112 072	0.0050 049	0.0450 049	0.1088 381	0.0048 852	0.0448 852	0.1076 496	0.0048 254	0.0448 254
57	0.1069 300	0.0047 893	0.0447 893	0.1046 117	0.0046 734	0.0446 734	0.1034 491	0.0046 154	0.0446 154
58	0.1028 173	0.0045 841	0.0445 841	0.1005 495	0.0044 716	0.0444 716	0.0994 126	0.0044 155	0.0444 155
59	0.0988 628	0.0043 884	0.0443 884	0.0966 451	0.0042 794	0.0442 794	0.0955 335	0.0042 250	0.0442 250
60	0.0950 604	0.0042 018	0.0442 018	0.0928 922	0.0040 962	0.0440 962	0.0918 058	0.0040 434	0.0440 434
61	0.0914 042	0.0040 240	0.0440 240	0.0892 851	0.0039 215	0.0439 215	0.0882 236	0.0038 704	0.0438 704
62	0.0878 887	0.0038 543	0.0438 543	0.0858 181	0.0037 550	0.0437 550	0.0847 812	0.0037 054	0.0437 054
63	0.0845 084	0.0036 924	0.0436 924	0.0824 856	0.0035 960	0.0435 960	0.0814 730	0.0035 480	0.0435 480
64	0.0812 580	0.0035 378	0.0435 378	0.0792 826	0.0034 444	0.0434 444	0.0782 940	0.0033 978	0.0433 978
65	0.0781 327	0.0033 902	0.0433 902	0.0762 040	0.0032 996	0.0432 996	0.0752 390	0.0032 544	0.0432 544
66	0.0751 276	0.0032 492	0.0432 492	0.0732 449	0.0031 613	0.0431 613	0.0723 032	0.0031 175	0.0431 175
67	0.0722 381	0.0031 145	0.0431 145	0.0704 007	0.0030 293	0.0430 293	0.0694 819	0.0029 868	0.0429 868
68	0.0694 597	0.0029 858	0.0429 858	0.0676 670	0.0029 031	0.0429 031	0.0667 708	0.0028 619	0.0428 619
69	0.0667 882	0.0028 627	0.0428 627	0.0650 394	0.0027 825	0.0427 825	0.0641 654	0.0027 426	0.0427 426
70	0.0642 194	0.0027 451	0.0427 451	0.0625 138	0.0026 673	0.0426 673	0.0616 617	0.0026 285	0.0426 285
71	0.0617 494	0.0026 325	0.0426 325	0.0600 863	0.0025 571	0.0425 571	0.0592 557	0.0025 195	0.0425 195
72	0.0593 744	0.0025 249	0.0425 249	0.0577 531	0.0024 517	0.0424 517	0.0569 435	0.0024 153	0.0424 153
73	0.0570 908	0.0024 219	0.0424 219	0.0555 105	0.0023 509	0.0423 509	0.0547 216	0.0023 156	0.0423 156
74	0.0548 950	0.0023 233	0.0423 233	0.0533 549	0.0022 545	0.0422 545	0.0525 864	0.0022 202	0.0422 202
75	0.0527 837	0.0022 290	0.0422 290	0.0512 831	0.0021 622	0.0421 622	0.0505 345	0.0021 290	0.0421 290
76	0.0507 535	0.0021 387	0.0421 387	0.0492 917	0.0020 739	0.0420 739	0.0485 626	0.0020 417	0.0420 417
77	0.0488 015	0.0020 522	0.0420 522	0.0473 777	0.0019 894	0.0419 894	0.0466 678	0.0019 581	0.0419 581
78	0.0469 245	0.0019 694	0.0419 694	0.0455 379	0.0019 084	0.0419 084	0.0448 408	0.0018 781	0.0418 781
79	0.0451 197	0.0018 901	0.0418 901	0.0437 696	0.0018 309	0.0418 309	0.0430 969	0.0018 015	0.0418 015
80	0.0433 843	0.0018 142	0.0418 142	0.0420 700	0.0017 567	0.0417 567	0.0414 153	0.0017 282	0.0417 282
81	0.0417 157	0.0017 413	0.0417 413	0.0404 364	0.0016 856	0.0416 856	0.0397 992	0.0016 580	0.0416 580
82	0.0401 112	0.0016 715	0.0416 715	0.0388 662	0.0016 175	0.0416 175	0.0382 453	0.0015 907	0.0415 907
83	0.0385 685	0.0016 046	0.0416 046	0.0373 570	0.0015 523	0.0415 523	0.0367 539	0.0015 263	0.0415 263
84	0.0370 851	0.0015 405	0.0415 405	0.0359 063	0.0014 897	0.0414 897	0.0353 198	0.0014 645	0.0414 645
85	0.0356 588	0 0014 791	0.0414 791	0.0345 121	0.0014 298	0.0414 298	0.0339 416	0.0014 054	0.0414 054
86	0.0342 873	0.0014 202	0.0414 202	0.0331 719	0.0013 724	0.0413 724	0.0326 173	0.0013 487	0.0413 487
87	0.0329 685	0.0013 637	0.0413 637	0.0318 838	0.0013 174	0.0413 174	0.0313 445	0.0012 944	0.0412 944
88	0.0317 005	0.0013 095	0.0413 095	0.0306 457	0.0012 646	0.0412 646	0.0301 215	0.0012 423	0.0412 423
89	0.0304 813	0.0012 576	0.0412 576	0.0294 557	0.0012 140	0.0412 140	0.0289 462	0.0011 924	0.0411 924
90	0.0293 089	0.0012 078	0.0412 078	0.0283 119	0.0011 655	0.0411 655	0.0278 167	0.0011 445	0.0411 445
91	0.0281 816	0.0011 600	0.0411 600	0.0272 125	0.0011 190	0.0411 190	0.0267 313	0.0010 986	0.0410 986
92	0.0270 977	0.0011 141	0.0411 141	0.0261 558	0.0010 743	0.0410 743	0.0256 882	0.0010 546	0.0410 546
93	0.0260 555	0.0010 701	0.0410 701	0.0251 402	0.0010 315	0.0410 315	0.0246 859	0.0010 124	0.0410 124
94	0.0250 534	0.0010 279	0.0410 279	0.0241 639	0.0009 905	0.0409 905	0.0237 227	0.0009 720	0.0409 720
95	0.0240 898	0.0009 874	0.0409 874	0.0232 256	0.0009 511	0.0409 511	0.0227 970	0.0009 332	0.0409 332
96	0.0231 632	0.0009 485	0.0409 485	0.0223 237	0.0009 133	0.0409 133	0.0219 075	0.0008 959	0.0408 959
97	0.0222 723	0.0009 112	0.0409 112	0.0214 569	0.0008 771	0.0408 771	0.0210 527	0.0008 602	0.0408 602
98	0.0214 157	0.0008 754	0.0408 754	0.0206 237	0.0008 423	0.0408 423	0.0202 312	0.0008 260	0.0408 260
99	0.0205 920	0.0008 410	0.0408 410	0.0198 228	0.0008 089	0.0408 089	0.0194 418	0.0007 931	0.0407 931
100	0.0198 000	0.0008 080	0.0408 080	0.0190 531	0.0007 769	0.0407 769	0.0186 832	0.0007 616	0.0407 616
	Ratio of Perpetual Ann.		0.0400 000	- - - - - - - - - -		0.0400 000	- - - - - - - - - -		0.0400 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0425.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02125.			RATIO *of* INTEREST: *QUARTERLY*, 0.010625.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
$\frac{1}{4}$	....	....	....	....	....	....	1.0106 250	0.2500 000	0.2473 72
$\frac{1}{2}$	....	....	....	1.0212 500	0.5000 000	0.4895 96	1.0213 629	0.5026 563	0.4921 43
$\frac{3}{4}$	....	....	....	....	....	....	1.0322 149	0.7579 970	0.7343 40
1	1.0425 000	1.0000 000	0.9592 33	1.0429 516	1.0106 250	0.9690 05	1.0431 822	1.0160 507	0.9739 92
$\frac{1}{4}$	....	....	....	....	....	....	1.0542 660	1.2768 462	1.2111 23
$\frac{1}{2}$	....	....	....	1.0651 143	1.5321 008	1.4384 38	1.0654 675	1.5404 127	1.4457 62
$\frac{3}{4}$	....	....	....	....	....	....	1.0767 881	1.8067 796	1.6779 34
2	1.0868 063	2.0425 000	1.8793 60	1.0877 480	2.0646 579	1.8981 03	1.0882 290	2.0759 766	1.9076 65
$\frac{1}{4}$	....	....	....	....	....	....	1.0997 914	2.3480 339	2.1349 81
$\frac{1}{2}$	....	....	....	1.1108 626	2.6085 319	2.3482 04	1.1114 767	2.6229 818	2.3599 07
$\frac{3}{4}$	....	....	....	....	....	....	1.1232 862	2.9008 509	2.5824 68
3	1.1329 955	3.1293 063	2.7619 76	1.1344 684	3.1639 632	2.7889 39	1.1352 211	3.1816 725	2.8026 90
$\frac{1}{4}$	....	....	....	....	....	....	1.1472 828	3.4654 777	3.0205 96
$\frac{1}{2}$	....	....	....	1.1585 759	3.7311 974	3.2205 03	1.1594 727	3.7522 984	3.2362 11
$\frac{3}{4}$	....	....	....	....	....	....	1.1717 921	4.0421 666	3.4495 60
4	1.1811 478	4.2623 018	3.6086 10	1.1831 956	4.3104 854	3.6430 88	1.1842 424	4.3351 146	3.6606 65
$\frac{1}{4}$	....	....	....	....	....	....	1.1968 249	4.6311 752	3.8695 51
$\frac{1}{2}$	....	....	....	1.2083 385	4.9020 832	4.0568 79	1.2095 412	4.9303 815	4.0762 41
$\frac{3}{4}$	....	....	....	....	....	....	1.2223 926	5.2327 668	4.2807 58
5	1.2313 466	5.4434 496	4.4207 29	1.2340 157	5.5062 525	4.4620 60	1.2353 805	5.5383 649	4.4831 25
$\frac{1}{4}$	....	....	....	....	....	....	1.2485 064	5.8472 100	4.6833 64
$\frac{1}{2}$	....	....	....	1.2602 386	6.1232 603	4.8588 10	1.2617 718	6.1593 366	4.8814 98
$\frac{3}{4}$	....	....	....	....	....	....	1.2751 781	6.4747 796	5.0775 49
6	1.2836 788	6.6747 962	5.1997 40	1.2870 186	6.7533 796	5.2473 05	1.2887 269	6.7935 741	5.2715 39
$\frac{1}{4}$	....	....	....	....	....	....	1.3024 196	7.1157 559	5.4634 90
$\frac{1}{2}$	....	....	....	1.3143 678	7.3968 889	5.6277 16	1.3162 578	7.4413 608	5.6534 22
$\frac{3}{4}$	....	....	....	....	....	....	1.3302 431	7.7704 252	5.8413 58
7	1.3382 352	7.9584 750	5.9469 93	1.3422 981	8.0540 728	6.0002 12	1.3443 769	8.1029 860	6.0273 17
$\frac{1}{4}$	....	....	....	....	....	....	1.3586 609	8.4390 802	6.2113 22
$\frac{1}{2}$	....	....	....	1.3708 219	8.7252 219	6.3649 56	1.3730 967	8.7787 454	6.3933 92
$\frac{3}{4}$	....	....	....	....	....	....	1.3876 858	9.1220 196	6.5735 48
8	1.3951 102	9.2967 102	6.6637 82	1.3999 519	9.4106 328	6.7221 12	1.4024 300	9.4689 411	6.7518 10
$\frac{1}{4}$	....	....	....	....	....	....	1.4173 308	9.8195 486	6.9281 98
$\frac{1}{2}$	....	....	....	1.4297 009	10.110 609	7.0718 35	1.4323 900	10.173 881	7.1027 32
$\frac{3}{4}$	....	....	....	....	....	....	1.4476 091	10.531 979	7.2754 30
9	1.4544 024	10.691 820	7.3513 50	1.4600 820	10.825 459	7.4142 82	1.4629 899	10.893 881	7.4463 13
$\frac{1}{4}$	....	....	....	....	....	....	1.4785 342	11.259 629	7.6154 00
$\frac{1}{2}$	....	....	....	1.4911 088	11.555 500	7.7496 03	1.4942 436	11.629 262	7.7827 08
$\frac{3}{4}$	....	....	....	....	....	....	1.5101 200	12.002 823	7.9482 58
10	1.5162 145	12.146 223	8.0108 87	1.5227 948	12.301 055	8.0779 46	1.5261 650	12.380 353	8.1120 67
$\frac{1}{4}$	....	....	....	....	....	....	1.5423 805	12.761 894	8.2741 54
$\frac{1}{2}$	....	....	....	1.5551 542	13.062 452	8.3994 58	1.5587 683	13.147 489	8.4345 37
$\frac{3}{4}$	....	....	....	....	....	....	1.5753 302	13.537 181	8.5932 34
11	1.5806 536	13.662 437	8.6435 37	1.5882 012	13.840 029	8.7142 79	1.5920 681	13.931 014	8.7502 63
$\frac{1}{4}$	....	....	....	....	....	....	1.6089 838	14.329 031	8.9056 40
$\frac{1}{2}$	....	....	....	1.6219 505	14.634 130	9.0225 50	1.6260 793	14.731 277	9.0593 84
$\frac{3}{4}$	....	....	....	....	....	....	1.6433 564	15.137 797	9.2115 12
12	1.6478 314	15.243 091	9.2503 95	1.6564 170	15.445 105	9.3244 06	1.6608 170	15.548 636	9.3620 40
$\frac{1}{4}$	....	....	....	....	....	....	1.6784 632	15.963 840	9.5109 86
$\frac{1}{2}$	....	....	....	1.6916 158	16.273 313	9.6199 82	1.6962 969	16.383 456	9.6583 66
$\frac{3}{4}$	....	....	....	....	....	....	1.7143 200	16.807 539	9.8041 97
13	1.7178 642	16.890 922	9.8325 13	1.7275 627	17.119 121	9.9094 07	1.7325 347	17.236 110	9.9484 94
$\frac{1}{4}$	....	....	....	....	....	....	1.7509 429	17.669 244	10.091 27
$\frac{1}{2}$	....	....	....	1.7642 734	17.982 903	10.192 81	1.7695 466	18.106 980	10.232 55
$\frac{3}{4}$	....	....	....	....	....	....	1.7883 481	18.549 366	10.372 35
14	1.7908 734	18.608 786	10.390 90	1.8017 642	18.865 039	10.470 32	1.8073 493	18.996 453	10.510 67
$\frac{1}{4}$	....	....	....	....	....	....	1.8265 523	19.448 291	10.647 54
$\frac{1}{2}$	....	....	....	1.8400 517	19.765 921	10.742 05	1.8459 595	19.904 929	10.782 97
$\frac{3}{4}$	....	....	....	....	....	....	1.8655 728	20.366 418	10.916 98
15	1.8669 855	20.399 660	10.926 52	1.8791 528	20.685 947	11.008 12	1.8853 945	20.832 812	11.049 58
$\frac{1}{4}$	....	....	....	....	....	....	1.9054 268	21.304 160	11.180 78
$\frac{1}{2}$	....	....	....	1.9190 848	21.625 524	11.268 67	1.9256 720	21.780 517	11.310 61
$\frac{3}{4}$	....	....	....	....	....	....	1.9461 322	22.261 935	11.439 07
16	1.9463 324	22.266 645	11.440 31	1.9598 653	22.585 066	11.523 78	1.9668 099	22.748 468	11.566 18
17	2.0290 516	24.212 978	11.933 15	2.0440 446	24.565 755	12.018 21	2.0517 410	24.746 847	12.061 39
18	2.1152 862	26.242 029	12.405 90	2.1318 395	26.631 517	12.492 27	2.1403 396	26.831 519	12.536 10
19	2.2051 859	28.357 316	12.859 38	2.2234 053	28.786 008	12.946 81	2.2327 641	29.006 213	12.991 17
20	2.2989 063	30.562 501	13.294 37	2.3189 041	31.033 037	13.382 63	2.3291 796	31.274 814	13.427 40
21	2.3966 098	32.861 408	13.711 62	2.4185 046	33.376 579	13.800 50	2.4297 586	33.641 379	13.845 56
22	2.4984 657	35.258 018	14.111 87	2.5223 832	35.820 780	14.201 17	2.5346 808	36.110 137	14.246 42
23	2.6046 505	37.756 483	14.495 80	2.6307 235	38.369 964	14.585 33	2.6441 338	38.685 501	14.630 69
24	2.7153 482	40.361 134	14.864 08	2.7437 172	41.028 639	14.953 67	2.7583 132	41.372 075	14.999 05
25	2.8307 505	43.076 482	15.217 34	2.8615 641	43.801 508	15.306 84	2.8774 231	44.174 661	15.352 16

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0425.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02125.			RATIO *of* INTEREST: *QUARTERLY*, 0.010625.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
0¼	....	....	....	....	....	....	0.9894 867	4.0000 000	4.0425 000
½	....	....	....	0.9791 921	2.0000 000	2.0425 000	0.9790 840	1.9894 933	2.0319 933
¾	....	....	....	....	....	....	0.9687 906	1.3192 665	1.3617 665
1	0.9592 326	1.0000 000	1.0425 000	0.9588 173	0.9894 867	1.0319 867	0.9586 053	0.9842 028	1.0267 028
1¼	....	....	....	....	....	....	0.9485 273	0.7831 797	0.8256 797
1½	....	....	....	0.9388 664	0.6526 985	0.6951 985	0.9385 551	0.6491 767	0.6916 767
1¾	....	....	....	....	....	....	0.9286 878	0.5534 710	0.5959 710
2	0.9201 272	0.4895 961	0.5320 961	0.9193 306	0.4843 417	0.5268 417	0.9189 242	0.4817 010	0.5242 010
2¼	....	....	....	....	....	....	0.9092 637	0.4258 883	0.4683 883
2½	....	....	....	0.9002 013	0.3833 574	0.4258 574	0.8997 040	0.3812 455	0.4237 455
2¾	....	....	....	....	....	....	0.8902 451	0.3447 264	0.3872 264
3	0.8826 161	0.3195 597	0.3620 597	0.8814 701	0.3160 593	0.3585 593	0.8808 857	0.3143 001	0.3568 001
3¼	....	....	....	....	....	....	0.8716 247	0.2885 605	0.3310 605
3½	....	....	....	0.8631 286	0.2680 105	0.3105 105	0.8624 610	0.2665 043	0.3090 043
3¾	....	....	....	....	....	....	0.8533 938	0.2473 921	0.2898 921
4	0.8466 341	0.2345 150	0.2771 150	0.8451 688	0.2319 924	0.2744 924	0.8444 217	0.2306 744	0.2731 744
4¼	....	....	....	....	....	....	0.8355 441	0.2159 279	0.2584 279
4½	....	....	....	0.8275 827	0.2039 949	0.2464 949	0.8267 597	0.2028 240	0.2453 240
4¾	....	....	....	....	....	....	0.8180 678	0.1911 035	0.2336 035
5	0.8121 190	0.1837 070	0.2262 070	0.8103 624	0.1816 117	0.2241 117	0.8094 672	0.1805 587	0.2230 587
5¼	....	....	....	....	....	....	0.8009 570	0.1710 217	0.2135 217
5½	....	....	....	0.7935 005	0.1633 117	0.2058 117	0.7925 363	0.1623 552	0.2048 552
5¾	....	....	....	....	....	....	0.7842 042	0.1544 454	0.1969 454
6	0.7790 111	0.1498 173	0.1923 173	0.7769 895	0.1480 740	0.1905 740	0.7759 596	0.1471 983	0.1896 983
6¼	....	....	....	....	....	....	0.7678 017	0.1405 332	0.1830 332
6½	....	....	....	0.7608 221	0.1351 920	0.1776 920	0.7597 296	0.1343 840	0.1768 840
6¾	....	....	....	....	....	....	0.7517 423	0.1286 931	0.1711 931
7	0.7472 528	0.1256 522	0.1681 522	0.7449 910	0.1241 608	0.1666 608	0.7438 390	0.1234 113	0.1659 113
7¼	....	....	....	....	....	....	0.7360 188	0.1184 963	0.1609 963
7½	....	....	....	0.7294 894	0.1146 103	0.1571 103	0.7282 808	0.1139 115	0.1564 115
7¾	....	....	....	....	....	....	0.7206 242	0.1096 248	0.1521 248
8	0.7167 893	0.1075 649	0.1500 649	0.7143 104	0.1062 628	0.1487 628	0.7130 481	0.1056 084	0.1481 084
8¼	....	....	....	....	....	....	0.7055 515	0.1018 377	0.1443 377
8½	....	....	....	0.6994 470	0.0989 060	0.1414 060	0.6981 339	0.0982 909	0.1407 909
8¾	....	....	....	....	....	....	0.6907 942	0.0949 489	0.1374 489
9	0.6875 676	0.0935 294	0.1360 294	0.6848 930	0.0923 748	0.1348 748	0.6835 317	0.0917 947	0.1342 947
9¼	....	....	....	....	....	....	0.6763 456	0.0888 129	0.1313 129
9½	....	....	....	0.6706 419	0.0865 389	0.1290 389	0.6692 349	0.0859 900	0.1284 900
9¾	....	....	....	....	....	....	0.6621 991	0.0833 137	0.1258 137
10	0.6595 373	0.0823 301	0.1248 301	0.6566 873	0.0812 938	0.1237 938	0.6552 372	0.0807 732	0.1232 732
10¼	....	....	....	....	....	....	0.6483 485	0.0783 583	0.1208 583
10½	....	....	....	0.6430 231	0.0765 553	0.1190 553	0.6415 322	0.0760 601	0.1185 601
10¾	....	....	....	....	....	....	0.6347 876	0.0738 706	0.1163 706
11	0.6326 497	0.0731 934	0.1156 934	0.6296 431	0.0722 542	0.1147 542	0.6281 139	0.0717 823	0.1142 823
11¼	....	....	....	....	....	....	0.6215 103	0.0697 884	0.1122 884
11½	....	....	....	0.6165 416	0.0683 334	0.1108 334	0.6149 762	0.0678 828	0.1103 828
11¾	....	....	....	....	....	....	0.6085 108	0.0660 598	0.1085 598
12	0.6068 582	0.0656 035	0.1081 035	0.6037 127	0.0647 455	0.1072 455	0.6021 133	0.0643 143	0.1068 143
12¼	....	....	....	....	....	....	0.5957 831	0.0626 416	0.1051 416
12½	....	....	....	0.5911 508	0.0614 503	0.1039 503	0.5895 195	0.0610 372	0.1035 372
12¾	....	....	....	....	....	....	0.5833 230	0.0594 971	0.1019 971
13	0.5821 182	0.0592 034	0.1017 034	0.5788 502	0.0584 142	0.1009 142	0.5771 890	0.0580 177	0.1005 177
13¼	....	....	....	....	....	....	0.5711 208	0.0565 955	0.0990 955
13½	....	....	....	0.5668 056	0.0556 084	0.0981 084	0.5651 165	0.0552 273	0.0977 273
13¾	....	....	....	....	....	....	0.5591 753	0.0539 102	0.0964 102
14	0.5583 868	0.0537 381	0.0962 381	0.5550 116	0.0530 081	0.0955 081	0.5532 965	0.0526 414	0.0951 414
14¼	....	....	....	....	....	....	0.5474 795	0.0514 184	0.0939 184
14½	....	....	....	0.5434 630	0.0505 921	0.0930 921	0.5417 237	0.0502 388	0.0927 388
14¾	....	....	....	....	....	....	0.5360 284	0.0491 004	0.0916 004
15	0.5356 228	0.0490 204	0.0915 204	0.5321 547	0.0483 420	0.0908 420	0.5303 930	0.0480 012	0.0905 012
15¼	....	....	....	....	....	....	0.5248 168	0.0469 392	0.0894 392
15½	....	....	....	0.5210 817	0.0462 417	0.0887 417	0.5192 992	0.0459 126	0.0884 126
15¾	....	....	....	....	....	....	0.5138 397	0.0449 197	0.0874 197
16	0.5137 869	0.0449 104	0.0874 104	0.5102 392	0.0442 770	0.0867 770	0.5084 375	0.0439 590	0.0864 590
17	0.4928 411	0.0413 002	0.0838 002	0.4892 261	0.0407 071	0.0832 071	0.4873 910	0.0404 092	0.0829 092
18	0.4727 493	0.0381 068	0.0806 068	0.4690 785	0.0375 495	0.0800 495	0.4672 156	0.0372 696	0.0797 696
19	0.4534 765	0.0352 643	0.0777 643	0.4497 606	0.0347 391	0.0772 391	0.4478 753	0.0344 754	0.0769 754
20	0.4349 894	0.0327 198	0.0752 198	0.4312 382	0.0322 237	0.0747 237	0.4293 357	0.0319 746	0.0744 746
21	0.4172 561	0.0304 308	0.0729 308	0.4134 786	0.0299 611	0.0724 611	0.4115 635	0.0297 253	0.0722 253
22	0.4002 456	0.0283 623	0.0708 623	0.3964 505	0.0279 168	0.0704 168	0.3945 270	0.0276 931	0.0701 931
23	0.3839 287	0.0264 855	0.0689 855	0.3801 236	0.0260 621	0.0685 621	0.3781 957	0.0258 495	0.0683 495
24	0.3682 769	0.0247 763	0.0672 763	0.3644 691	0.0243 732	0.0668 732	0.3625 404	0.0241 709	0.0666 709
25	0.3532 632	0.0232 145	0.0657 145	0.3494 592	0.0228 303	0.0653 303	0.3475 332	0.0226 374	0.0651 374

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0425.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02125.			RATIO *of* INTEREST: *QUARTERLY*, 0.010625.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	2.9510 574	45.907 233	15.556 20	2.9844 727	46.693 476	15.645 47	3.0016 764	47.098 269	15.690 65
27	3.0764 773	48.858 290	15.881 25	3.1126 605	49.709 659	15.970 16	3.1312 953	50.148 124	16.015 14
28	3.2072 276	51.934 767	16.193 04	3.2463 541	52.855 391	16.281 46	3.2665 114	53.329 679	16.326 19
29	3.3435 348	55.141 995	16.492 13	3.3857 901	56.136 238	16.579 95	3.4075 664	56.648 620	16.624 37
30	3.4856 350	58.485 530	16.779 02	3.5312 151	59.558 002	16.866 15	3.5547 124	60.110 880	16.910 20
31	3.6337 745	61.971 165	17.054 21	3.6828 863	63.126 737	17.140 56	3.7082 125	63.722 648	17.184 19
32	3.7882 099	65.604 939	17.318 19	3.8410 720	66.848 753	17.403 67	3.8683 412	67.490 380	17.446 85
33	3.9492 088	69.393 149	17.571 41	4.0060 521	70.730 637	17.655 94	4.0353 845	71.420 811	17.698 64
34	4.1170 502	73.342 358	17.814 30	4.1781 183	74.779 253	17.897 82	4.2096 411	75.520 966	17.940 00
35	4.2920 248	77.459 408	18.047 29	4.3575 750	79.001 764	18.129 75	4.3914 224	79.798 175	18.171 38
36	4.4744 359	81.751 433	18.270 78	4.5447 396	83.405 638	18.352 13	4.5810 535	84.260 082	18.393 17
37	4.6645 994	86.225 869	18.485 16	4.7399 433	87.998 666	18.565 35	4.7788 733	88.914 665	18.605 78
38	4.8628 449	90.890 468	18.690 80	4.9435 313	92.788 971	18.769 78	4.9852 353	93.770 242	18.809 59
39	5.0695 158	95.753 313	18.888 06	5.1558 637	97.785 027	18.965 79	5.2005 085	98.835 494	19.004 97
40	5.2849 702	100.82 283	19.077 28	5.3773 161	102.99 567	19.153 73	5.4250 777	104.11 947	19.192 26
41	5.5095 815	106.10 780	19.258 78	5.6082 802	108.43 012	19.333 93	5.6593 442	109.63 163	19.371 79
42	5.7437 387	111.61 738	19.432 88	5.8491 646	114.09 799	19.506 72	5.9037 269	115.38 181	19.543 89
43	5.9878 476	117.36 112	19.599 88	6.1003 953	120.00 930	19.672 38	6.1586 625	121.38 029	19.708 87
44	6.2423 311	123.34 897	19.760 08	6.3624 168	126.17 451	19.831 22	6.4246 068	127.63 781	19.867 02
45	6.5076 302	129.59 130	19.913 75	6.6356 926	132.60 453	19.983 53	6.7020 352	134.16 553	20.018 63
46	6.7842 045	136.09 893	20.061 15	6.9207 060	139.31 073	20.129 56	6.9914 435	140.97 514	20.163 95
47	7.0725 331	142.88 313	20.202 54	7.2179 611	146.30 497	20.269 57	7.2933 491	148.07 880	20.303 27
48	7.3731 158	149.95 567	20.338 17	7.5279 838	153.59 962	20.403 82	7.6082 916	155.48 922	20.436 81
49	7.6864 732	157.32 878	20.468 27	7.8513 225	161.20 759	20.532 54	7.9368 341	163.21 963	20.564 83
50	8.0131 483	165.01 525	20.593 06	8.1885 490	169.14 233	20.655 96	8.2795 637	171.28 385	20.687 55
51	8.3537 071	173.02 840	20.712 77	8.5402 600	177.41 788	20.774 30	8.6370 931	179.69 631	20.805 18
52	8.7087 397	181.38 211	20.827 60	8.9070 775	186.04 888	20.887 76	9.0100 613	188.47 203	20.917 95
53	9.0788 611	190.09 085	20.937 74	9.2896 504	195.05 660	20.996 55	9.3991 352	197.62 671	21.026 05
54	9.4647 127	199.16 971	21.043 40	9.6886 554	204.43 895	21.100 86	9.8050 101	207.17 671	21.129 68
55	9.8669 630	208.63 442	21.144 74	10.104 798	214.23 055	21.200 87	10.228 412	217.13 910	21.229 01
56	10.286 309	218.50 139	21.241 96	10.538 815	224.44 271	21.296 77	10.670 096	227.53 168	21.324 24
57	10.723 477	228.78 770	21.335 22	10.991 474	235.09 350	21.388 71	11.130 854	238.37 304	21.415 52
58	11.179 225	239.51 117	21.424 67	11.463 575	246 20 176	21.476 87	11.611 508	249.68 255	21.503 02
59	11.654 342	250.69 040	21.510 47	11.955 953	257.78 713	21.561 40	12.112 918	261.48 043	21.586 91
60	12.149 651	262.34 474	21.592 78	12.469 480	269.87 012	21.642 45	12.635 980	273.78 777	21.667 32
61	12.666 012	274.49 439	21.671 73	13.005 064	282.47 209	21.720 16	13.181 629	286.62 657	21.744 40
62	13.204 317	287.16 040	21.747 46	13.563 652	295.61 533	21.794 67	13.750 840	300.01 977	21.818 29
63	13.765 501	300.36 472	21.820 10	14.146 232	309.32 310	21.866 11	14.344 631	313.99 132	21.889 12
64	14.350 534	314.13 022	21.889 79	14.753 834	323.61 963	21.934 61	14.964 063	328.56 619	21.957 02
65	14.960 432	328.48 075	21.956 64	15.387 535	338.53 022	22.000 29	15.610 244	343.77 044	22.022 11
66	15.596 250	343.44 119	22.020 75	16.048 453	354.08 125	22.063 26	16.284 328	359.63 124	22.084 50
67	16.259 091	359.03 744	22.082 25	16.737 759	370.30 022	22.123 64	16.987 520	376.17 694	22.144 31
68	16.950 102	375.29 653	22.141 25	17.456 672	387.21 582	22.181 54	17.721 078	393.43 712	22.201 65
69	17.670 482	392.24 663	22.197 85	18.206 464	404.85 797	22.237 05	18.486 312	411.44 323	22.256 61
70	18.421 477	409.91 711	22.252 13	18.988 450	423.25 787	22.290 27	19.284 591	430.22 567	22.309 30
71	19.204 390	428.33 859	22.304 20	19.804 044	442.44 809	22.341 30	20.117 341	449.81 979	22.359 80
72	20.020 577	447.54 298	22.354 15	20.654 658	462.46 255	22.390 23	20.986 051	470.26 003	22.408 22
73	20.871 451	467.56 356	22.402 06	21.541 808	483.33 666	22.437 15	21.892 274	491.58 292	22.454 63
74	21.758 488	488.43 501	22.448 02	22.467 062	505.10 735	22.482 13	22.837 630	513.82 658	22.499 12
75	22.683 224	510.19 350	22.492 11	23.432 058	527.81 313	22.525 26	23.823 808	537.03 077	22.541 77
76	23.647 261	532.87 672	22.534 40	24.438 501	551.49 415	22.566 61	24.852 571	561.23 697	22.582 65
77	24.652 269	556.52 398	22.574 96	25.488 173	576.19 231	22.606 26	25.925 759	586.48 844	22.621 84
78	25.699 991	581.17 625	22.613 87	26.582 930	601.95 130	22.644 28	27.045 289	612.83 032	22.659 41
79	26.792 240	606.87 624	22.651 19	27.724 708	628.81 667	22.680 73	28.213 163	640.30 971	22.695 33
80	27.930 910	633.66 848	22.687 00	28.915 528	656.83 595	22.715 68	29.431 468	668.99 570	22.729 94
81	29.117 974	661.59 939	22.721 34	30.157 495	686.05 871	22.749 19	30.702 382	698.87 957	22.763 04
82	30.355 488	690.71 736	22.754 28	31.452 807	716.53 663	22.781 32	32.028 177	730.07 475	22.794 77
83	31.645 596	721.07 285	22.785 88	32.803 754	748.32 362	22.812 13	33.411 223	762.61 700	22.825 18
84	32.990 534	752.71 845	22.816 20	34.212 726	781.47 591	22.841 67	34.853 991	796.56 450	22.854 33
85	34.392 632	785.70 898	22.845 27	35.682 216	816.05 215	29 869 99	36.359 062	831.97 792	22.882 27
86	35.854 319	820.10 161	22.873 16	37.214 823	852.11 349	22.897 15	37.929 124	868.92 057	22.909 06
87	37.378 127	855.95 593	22.899 92	38.813 258	889.72 372	22.923 19	39.566 985	907.45 848	22.934 74
88	38.966 698	893.33 406	22.925 58	40.480 348	928.94 937	22.948 15	41.275 573	947.66 054	22.959 35
89	40.622 782	932.30 076	22.950 20	42.219 042	969.85 982	22.972 09	43.057 941	989.59 862	22.982 95
90	42.349 250	972.92 354	22.973 81	44.032 416	1012.5 274	22.995 04	44.917 276	1033.3 477	23.005 57
91	44.149 094	1015.2 728	22.996 46	45.923 677	1057.0 277	23.017 05	46.856 901	1078.9 859	23.027 26
92	46.025 430	1059.4 219	23.018 19	47.896 171	1103.4 393	23.038 15	48.880 283	1126.5 949	23.048 04
93	47.981 511	1105.4 473	23.039 03	49.953 386	1151.8 444	23.058 38	50.991 039	1176.2 597	23.067 97
94	50.020 725	1153.4 288	23.059 02	52.098 962	1202.3 285	23.077 78	53.192 941	1228.0 092	23.087 07
95	52.146 606	1203.4 496	23.078 20	54.336 694	1254.9 810	23.096 38	55.489 927	1282.1 159	23.105 38
96	54.362 837	1255.5 962	23.096 59	56.670 540	1309.8 951	23.114 21	57.886 102	1338.4 965	23.122 93
97	56.673 257	1309.9 590	23.114 24	59.104 628	1367.7 677	23.131 31	60.385 748	1397.3 117	23.139 76
98	59.081 871	1366.6 323	23.131 16	61.643 264	1426.9 003	23.147 70	62.993 335	1458.6 667	23.155 89
99	61.592 850	1425.7 141	23.147 40	64.290 939	1489.1 986	23.163 43	65.713 523	1522.6 711	23.171 35
100	64.210 546	1487.3 070	23.162 97	67.052 335	1554.1 726	23.178 50	68.551 174	1589.4 394	23.186 17
	Value of Perpetual Ann.		23.529 41	- - - - - - - - - -		23.529 41	- - - - - - - - - -		23.529 41

Years.	RATIO of INTEREST: ANNUALLY, 0.0425.			RATIO of INTEREST: HALF-YEARLY, 0.02125.			RATIO of INTEREST: QUARTERLY, 0.010625.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.3388 616	0.0217 831	0.0642 831	0.3350 676	0.0214 163	0.0639 163	0.3331 472	0.0212 322	0.0637 322
27	0.3250 471	0.0204 674	0.0629 674	0.3212 686	0.0201 168	0.0626 168	0.3193 567	0.0199 409	0.0624 409
28	0.3117 958	0.0192 549	0.0617 549	0.3080 379	0.0189 195	0.0614 195	0.3061 370	0.0187 513	0.0612 513
29	0.2990 847	0.0181 350	0.0606 350	0.2953 520	0.0178 138	0.0603 138	0.2934 646	0.0176 527	0.0601 527
30	0.2868 918	0.0170 982	0.0595 982	0.2831 887	0.0167 903	0.0592 903	0.2813 167	0.0166 359	0.0591 359
31	0.2751 959	0.0161 365	0.0586 365	0.2715 262	0.0158 411	0.0583 411	0.2696 717	0.0156 930	0.0581 930
32	0.2639 769	0.0152 428	0.0577 428	0.2603 440	0.0149 591	0.0574 591	0.2585 088	0.0148 169	0.0573 169
33	0.2532 153	0.0144 106	0.0569 106	0.2496 223	0.0141 381	0.0566 381	0.2478 079	0.0140 015	0.0565 015
34	0.2428 923	0.0136 347	0.0561 347	0.2393 422	0.0133 727	0.0558 727	0.2375 499	0.0132 414	0.0557 414
35	0.2329 903	0.0129 100	0.0554 100	0.2294 854	0.0126 579	0.0551 579	0.2277 166	0.0125 316	0.0550 316
36	0.2234 919	0.0122 322	0.0547 322	0.2200 346	0.0119 896	0.0544 896	0.2182 904	0.0118 680	0.0543 680
37	0.2143 807	0.0115 974	0.0540 974	0.2109 730	0.0113 638	0.0538 638	0.2092 543	0.0112 467	0.0537 467
38	0.2056 409	0.0110 023	0.0535 023	0.2022 846	0.0107 771	0.0532 771	0.2005 923	0.0106 644	0.0531 644
39	0.1972 575	0.0104 435	0.0529 435	0.1939 539	0.0102 264	0.0527 264	0.1922 889	0.0101 178	0.0526 178
40	0.1892 158	0.0099 184	0 0524 184	0.1859 664	0.0097 091	0.0522 091	0.1843 292	0.0096 044	0.0521 044
41	0.1815 020	0.0094 244	0.0519 244	0.1783 078	0.0092 225	0.0517 225	0.1766 989	0.0091 215	0.0516 215
42	0.1741 026	0.0089 592	0.0514 592	0.1709 646	0.0087 644	0.0512 644	0.1693 845	0.0086 669	0.0511 669
43	0.1670 049	0.0085 207	0.0510 207	0.1639 238	0.0083 327	0.0508 327	0.1623 729	0.0082 386	0.0507 386
44	0.1601 966	0.0081 071	0.0506 071	0.1571 730	0.0079 255	0.0504 255	0.1556 516	0.0078 347	0.0503 347
45	0.1536 658	0.0077 166	0.0502 166	0.1507 002	0.0075 412	0.0500 412	0.1492 084	0.0074 535	0.0499 535
46	0.1474 012	0.0073 476	0.0498 476	0.1444 939	0.0071 782	0.0496 782	0.1430 320	0.0070 934	0.0495 934
47	0.1413 921	0.0069 987	0.0494 987	0.1385 433	0.0068 350	0.0493 350	0.1371 112	0.0067 532	0.0492 532
48	0.1356 279	0.0066 686	0.0491 686	0.1328 377	0.0065 104	0.0490 104	0.1314 355	0.0064 313	0.0489 313
49	0.1300 987	0.0063 561	0.0488 561	0.1273 671	0.0062 032	0.0487 032	0.1259 948	0.0061 267	0.0486 267
50	0.1247 949	0.0060 600	0.0485 600	0 1221 218	0.0059 122	0.0484 122	0.1207 793	0.0058 383	0.0483 383
51	0.1197 073	0.0057 794	0.0482 794	0.1170 925	0.0056 364	0.0481 364	0.1157 797	0.0055 649	0.0480 649
52	0.1148 272	0.0055 132	0.0480 132	0.1122 703	0.0053 749	0.0478 749	0.1109 870	0.0053 058	0 0478 058
53	0.1101 460	0.0052 606	0.0477 606	0.1076 467	0.0051 269	0.0476 269	0.1063 928	0.0050 600	0.0475 600
54	0.1056 556	0.0050 208	0.0475 208	0.1032 135	0.0048 914	0.0473 914	0.1019 887	0.0048 268	0.0473 268
55	0.1013 483	0.0047 931	0.0472 931	0.0989 629	0.0046 679	0.0471 679	0.0977 669	0.0046 053	0.0471 053
56	0.0972 166	0.0045 766	0.0470 766	0.0948 873	0.0044 555	0.0469 555	0.0937 199	0.0043 950	0.0468 950
57	0.0932 533	0.0043 709	0.0468 709	0.0909 796	0.0042 536	0.0467 536	0.0898 404	0.0041 951	0.0466 951
58	0.0894 517	0.0041 752	0.0466 752	0.0872 328	0.0040 617	0.0465 617	0.0861 215	0.0040 051	0.0465 051
59	0.0858 049	0.0039 890	0.0464 890	0.0836 403	0.0038 792	0 0463 792	0.0825 565	0.0038 244	0.0463 244
60	0.0823 069	0.0038 118	0.0463 118	0.0801 958	0.0037 055	0.0462 055	0.0791 391	0.0036 525	0.0461 525
61	0.0789 515	0.0036 431	0.0461 431	0.0768 931	0.0035 402	0.0460 402	0.0758 632	0.0034 889	0.0459 889
62	0.0757 328	0.0034 824	0.0459 824	0.0737 264	0.0033 828	0.0458 828	0.0727 228	0.0033 331	0.0458 331
63	0 0726 454	0.0033 293	0 0458 293	0.0706 902	0.0032 329	0.0457 329	0.0697 125	0.0031 848	0.0456 848
64	0.0696 838	0.0031 834	0.0456 834	0.0677 790	0.0030 900	0.0455 900	0.0668 268	0.0030 435	0.0455 435
65	0.0668 430	0.0030 443	0.0455 443	0.0649 877	0.0029 539	0.0454 539	0.0640 605	0.0029 089	0.0454 089
66	0.0641 180	0.0029 117	0.0454 117	0.0623 113	0.0028 242	0.0453 242	0.0614 087	0.0027 806	0.0452 806
67	0.0615 041	0.0027 852	0.0452 852	0.0597 452	0.0027 005	0.0452 005	0.0588 667	0.0026 583	0.0451 583
68	0.0589 957	0.0026 646	0.0451 646	0.0572 847	0.0025 825	0.0450 825	0.0564 300	0.0025 417	0.0450 417
69	0.0565 916	0.0025 494	0.0450 494	0.0549 255	0.0024 700	0.0449 700	0.0540 941	0.0024 305	0.0449 305
70	0.0542 845	0.0024 395	0.0449 395	0.0526 636	0.0023 625	0.0448 626	0.0518 549	0.0023 244	0.0448 244
71	0.0520 714	0.0023 346	0.0448 346	0.0504 947	0.0022 602	0.0447 602	0.0497 084	0.0022 231	0.0447 231
72	0.0199 486	0.0022 344	0.0447 344	0.0484 152	0.0021 623	0.0446 623	0.0476 507	0.0021 265	0.0446 265
73	0.0479 123	0.0021 387	0.0446 387	0.0464 214	0.0020 689	0.0445 689	0.0456 782	0 0020 342	0.0445 342
74	0.0459 591	0.0020 474	0.0445 474	0.0445 096	0.0019 798	0.0444 798	0.0437 874	0.0019 462	0.0444 462
75	0.0440 855	0.0019 600	0.0444 600	0.0426 766	0.0018 946	0.0443 946	0.0419 748	0.0018 621	0.0443 621
76	0.0422 882	0.0018 766	0.0443 766	0.0409 190	0.0018 133	0.0443 133	0.0402 373	0.0017 818	0.0442 818
77	0.0405 642	0.0017 969	0.0442 969	0.0392 339	0.0017 355	0.0442 355	0.0385 717	0.0017 051	0.0442 051
78	0.0389 105	0.0017 206	0.0442 206	0.0376 181	0.0016 612	0.0441 612	0.0369 750	0.0016 318	0.0441 318
79	0.0373 242	0.0016 478	0.0441 478	0.0360 689	0.0015 903	0.0440 903	0.0354 444	0.0015 618	0.0440 618
80	0.0358 026	0.0015 781	0.0440 781	0.0345 835	0.0015 224	0.0440 224	0.0339 772	0.0014 948	0.0439 948
81	0.0343 430	0.0015 115	0.0440 115	0.0331 593	0.0014 576	0.0439 576	0 0325 708	0.0014 309	0.0439 309
82	0.0329 430	0.0014 478	0.0439 478	0.0317 937	0.0013 956	0.0438 956	0.0312 225	0.0013 697	0.0438 697
83	0.0316 000	0.0013 868	0.0438 868	0.0304 843	0.0013 363	0.0438 363	0.0299 301	0.0013 113	0.0438 113
84	0.0303 117	0.0013 285	0.0438 285	0.0292 289	0.0012 796	0.0437 796	0.0286 911	0.0012 554	0.0437 554
85	0.0290 760	0.0012 727	0.0437 727	0.0280 252	0.0012 254	0.0437 254	0.0275 035	0.0012 020	0.0437 020
86	0.0278 906	0.0012 194	0.0437 194	0.0268 710	0.0011 736	0.0436 736	0.0263 650	0.0011 509	0.0436 509
87	0.0267 536	0.0011 683	0.0436 683	0.0257 644	0.0011 239	0.0436 239	0.0252 736	0.0011 020	0.0436 020
88	0.0256 629	0.0011 194	0.0436 194	0.0247 033	0.0010 765	0.0435 765	0.0242 274	0.0010 552	0.0435 552
89	0.0246 167	0.0010 726	0.0435 726	0.0236 860	0.0010 311	0.0435 311	0.0232 245	0.0010 105	0.0435 105
90	0.0236 132	0.0010 278	0.0435 278	0.0227 105	0.0009 876	0.0434 876	0.0222 631	0.0009 677	0.0434 677
91	0.0226 505	0.0009 850	0.0434 850	0.0217 753	0.0009 460	0.0434 460	0.0213 416	0.0009 268	0.0434 268
92	0.0217 271	0.0009 439	0.0434 439	0.0208 785	0.0009 062	0.0434 062	0.0204 581	0.0008 876	0.0433 876
93	0.0208 414	0.0009 046	0.0434 046	0.0200 187	0.0008 682	0.0433 682	0.0196 113	0.0008 502	0.0433 502
94	0.0199 917	0.0008 670	0.0433 670	0.0191 942	0.0008 317	0.0433 317	0.0187 995	0.0008 143	0.0433 143
95	0.0191 767	0.0008 309	0.0433 309	0.0184 038	0.0007 968	0.0432 968	0.0180 213	0.0007 800	0.0432 800
96	0.0183 949	0.0007 964	0.0432 964	0.0176 459	0.0007 634	0.0432 634	0.0172 753	0.0007 471	0.0432 471
97	0.0176 450	0.0007 634	0.0432 634	0.0169 192	0.0007 314	0.0432 314	0.0165 602	0.0007 157	0.0432 157
98	0.0169 257	0.0007 317	0.0432 317	0.0162 224	0.0007 008	0.0432 008	0.0158 747	0.0006 856	0 0431 856
99	0.0162 357	0.0007 014	0.0432 014	0.0155 543	0.0006 715	0.0431 715	0.0152 176	0.0006 567	0.0431 567
100	0.0155 738	0.0006 724	0.0431 724	0.0149 137	0.0006 434	0.0431 434	0.0145 876	0.0006 292	0.0431 292
	Ratio of Perpetual Ann.		0.0425 000	- - - - - - - - - -		0.0425 000	- - - - - - - -		0.0425 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.045.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.0225.			RATIO *of* INTEREST: *QUARTERLY*, 0.01125.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
$\frac{1}{4}$	....	....	....	....	....	....	1.0112 500	0.2500 000	0.2472 19
$\frac{1}{2}$	....	....	....	1.0225 000	0.5000 000	0.4889 98	1.0226 266	0.5028 125	0.4916 87
$\frac{3}{4}$	....	....	....	....	....	....	1.0341 311	0.7584 691	0.7334 36
1	1.0450 000	1.0000 000	0.9569 38	1.0455 063	1.0112 500	0.9672 35	1.0457 651	1.0170 019	0.9724 96
$\frac{1}{4}$	....	....	....	....	....	....	1.0575 299	1.2784 432	1.2088 96
$\frac{1}{2}$	....	....	....	1.0690 301	1.5340 031	1.4349 48	1.0694 272	1.5428 257	1.4426 66
$\frac{3}{4}$	....	....	....	....	....	....	1.0814 582	1.8101 825	1.6738 35
2	1.0920 250	2.0450 000	1.8726 68	1.0930 833	2.0685 182	1.8923 70	1.0936 246	2.0805 470	1.9024 32
$\frac{1}{4}$	....	....	....	....	....	....	1.1059 279	2.3539 532	2.1284 87
$\frac{1}{2}$	....	....	....	1.1176 777	2.6150 599	2.3397 26	1.1183 696	2.6304 351	2.3520 27
$\frac{3}{4}$	....	....	....	....	....	....	1.1309 512	2.9100 275	2.5730 80
3	1.1411 661	3.1370 250	2.7489 64	1.1428 254	3.1738 987	2.7772 38	1.1436 744	3.1927 653	2.7916 73
$\frac{1}{4}$	....	....	....	....	....	....	1.1565 408	3.4786 840	3.0078 35
$\frac{1}{2}$	....	....	....	1.1685 390	3.7453 114	3.2051 23	1.1695 519	3.7678 192	3.2215 92
$\frac{3}{4}$	....	....	....	....	....	....	1.1827 093	4.0602 071	3.4329 71
4	1.1925 186	4.2781 911	3.5875 26	1.1948 311	4.3295 809	3.6235 92	1.1960 148	4.3558 844	3.6419 99
$\frac{1}{4}$	....	....	....	....	....	....	1.2094 709	4.6548 881	3.8487 01
$\frac{1}{2}$	....	....	....	1.2217 148	4.9269 965	4.0328 53	1.2230 765	4.9572 556	4.0531 03
$\frac{3}{4}$	....	....	....	....	....	....	1.2368 361	5.2030 248	4.2552 32
5	1.2461 819	5.4707 097	4.3899 77	1.2492 034	5.5378 539	4.4331 08	1.2507 505	5.5722 338	4.4551 12
$\frac{1}{4}$	....	....	....	....	....	....	1.2648 215	5.8849 214	4.6527 68
$\frac{1}{2}$	....	....	....	1.2773 105	6.1624 556	4.8245 56	1.2790 507	6.2011 268	4.8482 26
$\frac{3}{4}$	....	....	....	....	....	....	1.2934 400	6.5208 895	5.0415 09
6	1.3022 601	6.7168 917	5.1578 72	1.3060 500	6.8011 109	5.2073 89	1.3079 912	6.8442 495	5.2326 42
$\frac{1}{4}$	....	....	....	....	....	....	1.3227 061	7.1712 473	5.4216 48
$\frac{1}{2}$	....	....	....	1.3354 361	7.4541 359	5.5817 99	1.3375 866	7.5019 238	5.6085 52
$\frac{3}{4}$	....	....	....	....	....	....	1.3526 344	7.8363 205	5.7933 76
7	1.3608 618	8.0191 518	5.8927 01	1.3654 834	8.1218 539	5.9479 70	1.3678 516	8.1744 791	5.9761 45
$\frac{1}{4}$	....	....	....	....	....	....	1.3832 399	8.5164 420	6.1568 80
$\frac{1}{2}$	....	....	....	1.3962 068	8.8045 957	6.3060 83	1.3988 013	8.8622 519	6.3356 04
$\frac{3}{4}$	....	....	....	....	....	....	1.4145 379	9.2119 523	6.5123 41
8	1.4221 006	9.3800 136	6.5958 86	1.4276 215	9.5026 991	6.6563 16	1.4304 514	9.5655 867	6.6871 11
$\frac{1}{4}$	....	....	....	....	....	....	1.4465 440	9.9231 996	6.8599 36
$\frac{1}{2}$	....	....	....	1.4597 429	10.216 510	6.9988 42	1.4628 176	10.284 836	7.0308 39
$\frac{3}{4}$	....	....	....	....	....	....	1.4792 743	10.650 540	7.1998 41
9	1.4860 951	10.802 114	7.2687 90	1.4925 872	10.946 381	7.3338 31	1.4959 161	11.020 359	7.3669 63
$\frac{1}{4}$	....	....	....	....	....	....	1.5127 452	11.394 338	7.5322 25
$\frac{1}{2}$	....	....	....	1.5261 704	11.692 675	7.6614 48	1.5297 636	11.772 524	7.6956 49
$\frac{3}{4}$	....	....	....	....	....	....	1.5469 734	12.154 965	7.8572 55
10	1.5529 694	12.288 209	7.9127 18	1.5605 092	12.455 760	7.9818 56	1.5643 769	12.541 708	8.0170 63
$\frac{1}{4}$	....	....	....	....	....	....	1.5819 761	12.932 802	8.1750 93
$\frac{1}{2}$	....	....	....	1.5956 207	13.236 015	8.2952 14	1.5997 733	13.328 296	8.3313 66
$\frac{3}{4}$	....	....	....	....	....	....	1.6177 708	13.728 240	8.4858 99
11	1.6228 530	13.841 179	8.5289 17	1.6315 221	14.033 825	8.6016 76	1.6359 707	14.132 682	8.6387 14
$\frac{1}{4}$	....	....	....	....	....	....	1.6543 754	14.541 675	8.7898 28
$\frac{1}{2}$	....	....	....	1.6682 314	14.849 586	8.9013 95	1.6729 871	14.955 269	8.9392 64
$\frac{3}{4}$	....	....	....	....	....	....	1.6918 082	15.373 516	9.0870 32
12	1.6958 814	15.464 032	9.1185 81	1.7057 666	15.683 702	9.1945 18	1.7108 410	15.796 468	9.2321 59
$\frac{1}{4}$	....	....	....	....	....	....	1.7300 880	16.224 178	9.3776 61
$\frac{1}{2}$	....	....	....	1.7441 463	16.536 585	9.4811 91	1.7495 515	16.656 700	9.5205 54
$\frac{3}{4}$	....	....	....	....	....	....	1.7692 340	17.094 088	9.6618 58
13	1.7721 961	17.1599 13	9.6828 52	1.7833 896	17.408 658	9.7615 56	1.7891 378	17.536 396	9.8015 90
$\frac{1}{4}$	....	....	....	....	....	....	1.8092 656	17.983 681	9.9397 68
$\frac{1}{2}$	....	....	....	1.8235 159	18.300 353	10.035 75	1.8296 199	18.435 997	10.076 41
$\frac{3}{4}$	....	....	....	....	....	....	1.8502 031	18.893 402	10 211 53
14	1.8519 449	18.932 109	10.222 83	1.8645 450	19.212 111	10.303 91	1.8710 179	19.355 953	10.345 15
$\frac{1}{4}$	....	....	....	....	....	....	1.8920 668	19.823 707	10.477 28
$\frac{1}{2}$	....	....	....	1.9064 973	20.144 383	10.566 17	1.9133 526	20.296 724	10.607 94
$\frac{3}{4}$	....	....	....	....	....	....	1.9348 778	20.775 062	10.737 14
15	1.9352 824	20.784 054	10.739 55	1.9493 934	21.097 632	10.822 66	1.9566 452	21.258 782	10.864 91
$\frac{1}{4}$	....	....	....	....	....	....	1.9786 574	21.747 943	10.991 26
$\frac{1}{2}$	....	....	....	1.9932 548	22.072 329	11.073 51	2.0009 173	22.242 607	11.116 21
$\frac{3}{4}$	....	....	....	....	....	....	2.0234 277	22.742 837	11.239 76
16	2.0223 702	22.719 337	11.234 01	2.0381 030	23.068 956	11.318 84	2.0461 912	23.248 694	11.361 94
17	2.1133 768	24.741 707	11.707 19	2.1308 495	25.129 988	11.793 41	2.1398 353	25.329 674	11.837 21
18	2.2084 788	26.855 084	12.159 99	2.2278 164	27.284 809	12.247 33	2.2377 651	27.505 891	12.291 68
19	2.3078 603	29.063 562	12.593 29	2.3291 960	29.537 689	12.681 50	2.3401 766	29.781 702	12.726 26
20	2.4117 140	31.371 423	13.007 94	2.4351 890	31.893 038	13.096 76	2.4472 750	32.161 666	13.141 83
21	2.5202 412	33.783 137	13 404 72	2.5460 053	34.355 673	13.493 95	2.5592 747	34.650 550	13.539 21
22	2.6336 520	36.303 378	13.784 42	2.6618 644	36.930 321	13.873 85	2.6764 002	37.253 337	13.919 20
23	2.7521 663	38.937 030	14.147 77	2.7829 959	39.622 131	14.237 22	2.7988 858	39.975 241	14.282 56
24	2.8760 138	41.689 196	14.495 48	2.9096 396	42.436 436	14.584 77	2.9269 771	42.821 713	14.630 01
25	3.0054 345	44.565 210	14.828 21	3.0420 464	45.378 809	14.917 20	3.0609 305	45.798 454	14.962 27

Years.	RATIO of INTEREST: ANNUALLY, 0.045.			RATIO of INTEREST: HALF-YEARLY, 0.0225.			RATIO of INTEREST: QUARTERLY, 0.01125.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
½	....	....	....	....	....	....	0.9888 752	4.0000 000	4.0450 000
	....	....	....	0.9779 950	2.0000 000	2.0450 000	0.9778 741	1.9888 130	2.0338 130
1	0.9569 378	1.0000 000	1.0450 000	0.9564 744	0.9888 752	1.0338 752	0.9669 953	1.3184 452	1.3634 452
							0.9562 377	0.9832 823	1.0282 823
1½	....	....	....	....	....	....	0.9455 997	0.7822 013	0.8272 013
	....	....	....	0.9354 273	0.6518 891	0.6968 891	0.9350 800	0.6481 614	0.6931 614
	....	....	....	....	....	....	0.9246 774	0.5524 305	0.5974 305
2	0.9157 300	0.4889 976	0.5339 976	0.9148 434	0.4834 379	0.5284 379	0.9143 905	0.4806 428	0.5256 428
2½	....	....	....	....	....	....	0.9042 181	0.4248 173	0.4698 173
	....	....	....	0.8947 123	0.3823 996	0.4273 996	0.8941 588	0.3801 653	0.4251 653
	....	....	....	....	....	....	0.8842 114	0.3436 394	0.3886 394
3	0.8762 966	0.3187 734	0.3637 734	0.8750 243	0.3150 699	0.3600 699	0.8743 747	0.3132 078	0.3582 078
3½	....	....	....	....	....	....	0.8646 474	0.2874 650	0.3324 650
	....	....	....	0.8557 694	0.2670 005	0.3120 005	0.8550 283	0.2654 055	0.3104 055
	....	....	....	....	....	....	0.8455 163	0.2462 929	0.2912 929
4	0.8385 614	0.2337 437	0.2787 437	0.8369 384	0.2309 692	0.2759 692	0.8361 101	0.2295 745	0.2745 745
4½	....	....	....	....	....	....	0.8268 084	0.2148 279	0.2598 279
	....	....	....	0.8185 216	0.2029 647	0.2479 647	0.8176 104	0.2017 245	0.2467 245
	....	....	....	....	....	....	0.8085 145	0.1900 048	0.2350 048
5	0.8024 510	0.1827 919	0.2277 919	0.8005 101	0.1805 754	0.2255 754	0.7995 200	0.1794 612	0.2244 612
5½	....	....	....	....	....	....	0.7906 254	0.1699 258	0.2149 258
	....	....	....	0.7828 950	0.1622 730	0.2072 730	0.7818 298	0.1612 610	0.2062 610
	....	....	....	....	....	....	0.7731 321	0 1533 533	0.1983 533
6	0.7678 957	0.1488 784	0.1938 784	0.7656 675	0.1470 348	0.1920 348	0.7645 311	0.1461 081	0.1911 081
6½	....	....	....	....	....	....	0.7560 259	0.1394 457	0.1844 457
	....	....	....	0.7488 191	0.1341 537	0.1791 537	0.7476 152	0.1332 991	0.1782 991
	....	....	....	....	....	....	0.7392 980	0.1276 109	0.1726 109
7	0.7348 284	0.1247 015	0.1697 015	0.7323 413	0.1231 246	0.1681 246	0.7310 736	0.1223 319	0.1673 319
7½	....	....	....	....	....	....	0.7229 404	0.1174 199	0.1624 199
	....	....	....	0.7162 263	0.1135 771	0.1585 771	0.7148 978	0.1128 382	0.1578 382
	....	....	....	....	....	....	0.7069 448	0.1085 546	0.1535 546
8	0.7031 851	0.1066 097	0.1516 097	0.7004 659	0.1052 333	0.1502 333	0.6990 800	0.1045 414	0.1495 414
8½	....	....	....	....	....	....	0.6913 029	0.1007 740	0.1457 740
	....	....	....	0.6850 521	0.0978 808	0.1428 808	0.6836 122	0.0972 304	0.1422 304
	....	....	....	....	....	....	0.6760 072	0.0938 920	0.1388 920
9	0.6729 044	0.0925 745	0.1375 745	0.6699 776	0.0913 544	0.1363 544	0.6684 867	0.0907 412	0.1357 412
9½	....	....	....	....	....	....	0.6610 499	0.0877 629	0.1327 629
	....	....	....	0.6552 348	0.0855 236	0.1305 236	0.6536 958	0.0849 436	0.1299 436
	....	....	....	....	....	....	0.6464 235	0.0822 709	0.1272 709
10	0.6439 277	0.0813 788	0.1263 788	0.6408 165	0.0802 841	0.1252 841	0.6392 322	0.0797 338	0.1247 338
10½	....	....	....	....	....	....	0.6321 208	0.0773 228	0.1223 228
	....	....	....	0.6267 153	0.0755 514	0.1205 514	0.6250 885	0.0750 283	0.1200 283
	....	....	....	....	....	....	0.6181 345	0.0728 425	0.1178 425
11	0.6161 988	0.0722 482	0.1172 482	0.6129 246	0.0712 564	0.1162 564	0.6112 579	0.0707 580	0.1157 580
11½	....	....	....	....	....	....	0.6044 577	0.0687 679	0.1137 679
	....	....	....	0.5994 372	0.0673 419	0.1123 419	0.5977 332	0.0668 661	0.1118 661
	....	....	....	....	....	....	0.5910 835	0.0650 469	0.1100 469
12	0.5896 639	0.0646 662	0.1096 662	0.5862 467	0.0637 605	0.1087 605	0.5845 078	0.0633 053	0.1083 053
12½	....	....	....	....	....	....	0.5780 053	0.0616 364	0.1066 364
	....	....	....	0.5733 464	0.0604 720	0.1054 720	0.5715 751	0.0600 355	0.1050 355
	....	....	....	....	....	....	0.5652 164	0.0584 998	0.1034 998
13	0.5642 716	0.0582 754	0.1032 754	0.5607 300	0.0574 427	0.1024 427	0.5589 284	0.0570 243	0.1020 243
13½	....	....	....	....	....	....	0.5527 104	0.0556 060	0.1006 060
	....	....	....	0.5483 912	0.0546 438	0.0996 438	0.5465 616	0.0542 417	0.0992 417
	....	....	....	....	....	....	0.5404 812	0.0529 285	0.0979 285
14	0.5399 728	0.0528 203	0.0978 203	0.5363 239	0.0520 505	0.0970 505	0.5344 684	0.0516 637	0.0966 637
14½	....	....	....	....	....	....	0.5285 226	0.0504 446	0.0954 446
	....	....	....	0.5245 221	0.0496 416	0.0946 416	0.5226 428	0.0492 690	0.0942 690
	....	....	....	....	....	....	0.5168 285	0.0481 344	0.0931 344
15	0.5167 204	0.0481 138	0.0931 138	0.5129 801	0.0473 987	0.0923 987	0.5110 789	0.0470 394	0.0920 394
15½	....	....	....	....	....	....	0.5053 932	0.0459 814	0.0909 814
	....	....	....	0.5016 920	0.0453 056	0.0903 056	0.4997 708	0.0449 588	0.0899 588
	....	....	....	....	....	....	0.4942 109	0.0439 699	0.0889 699
16	0.4944 693	0.0440 154	0.0890 154	0.4906 523	0.0433 483	0.0883 483	0.4887 129	0.0430 132	0.0880 132
17	0.4731 764	0.0404 176	0.0854 176	0.4692 964	0.0397 931	0.0847 931	0.4673 257	0.0394 794	0.0844 794
18	0.4528 004	0.0372 369	0.0822 369	0.4488 700	0.0366 504	0.0816 504	0.4468 744	0.0363 559	0.0813 559
19	0.4333 018	0.0344 073	0.0794 073	0.4293 327	0.0338 551	0.0788 551	0.4273 182	0.0335 777	0.0785 777
20	0.4146 429	0.0318 761	0.0768 761	0.4106 458	0.0313 548	0.0763 548	0.4086 178	0.0310 929	0.0760 929
21	0.3967 874	0.0296 006	0.0746 006	0.3927 721	0.0291 073	0.0741 073	0.3907 357	0.0288 596	0.0738 596
22	0.3797 009	0.0275 456	0.0725 456	0.3756 765	0.0270 780	0.0720 780	0.3736 362	0.0268 432	0.0718 432
23	0.3633 501	0.0256 825	0.0706 825	0.3593 250	0.0252 384	0.0702 384	0.3572 850	0.0250 155	0.0700 155
24	0.3477 035	0.0239 870	0.0689 870	0.3436 852	0.0235 647	0.0685 647	0.3416 494	0.0233 526	0.0683 526
25	0.3327 306	0.0224 390	0.0674 390	0.3287 261	0.0220 367	0.0670 367	0.3266 981	0.0218 348	0.0668 348

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.045.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.0225.			RATIO *of* INTEREST: *QUARTERLY*, 0.01125.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	3.1406 790	47.570 645	15.146 61	3.1804 785	48.455 078	15.235 15	3.2010 142	48.911 427	15.279 98
27	3.2820 096	50.711 324	15.451 30	3.3252 102	51.671 337	15.539 27	3.3475 089	52.166 864	15.583 79
28	3.4297 000	53.993 333	15.742 87	3.4765 280	55.033 956	15.830 15	3.5007 079	55.571 287	15.874 30
29	3.5840 365	57.423 033	16.021 89	3.6347 318	58.549 595	16.108 37	3.6609 181	59.131 514	16.152 10
30	3.7453 181	61.007 070	16.288 89	3.8001 348	62.225 217	16.374 48	3.8284 604	62.854 675	16.417 74
31	3.9138 575	64.752 388	16.544 39	3.9730 647	66.068 104	16.629 00	4.0036 702	66.748 226	16.671 76
32	4.0899 810	68.666 245	16.788 89	4.1538 639	70.085 865	16.872 49	4.1868 985	70.819 966	16.914 66
33	4.2740 302	72.756 226	17.022 86	4.3428 907	74.286 460	17.105 30	4.3785 123	75.078 050	17.146 93
34	4.4663 615	77.030 256	17.246 76	4.5405 194	78.678 209	17.328 02	4.5788 952	79.531 006	17.369 04
35	4.6673 478	81.496 618	17.461 01	4.7471 414	83.269 809	17.541 04	4.7884 488	84.187 751	17.581 42
36	4.8773 785	86.163 966	17.666 04	4.9631 660	88.070 355	17.744 79	5.0075 926	89.057 612	17.784 51
37	5.0968 605	91.041 344	17.862 24	5.1890 211	93.089 357	17.939 68	5.2367 655	94.150 344	17.978 72
38	5.3262 192	96.138 205	18.049 99	5.4251 540	98.336 755	18.126 08	5.4764 265	99.476 144	18.164 43
39	5.5658 991	101.46 442	18.229 66	5.6720 324	103.82 294	18 304 36	5.7270 556	105.04 568	18.342 00
40	5.8163 645	107.03 032	18.401 58	5.9301 453	109.55 878	18.474 89	5.9891 548	110.87 011	18.511 81
41	6.0781 009	112.84 669	18.566 11	6.2000 040	115.55 564	18.637 99	6.2632 490	116.96 109	18.674 19
42	6.3516 155	118.92 479	18.723 55	6.4821 429	121.82 540	18.794 00	6.5498 871	123.33 083	18.829 47
43	6.6374 382	125.27 640	18.874 21	6.7771 209	128.38 046	18.943 22	6.8496 433	129.99 207	18.977 94
44	6.9361 229	131.91 384	19.018 38	7.0855 223	135 23 383	19.085 94	7.1631 178	136.95 817	19.119 91
45	7.2482 484	138.84 997	19.156 35	7.4079 578	142.39 906	19.222 44	7.4909 385	144.24 308	19.255 67
46	7.5744 196	146.09 821	19.288 37	7.7450 662	149.89 036	19.353 01	7.8337 619	151.86 138	19.385 50
47	7.9152 685	153.67 263	19.414 71	8.0975 151	157.72 256	19.477 90	8.1922 747	159.82 833	19.509 64
48	8.2714 556	161.58 790	19.535 61	8.4660 027	165.91 117	19.597 34	8.5671 949	168.15 989	19.628 35
49	8.6436 711	169.85 936	19.651 30	8.8512 587	174 47 242	19.711 59	8.9592 733	176.87 274	19.741 86
50	9.0326 363	178.50 303	19.762 01	9.2540 463	183.42 325	19.820 87	9.3692 952	185.98 434	19.850 41
51	9.4391 049	187.53 566	19.867 95	9.6751 632	192.78 141	19.925 39	9.7980 818	195.51 293	19.954 20
52	9.8638 646	196.97 477	19.969 33	10.115 444	202.56 541	20.025 36	10.246 492	205.47 760	20.053 46
53	10.307 739	206.83 863	20.066 34	10.575 760	212.79 466	20.120 98	10.715 423	215.89 830	20.148 37
54	10.771 587	217.14 637	20.159 18	11.057 023	223.48 939	20.212 44	11.205 816	226.79 591	20.239 12
55	11.256 308	227.91 795	20.248 02	11.560 186	234.67 081	20.299 92	11.718 651	238.19 224	20.325 91
56	11.762 842	239.17 427	20 333 03	12.086 247	246.36 105	20.383 59	12.254 956	250.11 013	20.408 90
57	12.292 170	250.93 711	20.414 39	12.636 247	258.58 326	20.463 61	12.815 805	262.57 345	20.488 25
58	12.845 318	263.22 928	20.492 24	13.211 275	271.36 167	20 540 16	13.402 322	275.60 714	20.564 14
59	13.423 357	276.07 460	20.566 73	13.812 471	284.72 157	20.613 37	14.015 680	289.23 733	20.636 70
60	14.027 408	289.49 795	20.638 02	14.441 024	298.68 944	20.683 40	14.657 109	303 49 130	20.706 08
61	14.658 641	303.52 536	20.706 24	15.098 181	313.29 292	20.750 37	15.327 893	318.39 761	20.772 43
62	15.318 280	318.18 400	20.771 52	15.785 243	328.56 095	20 814 44	16.029 375	333.98 611	20.835 88
63	16.007 603	333.50 228	20 833 99	16.503 570	344.52 378	20.875 71	16.762 961	350.28 801	20.896 55
64	16.727 945	349.50 989	20.893 77	17.254 586	361.21 301	20.934 32	17.530 119	367 33 598	20.954 56
65	17.480 702	366.23 783	20.950 98	18.039 777	378.66 171	20.990 38	18.332 386	385.16 414	21.010 04
66	18.267 334	383.71 853	21.005 72	18.860 700	396.90 444	21.043 99	19.171 370	403.80 821	21.063 09
67	19.089 364	401.98 587	21.058 11	19.718 979	415.97 732	21.095 27	20.048 749	423.30 553	21.113 81
68	19.948 385	421.07 523	21.108 24	20.616 316	435.91 814	21.144 33	20 966 282	443.69 515	21.162 32
69	20.846 063	441.02 362	21.156 21	21.554 488	456.76 639	21.191 24	21.925 805	465.01 790	21.208 70
70	21.784 136	461.86 968	21.202 11	22.535 351	478.56 337	21.236 12	22.929 242	487.31 648	21.253 06
71	22.764 422	483.65 382	21.246 04	23.560 851	501.35 224	21.279 04	23.978 601	510.63 557	21.295 47
72	23.788 821	506.41 824	21.288 08	24.633 017	525.17 815	21.320 09	25.075 983	535.02 185	21.336 03
73	24.859 318	530.20 706	21.328 31	25.753 973	550 08 829	21.359 36	26.223 588	560 52 417	21.374 81
74	25.977 987	555.06 638	21 366 80	26.925 940	576.13 199	21.396 91	27.423 713	587.19 361	21.411 89
75	27.146 996	581.04 436	21.403 63	28.151 238	603.36 085	21.432 83	28.678 761	615.08 358	21.447 35
76	28.368 611	608.19 136	21.438 88	29.432 296	631.82 879	21.467 19	29.991 247	644.24 993	21.481 27
77	29.645 199	636.55 997	21.472 62	30.771 649	661.59 220	21.500 05	31.363 799	674 75 109	21.513 69
78	30.979 233	666.20 517	21.504 90	32.171 951	692.71 003	21.531 48	32.799 166	706 64 813	21 544 70
79	32.373 298	697.18 440	21.535 79	33 635 976	725.24 391	21.561 55	34.300 223	740.00 495	21.574 35
80	33.830 096	729.55 770	21.565 35	35.166 623	759.25 829	21.590 31	35.869 975	774.88 834	21.602 70
81	35.352 451	763.38 779	21.593 63	36.766 924	794.82 054	21.617 82	37.511 568	811.36 818	21.629 82
82	36.943 311	798.74 025	21.620 70	38.440 049	832.00 109	21.644 12	39.228 288	849.51 751	21.655 74
83	38 605 760	835.68 356	21.646 61	40.189 312	870.87 359	21.669 29	41.023 574	889.41 276	21.680 53
84	40.343 019	874.28 932	21.671 39	42.018 177	911 51 504	21.693 35	42.901 021	931.13 381	21.704 23
85	42.158 455	914.63 234	21.695 11	43.930 266	954.00 592	21.716 37	44.864 390	974.76 423	21.726 90
86	44.055 586	956.79 079	21.717 81	45.929 368	998.43 040	21.738 39	46.917 613	1020.3 914	21.748 58
87	46.038 087	1000 8 464	21.739 53	48.019 441	1044.8 765	21.759 45	49.064 802	1068.1 067	21.769 31
88	48.109 801	1046.8 845	21.760 32	50.204 626	1093.4 361	21.779 59	51.310 257	1118.0 057	21.789 13
89	50 274 742	1094.9 943	21.780 21	52.489 250	1144.2 056	21.798 85	53.658 475	1170.1 883	21.808 08
90	52.537 105	1145.2 690	21.799 24	54.877 839	1197.2 853	21.817 28	56.114 160	1224.7 591	21.826 20
91	54.901 275	1197.8 061	21.817 46	57.375 124	1252.7 805	21.834 91	58.682 229	1281.8 273	21.843 54
92	57.371 832	1252.7 074	21.834 89	59.986 051	1310.8 011	21.851 77	61.367 826	1341.5 073	21.860 11
93	59.953 565	1310.0 792	21.851 57	62.715 791	1371.4 620	21.867 89	64.176 330	1403.9 184	21.875 95
94	62.651 475	1370.0 328	21.867 53	65.569 751	1434.8 834	21.883 31	67.113 365	1469.1 859	21.891 11
95	65.470 792	1432.6 843	21.882 80	68.553 585	1501.1 908	21.898 06	70.184 814	1537.4 403	21.905 60
96	68.416 977	1498.1 551	21.897 42	71.673 201	1570.5 156	21.912 17	73.396 828	1608.8 184	21.919 46
97	71.495 741	1566.5 720	21.911 41	74.934 780	1642.9 951	21.925 67	76.755 841	1683.4 631	21.932 70
98	74.713 050	1638.0 678	21.924 79	78.344 781	1718.7 729	21.938 58	80.268 577	1761.5 239	21.945 37
99	78.075 137	1712.7 808	21.937 60	81.909 958	1797.9 991	21.950 93	83.942 076	1843.1 572	21.957 49
100	81.588 518	1790.8 560	21.949 85	85.637 373	1880.8 305	21.962 73	87.783 692	1928.5 265	21.969 07
	Value of Perpetual Annu.		22.222 22	- - - - - - - - - -		22.222 22	- - - - - - - - - -		22.222 22

Years.	RATIO of INTEREST: ANNUALLY, 0.045.			RATIO of INTEREST: HALF-YEARLY, 0.0225.			RATIO of INTEREST: QUARTERLY, 0.01125.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.3184 025	0.0210 214	0.0660 214	0.3144 181	0.0206 377	0.0656 377	0.3124 010	0.0204 451	0.0654 451
27	0.3046 914	0.0197 195	0.0647 195	0.3007 329	0.0193 531	0.0643 531	0.2987 296	0.0191 693	0.0641 693
28	0.2915 707	0.0185 208	0.0635 208	0.2876 433	0.0181 706	0.0631 706	0.2856 565	0.0179 949	0.0629 949
29	0.2790 150	0.0174 145	0.0624 145	0.2751 235	0.0170 795	0.0620 795	0.2731 555	0.0169 114	0.0619 114
30	0.2670 000	0.0163 915	0.0613 915	0.2631 486	0.0160 707	0.0610 707	0.2612 016	0.0159 097	0.0609 097
31	0.2555 024	0.0154 434	0.0604 434	0.2516 949	0.0151 359	0.0601 359	0.2497 708	0.0149 817	0.0599 817
32	0.2444 999	0.0145 632	0.0595 632	0.2407 397	0.0142 682	0.0592 682	0.2388 403	0.0141 203	0.0591 203
33	0.2339 712	0.0137 445	0.0587 445	0.2302 614	0.0134 614	0.0584 614	0.2283 881	0.0133 195	0.0583 195
34	0.2238 959	0.0129 819	0.0579 819	0.2202 391	0.0127 100	0.0577 100	0.2183 933	0.0125 737	0.0575 737
35	0.2142 544	0.0122 704	0.0572 704	0.2106 531	0.0120 092	0.0570 092	0.2088 359	0.0118 782	0.0568 782
36	0.2050 282	0.0116 058	0.0566 058	0.2014 843	0.0113 546	0.0563 546	0.1996 968	0.0112 287	0.0562 287
37	0.1961 992	0.0109 840	0.0559 840	0.1927 146	0.0107 424	0.0557 424	0.1909 576	0.0106 213	0.0556 213
38	0.1877 504	0.0104 017	0.0554 017	0.1843 266	0.0101 691	0.0551 691	0.1826 008	0.0100 526	0.0550 526
39	0.1796 655	0.0098 557	0.0548 557	0.1763 037	0.0096 318	0.0546 318	0.1746 098	0.0095 197	0.0545 197
40	0.1719 287	0.0093 431	0.0543 431	0.1686 299	0.0091 275	0.0541 275	0.1669 685	0.0090 196	0.0540 196
41	0.1645 251	0.0088 616	0.0538 616	0.1612 902	0.0086 538	0.0536 538	0.1596 616	0.0085 499	0.0535 499
42	0.1574 403	0.0084 087	0.0534 087	0.1542 700	0.0082 084	0.0532 084	0.1526 744	0.0081 083	0.0531 083
43	0.1506 605	0.0079 823	0.0529 823	0.1475 553	0.0077 893	0.0527 893	0.1459 930	0.0076 928	0.0526 928
44	0.1441 728	0.0075 807	0.0525 807	0.1411 329	0.0073 946	0.0523 946	0.1396 040	0.0073 015	0.0523 015
45	0.1379 644	0.0072 020	0.0522 020	0.1349 900	0.0070 225	0.0520 225	0.1334 946	0.0069 327	0.0519 327
46	0.1320 233	0.0068 445	0.0518 445	0.1291 145	0.0066 715	0.0516 715	0.1276 526	0.0065 850	0.0515 850
47	0.1263 381	0.0065 073	0.0515 073	0.1234 947	0.0063 402	0.0513 402	0.1220 662	0.0062 567	0.0512 567
48	0.1208 977	0.0061 886	0.0511 886	0.1181 195	0.0060 273	0.0510 273	0.1167 243	0.0059 467	0.0509 467
49	0.1156 916	0.0058 872	0.0508 872	0.1129 783	0.0057 316	0.0507 316	0.1116 162	0.0056 538	0.0506 538
50	0.1107 096	0.0056 021	0.0506 021	0.1080 608	0.0054 519	0.0504 519	0.1067 316	0.0053 768	0.0503 768
51	0.1059 422	0.0053 323	0.0503 323	0.1033 574	0.0051 872	0.0501 872	0.1020 608	0.0051 148	0.0501 148
52	0.1013 801	0.0050 768	0.0500 768	0.0988 587	0.0049 367	0.0499 367	0.0975 944	0.0048 667	0.0498 667
53	0.0970 145	0.0048 347	0.0498 347	0.0945 559	0.0046 994	0.0496 994	0.0933 234	0.0046 318	0.0496 318
54	0.0928 368	0.0046 052	0.0496 052	0.0904 403	0.0044 745	0.0494 745	0.0892 394	0.0044 093	0.0494 093
55	0.0888 391	0.0043 876	0.0493 876	0.0865 038	0.0042 613	0.0492 613	0.0853 341	0.0041 983	0.0491 983
56	0.0850 135	0.0041 811	0.0491 811	0.0827 387	0.0040 591	0.0490 591	0.0815 997	0.0039 982	0.0489 982
57	0.0813 526	0.0039 851	0.0489 851	0.0791 374	0.0038 672	0.0488 672	0.0780 287	0.0038 085	0.0488 085
58	0.0778 494	0.0037 990	0.0487 990	0.0756 929	0.0036 851	0.0486 851	0.0746 139	0.0036 284	0.0486 284
59	0.0744 970	0.0036 222	0.0486 222	0.0723 983	0.0035 122	0.0485 122	0.0713 487	0.0034 574	0.0484 574
60	0.0712 890	0.0034 543	0.0484 543	0.0692 472	0.0033 480	0.0483 480	0.0682 263	0.0032 950	0.0482 950
61	0.0682 192	0.0032 946	0.0482 946	0.0662 331	0.0031 919	0.0481 919	0.0652 405	0.0031 407	0.0481 407
62	0.0652 815	0.0031 428	0.0481 428	0.0633 503	0.0030 436	0.0480 436	0.0623 855	0.0029 941	0.0479 941
63	0.0624 703	0.0029 985	0.0479 985	0.0605 929	0.0029 026	0.0479 026	0.0596 553	0.0028 548	0.0478 548
64	0.0597 802	0.0028 611	0.0478 611	0.0579 555	0.0027 684	0.0477 684	0.0570 447	0.0027 223	0.0477 223
65	0.0572 059	0.0027 305	0.0477 305	0.0554 331	0.0026 409	0.0476 409	0.0545 483	0.0025 963	0.0475 963
66	0.0547 425	0.0026 061	0.0476 061	0.0530 203	0.0025 195	0.0475 195	0.0521 611	0.0024 764	0.0474 764
67	0.0523 852	0.0024 877	0.0474 877	0.0507 126	0.0024 040	0.0474 040	0.0498 784	0.0023 624	0.0473 624
68	0.0501 294	0.0023 749	0.0473 749	0.0485 053	0.0022 940	0.0472 940	0.0476 956	0.0022 538	0.0472 538
69	0.0479 707	0.0022 675	0.0472 675	0.0463 941	0.0021 893	0.0471 893	0.0456 084	0.0021 505	0.0471 505
70	0.0459 050	0.0021 651	0.0471 651	0.0443 747	0.0020 896	0.0470 896	0.0436 124	0.0020 521	0.0470 521
71	0.0439 282	0.0020 676	0.0470 676	0.0424 433	0.0019 946	0.0469 946	0.0417 039	0.0019 583	0.0469 583
72	0.0420 365	0.0019 747	0.0469 747	0.0405 959	0.0019 041	0.0469 041	0.0398 788	0.0018 691	0.0468 691
73	0.0402 264	0.0018 861	0.0468 861	0.0388 290	0.0018 179	0.0468 179	0.0381 336	0.0017 840	0.0467 840
74	0.0384 941	0.0018 016	0.0468 016	0.0371 389	0.0017 357	0.0467 357	0.0364 648	0.0017 030	0.0467 030
75	0.0368 365	0.0017 210	0.0467 210	0.0355 224	0.0016 574	0.0466 574	0.0348 690	0.0016 258	0.0466 258
76	0.0352 502	0.0016 442	0.0466 442	0.0339 763	0.0015 827	0.0465 827	0.0333 431	0.0015 522	0.0465 522
77	0.0337 323	0.0015 709	0.0465 709	0.0324 974	0.0015 115	0.0465 115	0.0318 839	0.0014 820	0.0464 820
78	0.0322 797	0.0015 010	0.0465 010	0.0310 830	0.0014 436	0.0464 436	0.0304 886	0.0014 151	0.0464 151
79	0.0308 897	0.0014 343	0.0464 343	0.0297 301	0.0013 788	0.0463 788	0.0291 543	0.0013 513	0.0463 513
80	0.0295 595	0.0013 707	0.0463 707	0.0284 361	0.0013 171	0.0463 171	0.0278 785	0.0012 905	0.0462 905
81	0.0282 866	0.0013 100	0.0463 100	0.0271 984	0.0012 581	0.0462 581	0.0266 584	0.0012 325	0.0462 325
82	0.0270 685	0.0012 520	0.0462 520	0.0260 145	0.0012 019	0.0462 019	0.0254 918	0.0011 771	0.0461 771
83	0.0259 029	0.0011 966	0.0461 966	0.0248 822	0.0011 483	0.0461 483	0.0243 762	0.0011 243	0.0461 243
84	0.0247 874	0.0011 438	0.0461 438	0.0237 992	0.0010 971	0.0460 971	0.0233 095	0.0010 740	0.0460 740
85	0.0237 200	0.0010 933	0.0460 933	0.0227 633	0.0010 482	0.0460 482	0.0222 894	0.0010 259	0.0460 259
86	0.0226 986	0.0010 452	0.0460 452	0 0217 726	0.0010 016	0.0460 016	0.0213 140	0.0009 800	0.0459 800
87	0.0217 211	0.0009 992	0.0459 992	0.0208 249	0.0009 571	0.0459 571	0.0203 812	0.0009 362	0.0459 362
88	0.0207 858	0.0009 552	0.0459 552	0.0199 185	0.0009 145	0.0459 145	0.0194 893	0.0008 944	0.0458 944
89	0.0198 907	0.0009 133	0.0459 133	0.0190 515	0.0008 740	0.0458 740	0.0186 364	0.0008 546	0.0458 546
90	0.0190 342	0.0008 732	0.0458 732	0.0182 223	0.0008 352	0.0458 352	0.0178 208	0.0008 165	0.0458 165
91	0.0182 145	0.0008 349	0.0458 349	0.0174 292	0.0007 982	0.0457 982	0.0170 409	0.0007 801	0.0457 801
92	0.0174 302	0.0007 983	0.0457 983	0.0166 705	0.0007 629	0.0457 629	0.0162 952	0.0007 454	0.0457 454
93	0.0166 796	0.0007 633	0.0457 633	0.0159 449	0.0007 291	0.0457 291	0.0155 821	0.0007 123	0.0457 123
94	0.0159 613	0.0007 299	0.0457 299	0.0152 509	0.0006 969	0.0456 969	0.0149 002	0.0006 806	0.0456 806
95	0.0152 740	0.0006 980	0.0456 980	0.0145 871	0.0006 661	0.0456 661	0.0142 481	0.0006 504	0.0456 504
96	0.0146 163	0.0006 675	0.0456 675	0.0139 522	0.0006 367	0.0456 367	0.0136 246	0.0006 216	0.0456 216
97	0.0139 868	0.0006 383	0.0456 383	0.0133 449	0.0006 086	0.0456 086	0.0130 283	0.0005 940	0.0455 940
98	0.0133 845	0.0006 105	0.0456 105	0.0127 641	0.0005 818	0.0455 818	0.0124 582	0.0005 677	0.0455 677
99	0.0128 082	0.0005 838	0.0455 838	0.0122 085	0.0005 562	0.0455 562	0.0119 130	0.0005 425	0.0455 425
100	0.0122 566	0.0005 584	0.0455 584	0.0116 771	0.0005 317	0.0455 317	0.0113 916	0.0005 185	0.0455 185
	Ratio of Perpetual Ann.		0.0450 000	- - - - - - - - - -		0.0450 000	- - - - - - - - - -		0.0450 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0475.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02375.			RATIO *of* INTEREST: *QUARTERLY*, 0.011875.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
$0\frac{1}{4}$	....	....	....	....	....	....	1.0118 750	0.2500 000	0.2470 66
$0\frac{2}{4}$	....	....	....	1.0237 500	0.5000 000	0.4884 00	1.0238 910	0.5029 688	0.4912 33
$0\frac{3}{4}$	....	....	....	....	....	....	1.0360 497	0.7589 415	0.7325 34
1	1.0475 000	1.0000 000	0.9546 54	1.0480 641	1.0118 750	0.9654 71	1.0483 528	1.0179 539	0.9710 03
$1\frac{1}{4}$	....	....	....	....	....	....	1.0608 020	1.2800 421	1.2066 74
$1\frac{2}{4}$	....	....	....	1.0729 556	1.5359 070	1.4314 73	1.0733 990	1.5452 426	1.4395 79
$1\frac{3}{4}$	....	....	....	....	....	....	1.0861 456	1.8135 924	1.6697 51
2	1.0972 563	2.0475 000	1.8660 18	1.0984 383	2.0723 848	1.8866 65	1.0990 436	2.0851 288	1.8972 21
$2\frac{1}{4}$	....	....	....	....	....	....	1.1120 948	2.3598 897	2.1220 22
$2\frac{2}{4}$	....	....	....	1.1245 262	2.6216 040	2.3312 96	1.1253 009	2.6379 134	2.3441 85
$2\frac{3}{4}$	....	....	....	....	....	....	1.1386 638	2.9192 386	2.5637 41
3	1.1493 759	3.1447 563	2.7360 55	1.1512 337	3.1838 671	2.7656 13	1.1521 855	3.2039 046	2.7807 20
$3\frac{1}{4}$	....	....	....	....	....	....	1.1658 677	3.4919 509	2.9951 52
$3\frac{2}{4}$	....	....	....	1.1785 755	3.7594 839	3.1898 54	1.1797 123	3.7834 179	3.2070 68
$3\frac{3}{4}$	....	....	....	....	....	....	1.1937 214	4.0783 460	3.4164 97
4	1.2039 713	4.2941 322	3.5666 40	1.2065 667	4.3487 716	3.6042 53	1.2078 969	4.3767 763	3.6234 69
$4\frac{1}{4}$	....	....	....	....	....	....	1.2222 407	4.6787 505	3.8280 11
$4\frac{2}{4}$	....	....	....	1.2352 226	4.9520 550	4.0090 38	1.2367 548	4.9843 107	4.0301 53
$4\frac{3}{4}$	....	....	....	....	....	....	1.2514 412	5.2934 994	4.2299 23
5	1.2611 599	5.4981 035	4.3595 61	1.2645 591	5.5636 663	4.4044 33	1.2663 021	5.6063 597	4.4273 48
$5\frac{1}{4}$	....	....	....	....	....	....	1.2813 394	5.9229 352	4 6224 56
$5\frac{2}{4}$	....	....	....	1.2945 924	6.2019 458	4.7906 55	1.2965 553	6.2432 701	4.8152 75
$5\frac{3}{4}$	....	....	....	....	....	....	1.3119 519	6.5674 089	5.0058 31
6	1.3210 650	6.7592 634	5.1165 26	1.3253 390	6.8492 421	5.1679 17	1.3275 314	6.8953 969	5.1941 50
$6\frac{1}{4}$	....	....	....	....	....	....	1.3432 958	7.2272 797	5.3802 59
$6\frac{2}{4}$	....	....	....	1.3568 158	7.5119 116	5.5364 27	1.3592 474	7.5631 037	5.5641 85
$6\frac{3}{4}$	....	....	....	....	....	....	1.3753 885	7.9029 155	5.7459 52
7	1.3838 156	8.0803 284	5.8391 65	1.3890 402	8.1903 195	5.8963 88	1.3917 212	8.2467 626	5.9255 85
$7\frac{1}{4}$	....	....	....	....	....	....	1.4082 479	8.5946 929	6.1031 11
$7\frac{2}{4}$	....	....	....	1.4220 299	8.8848 395	6.2479 98	1.4249 709	8.9467 549	6.2785 53
$7\frac{3}{4}$	....	....	....	....	....	....	1.4418 924	9.3029 976	6.4519 36
8	1.4495 468	9.4641 440	6.5290 36	1.4558 031	9.5958 545	6.5914 51	1.4590 149	9.6634 707	6.6232 85
$8\frac{1}{4}$	....	....	....	....	....	....	1.4763 407	10.028 224	6.7926 22
$8\frac{2}{4}$	....	....	....	1.4903 784	10.323 756	6.9269 36	1.4938 722	10.397 310	6.9599 73
$8\frac{3}{4}$	....	....	....	....	....	....	1.5116 119	10.770 778	7.1253 59
9	1.5184 003	10.913 691	7.1876 24	1.5257 749	11.068 945	7.2546 38	1.5295 623	11.148 681	7.2888 04
$9\frac{1}{4}$	....	....	....	....	....	....	1.5477 259	11.531 071	7.4503 32
$9\frac{2}{4}$	....	....	....	1.5620 121	11.831 833	7.5747 38	1.5661 051	11.918 003	7.6099 63
$9\frac{3}{4}$	....	....	....	....	....	....	1.5847 026	12.309 529	7.7677 22
10	1.5905 243	12.432 091	7.8163 48	1.5991 098	12.612 839	7.8874 12	1.6035 210	12.705 705	7.9236 29
$10\frac{1}{4}$	....	....	....	....	....	....	1.6225 628	13.106 585	8.0777 06
$10\frac{2}{4}$	....	....	....	1.6370 887	13.412 394	8.1928 32	1.6418 307	13.512 226	8.2299 75
$10\frac{3}{4}$	....	....	....	....	....	....	1.6613 275	13.922 683	8.3804 57
11	1.6660 742	14.022 615	8.4165 61	1.6759 696	14.230 938	8.4911 67	1.6810 557	14.338 015	8.5291 73
$11\frac{1}{4}$	....	....	....	....	....	....	1.7010 183	14.758 279	8.6761 44
$11\frac{2}{4}$	....	....	....	1.7157 738	15.068 923	8.7825 81	1.7212 178	15.183 534	8.8213 90
$11\frac{3}{4}$	....	....	....	....	....	....	1.7416 573	15.613 838	8.9649 31
12	1.7452 128	15.688 690	8.9895 57	1.7565 235	15.926 810	9.0672 34	1.7623 395	16.049 252	9.1067 88
$12\frac{1}{4}$	....	....	....	....	....	....	1.7832 673	16.489 837	9.2469 80
$12\frac{2}{4}$	....	....	....	1.7982 409	16.805 071	9.3452 84	1.8044 436	16.935 654	9.3855 27
$12\frac{3}{4}$	....	....	....	....	....	....	1.8258 713	17.386 765	9.5224 48
13	1.8281 104	17.433 902	9.5365 70	1.8409 491	17.704 192	9.6168 83	1.8475 536	17.843 233	9.6577 62
$13\frac{1}{4}$	....	....	....	....	....	....	1.8694 933	18.305 121	9.7914 88
$13\frac{2}{4}$	....	....	....	1.8846 717	18.624 666	9.8821 81	1.8916 935	18.772 495	9.9236 45
$13\frac{3}{4}$	....	....	....	....	....	....	1.9141 574	19.245 418	10.054 25
14	1.9149 456	19.262 013	10.058 78	1.9294 326	19.567 002	10.141 32	1.9368 880	19.723 957	10.183 32
$14\frac{1}{4}$	....	....	....	....	....	....	1.9598 885	20.208 179	10.310 88
$14\frac{2}{4}$	....	....	....	1.9752 566	20.531 719	10.394 46	1.9831 622	20.698 151	10.436 94
$14\frac{3}{4}$	....	....	....	....	....	....	2.0067 122	21.193 942	10.561 53
15	2.0059 055	21.176 958	10.557 31	2.0221 690	21.519 347	10.641 72	2.0305 419	21.695 620	10.684 65
$15\frac{1}{4}$	....	....	....	....	....	....	2.0546 546	22.203 255	10.806 32
$15\frac{2}{4}$	....	....	....	2.0701 955	22.530 431	10.883 24	2.0790 537	22.716 919	10.926 57
$15\frac{3}{4}$	....	....	....	....	....	....	2.1037 424	23.236 683	11.045 40
16	2.1011 860	23.182 864	11.033 23	2.1193 626	23.565 529	11.119 16	2.1287 244	23.762 618	11.162 84
17	2.2009 924	25.284 050	11.487 57	2.2212 278	25.710 059	11.574 71	2.2316 542	25.929 561	11.618 99
18	2.3055 395	27.485 042	11.921 31	2.3279 890	27.957 664	12.009 36	2.3395 609	28.201 283	12.054 09
19	2.4150 526	29.790 582	12.335 38	2.4398 817	30.313 298	12.424 09	2.4526 853	30.582 848	12.469 13
20	2.5297 676	32.205 635	12.730 67	2.5571 523	32.782 153	12.819 79	2.5712 795	33.079 568	12.865 02
21	2.6499 316	34.735 402	13.108 04	2.6800 594	35.369 672	13.197 35	2.6956 081	35.697 013	13.242 66
22	2.7758 034	37.385 334	13.468 29	2.8088 739	38.081 557	13.557 59	2.8259 483	38.441 017	13.602 88
23	2.9076 540	40.161 137	13.812 21	2.9438 798	40.923 786	13.901 31	2.9625 909	41.317 703	13.946 48
24	3.0457 676	43.068 791	14.140 54	3.0853 747	43.902 624	14.229 27	3.1058 405	44.333 484	14.274 23
25	3.1914 415	46.114 559	14.453 97	3.2336 703	47.024 638	14.542 19	3.2560 166	47.495 086	14.586 87

YEARS.	RATIO *of* INTEREST: *ANNUALLY*, 0.0475.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02375.			RATIO *of* INTEREST: *QUARTERLY*, 0.011875.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
0½	....	....	....	....	....	....	0.9882 644	4.0000 000	4.0475 000
	....	....	....	0.9768 009	2.0000 000	2.0475 000	0.9766 665	1.9881 951	2.0356 951
	....	....	....	....	....	....	0.9652 047	1.3176 247	1.3651 247
1	0.9546 540	1.0000 000	1.0475 000	0.9541 401	0.9882 644	1.0357 644	0.9538 774	0.9823 627	1.0298 627
1½	....	....	....	....	....	....	0.9426 830	0.7812 243	0.8287 243
	....	....	....	0.9320 050	0.6510 811	0.6985 811	0.9316 200	0.6471 476	0.6946 476
	....	....	....	....	....	....	0.9206 869	0.5513 918	0.5988 918
2	0.9113 641	0.4884 005	0.5359 005	0.9103 834	0.4825 359	0.5300 359	0.9098 820	0.4795 867	0.5270 867
2½	....	....	....	....	....	....	0.8992 039	0.4237 486	0.4712 486
	....	....	....	0.8892 634	0.3814 459	0.4289 459	0.8886 512	0.3790 875	0.4265 875
	....	....	....	....	....	....	0.8782 223	0.3425 551	0.3900 551
3	0.8700 374	0.3179 897	0.3654 897	0.8686 334	0.3140 835	0.3615 835	0.8679 158	0.3121 191	0.3596 191
3½	....	....	....	....	....	....	0.8577 303	0.2863 729	0.3338 729
	....	....	....	0.8484 819	0.2659 940	0.3134 940	0.8476 643	0.2643 113	0.3118 113
	....	....	....	....	....	....	0.8377 163	0.2451 974	0.2926 974
4	0.8305 846	0.2328 759	0.2803 759	0.8287 980	0.2299 500	0.2774 500	0.8278 853	0.2284 787	0.2759 787
4½	....	....	....	....	....	....	0.8181 694	0.2137 323	0.2612 323
	....	....	....	0.8095 707	0.2019 368	0.2494 368	0.8085 677	0.2006 295	0.2481 295
	....	....	....	....	....	....	0.7990 787	0.1889 110	0.2364 110
5	0.7929 207	0.1818 809	0.2293 809	0.7907 894	0.1795 440	0.2270 440	0.7897 011	0.1783 689	0.2258 689
5½	....	....	....	....	....	....	0.7804 333	0.1688 352	0.2163 352
	....	....	....	0.7724 438	0.1612 397	0.2087 397	0.7712 744	0.1601 725	0.2076 725
	....	....	....	....	....	....	0.7622 231	0.1522 671	0.1997 671
6	0.7569 650	0.1479 451	0.1954 451	0.7545 239	0.1460 016	0.1935 016	0.7532 779	0.1450 243	0.1925 243
6½	....	....	....	....	....	....	0.7444 377	0.1383 646	0.1858 646
	....	....	....	0.7370 197	0.1331 219	0.1806 219	0.7357 012	0.1322 209	0.1797 209
	....	....	....	....	....	....	0.7270 673	0.1265 356	0.1740 356
7	0.7226 396	0.1237 574	0.1712 574	0.7199 216	0.1220 954	0.1695 954	0.7185 347	0.1212 597	0.1687 597
7½	....	....	....	....	....	....	0.7101 023	0.1163 509	0.1638 509
	....	....	....	0.7032 201	0.1125 513	0.1600 513	0.7017 687	0.1117 724	0.1592 724
	....	....	....	....	....	....	0.6935 330	0.1074 922	0.1549 922
8	0.6898 708	0.1056 620	0.1531 620	0.6869 061	0.1042 117	0.1517 117	0.6853 940	0.1034 825	0.1509 825
8½	....	....	....	....	....	....	0.6773 505	0.0997 185	0.1472 185
	....	....	....	0.6709 705	0.0968 640	0.1443 640	0.6694 013	0.0961 787	0.1436 787
	....	....	....	....	....	....	0.6615 454	0.0928 434	0.1403 434
9	0.6585 879	0.0916 280	0.1391 280	0.6554 047	0.0903 428	0.1378 428	0.6537 818	0.0896 967	0.1371 967
9½	....	....	....	....	....	....	0.6461 092	0.0867 222	0.1342 222
	....	....	....	0.6401 999	0.0845 178	0.1320 178	0.6385 267	0.0839 067	0.1314 067
	....	....	....	....	....	....	0.6310 332	0.0812 379	0.1287 379
10	0.6287 235	0.0804 370	0.1279 370	0.6253 478	0.0792 843	0.1267 843	0.6236 276	0.0787 048	0.1262 048
10½	....	....	....	....	....	....	0.6163 090	0.0762 975	0.1237 975
	....	....	....	0.6108 404	0.0745 579	0.1220 579	0.6090 762	0.0740 071	0.1215 071
	....	....	....	....	....	....	0.6019 283	0.0718 252	0.1193 252
11	0.6002 133	0.0713 134	0.1188 134	0.5966 696	0.0702 694	0.1177 694	0.5948 642	0.0697 447	0.1172 447
11½	....	....	....	....	....	....	0.5878 832	0.0677 586	0.1152 586
	....	....	....	0.5828 274	0.0663 617	0.1138 617	0.5809 840	0.0658 608	0.1133 608
	....	....	....	....	....	....	0.5741 658	0.0640 458	0.1115 458
12	0.5729 960	0.0637 402	0.1112 402	0.5693 064	0.0627 872	0.1102 872	0.5674 276	0.0623 082	0.1098 082
12½	....	....	....	....	....	....	0.5607 684	0.0606 434	0.1081 434
	....	....	....	0.5560 990	0.0595 058	0.1070 058	0.5541 875	0.0590 470	0.1065 470
	....	....	....	....	....	....	0.5476 837	0.0575 150	0.1050 150
13	0.5470 128	0.0573 595	0.1048 595	0.5431 981	0.0564 838	0.1039 838	0.5412 563	0.0560 438	0.1035 438
13½	....	....	....	....	....	....	0.5349 043	0.0546 295	0.1021 295
	....	....	....	0.5305 964	0.0536 922	0.1011 922	0.5286 269	0.0532 694	0.1007 694
	....	....	....	....	....	....	0.5224 230	0.0519 604	0.0994 604
14	0.5222 081	0.0519 157	0.0994 157	0.5182 871	0.0511 065	0.0986 065	0.5162 921	0.0506 998	0.0981 998
14½	....	....	....	....	....	....	0.5102 331	0.0494 849	0.0969 849
	....	....	....	0.5062 633	0.0487 051	0.0962 051	0.5042 452	0.0483 135	0.0958 135
	....	....	....	....	....	....	0.4983 276	0.0471 833	0.0946 833
15	0.4985 280	0.0472 211	0.0947 211	0.4945 185	0.0464 698	0.0939 698	0.4924 793	0.0460 923	0.0935 923
15½	....	....	....	....	....	....	0.4866 999	0.0450 384	0.0925 384
	....	....	....	0.4830 461	0.0443 844	0.0918 844	0.4809 881	0.0440 201	0.0915 201
	....	....	....	....	....	....	0.4753 433	0.0430 354	0.0905 354
16	0.4759 217	0.0431 353	0.0906 353	0.4718 399	0.0424 349	0.0899 349	0.4697 649	0.0420 829	0.0895 829
17	0.4543 405	0.0395 506	0.0870 506	0.4502 015	0.0388 953	0.0863 953	0.4480 981	0.0385 660	0.0860 660
18	0.4337 380	0.0363 834	0.0838 834	0.4295 553	0.0357 684	0.0832 684	0.4274 306	0.0354 594	0.0829 594
19	0.4140 696	0.0335 677	0.0810 677	0.4098 560	0.0329 888	0.0804 888	0.4077 164	0.0326 981	0.0801 981
20	0.3952 932	0.0310 505	0.0785 505	0.3910 600	0.0305 044	0.0780 044	0.3889 115	0.0302 301	0.0777 301
21	0.3773 682	0.0287 891	0.0762 891	0.3731 261	0.0282 598	0.0757 598	0.3709 738	0.0280 135	0.0755 135
22	0.3602 561	0.0267 485	0.0742 485	0.3560 145	0.0262 594	0.0737 594	0.3538 635	0.0260 139	0.0735 139
23	0.3439 199	0.0248 997	0.0723 997	0.3396 878	0.0244 357	0.0719 357	0.3375 424	0.0242 027	0.0717 027
24	0.3283 245	0.0232 187	0.0707 187	0.3241 098	0.0227 777	0.0702 777	0.3219 741	0.0225 563	0.0700 563
25	0.3134 362	0.0216 851	0.0691 851	0.3092 461	0.0212 654	0.0687 654	0.3071 237	0.0210 548	0.0685 548

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0475.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02375.			RATIO *of* INTEREST: *QUARTERLY*, 0.011875.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	3.3419 875	49.305 000	14.753 20	3.3890 936	50.296 708	14.840 75	3.4134 542	50.809 561	14.885 09
27	3.5007 319	52.646 988	15.038 85	3.5519 872	53.726 047	15.125 63	3.5785 043	54.284 300	15.169 55
28	3.6670 167	56.147 720	15.311 55	3.7227 102	57.320 214	15.397 45	3.7515 350	57.927 053	15.440 89
29	3.8412 000	59.814 736	15.571 89	3.9016 388	61.087 132	15.656 79	3.9329 323	61.745 943	15.699 72
30	4.0236 570	63.655 936	15.820 42	4.0891 674	65.035 102	15.904 24	4.1231 006	65.749 486	15.946 61
31	4.2147 807	67.679 593	16.057 68	4.2857 094	69.172 829	16.140 35	4.3224 641	69.946 613	16.182 12
32	4.4149 828	71.894 374	16.284 18	4.4916 980	73.509 431	16.365 62	4.5314 674	74.346 682	16.405 76
33	4.6246 944	76.309 357	16.500 41	4.7075 872	78.054 468	16.580 57	4.7505 766	78.959 507	16.621 04
34	4.8443 674	80.934 051	16.706 84	4.9338 530	82.817 996	16.785 66	4.9802 803	83.795 375	16.825 43
35	5.0744 749	85.778 419	16.903 90	5.1709 940	87.810 400	16.981 34	5.2210 999	88.865 071	17.020 40
36	5.3155 124	90.852 894	17.092 03	5.4195 330	93.042 800	17.168 05	5.4735 453	94.179 901	17.206 38
37	5.5679 993	96.168 406	17.271 62	5.6800 177	98.526 689	17.346 19	5.7382 066	99.751 718	17.383 78
38	5.8324 792	101.73 641	17.443 08	5.9530 225	104.27 416	17.516 17	6.0156 650	105.59 295	17.553 00
39	6.1095 220	107.56 838	17.606 76	6.2391 489	110.29 787	17.678 35	6.3065 394	111.71 662	17.714 41
40	6.3997 243	113.67 841	17.763 02	6.5390 278	116.61 111	17.833 10	6.6114 783	118.13 638	17.868 38
41	6.7037 112	120.07 813	17.912 19	6.8533 200	123.22 779	17.980 74	6.9311 618	124.86 657	18.015 24
42	7.0221 375	126.78 184	18.054 59	7.1827 184	130.16 249	18.121 62	7.2663 030	131.92 217	18.155 33
43	7.3556 890	133.80 398	18.190 54	7.5279 490	137.43 051	18.256 03	7.6176 492	139.31 893	18.288 96
44	7.7050 843	141.15 967	18.320 33	7.8897 728	145.04 785	18.384 29	7.9859 840	147.07 335	18.416 43
45	8.0710 758	148.86 475	18.444 23	8.2689 874	153.03 131	18.506 66	8.3721 287	155.20 271	18.538 02
46	8.4544 519	156.93 583	18.562 51	8.6664 285	161.39 849	18.623 41	8.7769 447	163.72 515	18.654 00
47	8.8560 383	165.39 028	18.675 42	9.0829 723	170.16 784	18.734 82	9.2013 347	172.65 968	18.764 63
48	9.2767 001	174.24 632	18.783 22	9.5195 368	179.35 867	18.841 11	9.6462 451	182.02 621	18.870 16
49	9.7173 434	183.52 302	18.886 13	9.9770 844	188.99 125	18.942 53	10.112 668	191.84 564	18.970 82
50	10.178 917	193.24 036	18.984 37	10.456 624	199.08 681	19.039 30	10.601 644	202.13 988	19.066 84
51	10.662 416	203.41 928	19.078 16	10.959 211	209.66 761	19.131 63	11.114 263	212.93 186	19.158 43
52	11.168 881	214.08 170	19.167 69	11.485 956	220.75 696	19.219 73	11.651 669	224.24 567	19.245 80
53	11.699 402	225.25 058	19.253 17	12.038 017	232.37 931	19.303 79	12.215 060	236.10 653	19.329 13
54	12.255 124	236.94 998	19.334 77	12.616 613	244.56 028	19.383 99	12.805 693	248.54 090	19.408 62
55	12.837 242	249.20 510	19.412 67	13.223 019	257.32 672	19.460 51	13.424 884	261.57 651	19.484 45
56	13.447 011	262.04 234	19.487 04	13.858 571	270.70 676	19.533 53	14.074 015	275.24 242	19.556 78
57	14.085 744	275.48 936	19.558 03	14.524 670	284.72 990	19.603 19	14.754 533	289.56 912	19.625 77
58	14.754 817	289.57 510	19.625 80	15.222 785	299.42 705	19.669 66	15.467 956	304.58 855	19.691 58
59	15.455 671	304.32 992	19.690 50	15.954 454	314.83 061	19.733 09	16.215 875	320.33 422	19.754 36
60	16.189 815	319.78 559	19.752 27	16.721 290	330.97 452	19.793 60	16.999 959	336.84 123	19.814 24
61	16.958 832	335.97 540	19.811 23	17.524 983	347.89 438	19.851 34	17.821 954	354.14 641	19.871 35
62	17.764 376	352.93 424	19.867 53	18.367 305	365.62 747	19.906 43	18.683 696	372.28 834	19.925 84
63	18.608 184	370.69 861	19.921 27	19.250 112	384.21 288	19.959 00	19.587 105	391.30 748	19.977 81
64	19.492 073	389.30 680	19.972 57	20.175 351	403.69 159	20.009 15	20.534 197	411.24 625	20.027 38
65	20.417 946	408.79 887	20.021 55	21.145 060	424.10 652	20.057 00	21.527 083	432.14 912	20.074 67
66	21.387 799	429.21 681	20.068 30	22.161 377	445.50 268	20.102 66	22.567 978	454.06 269	20.119 78
67	22.403 719	450.60 461	20.112 94	23.226 543	467.92 723	20.146 23	23.659 203	477.03 986	20.162 80
68	23.467 895	473.00 833	20.155 55	24.342 905	491.42 958	20.187 80	24.803 192	501.11 984	20.203 84
69	24.582 621	496.47 623	20.196 23	25 512 924	516.06 156	20.227 46	26.002 496	526.36 834	20.242 99
70	25.750 295	521.05 885	20.235 06	26.739 179	541.87 745	20.265 30	27.259 790	552.83 769	20.280 33
71	26.973 434	546.80 914	20.272 14	28.024 373	568.93 416	20.301 41	28.577 878	580.58 689	20.315 95
72	28.254 673	573.78 258	20.307 53	29.371 338	597.29 132	20.335 86	29.959 698	609.67 786	20.349 93
73	29.596 769	602.03 725	20.341 32	30.783 044	627.01 144	20.368 72	31.408 334	640.17 545	20.382 34
74	31.002 616	631.63 402	20.373 57	32.262 602	658.16 003	20.400 09	32.927 015	672.14 769	20.413 26
75	32.475 240	662.63 664	20.404 36	33.813 273	690.80 575	20.430 02	34.519 129	705.66 587	20.442 75
76	34.017 814	695.11 188	20.433 76	35.438 477	725.02 056	20.458 57	36.188 226	740.80 476	20.470 87
77	35.633 660	729.12 969	20.461 82	37.141 794	760.87 987	20.485 81	37.938 028	777.64 270	20.497 70
78	37.326 259	764.76 335	20 488 61	38.926 979	798.46 272	20.511 81	39.772 439	816.26 187	20.523 30
79	39.099 257	802.08 961	20.514 13	40.797 968	837.85 196	20.536 61	41.695 548	856.74 838	20.547 71
80	40.956 471	841.18 887	20.538 60	42.758 884	879.13 440	20.560 28	43.711 645	899.19 253	20.571 01
81	42.901 904	882.14 534	20.561 91	44 814 050	922.40 105	20.582 85	45.825 226	943.68 897	20.593 22
82	44.939 744	925.04 724	20.584 16	46.967 995	967.74 727	20.604 40	48.041 005	990.33 694	20.614 40
83	47.074 382	969.98 699	20.605 40	49.225 468	1015.2 730	20.624 95	50.363 922	1039.2 405	20.634 62
84	49.310 415	1017.0 614	20.625 68	51.591 444	1065.0 830	20.644 57	52.799 159	1090.5 086	20.653 90
85	51.652 660	1066.3 718	20.645 04	54.071 138	1117.2 871	20.663 28	55.352 147	1144.2 557	20.672 29
86	54.106 161	1118.0 244	20.663 53	56.670 017	1172.0 004	20.681 14	58.028 579	1200.6 017	20.689 83
87	56.676 204	1172.1 306	20.681 17	59.393 808	1229.3 433	20.698 17	60.834 424	1259.6 721	20.706 56
88	59.368 323	1228.8 068	20.698 01	62 248 516	1289.4 424	20.714 43	63.775 940	1321.5 987	20.722 52
89	62.188 319	1288.1 751	20.714 10	65.240 432	1352.4 301	20.729 94	66.859 686	1386.5 197	20.737 75
90	65.142 264	1350.3 635	20.729 44	68.376 152	1418.4 453	20.744 73	70.092 540	1454.5 798	20.752 26
91	68.236 521	1415.5 057	20.744 10	71.662 588	1487.6 334	20.758 86	73.481 711	1525.9 308	20.766 13
92	71.477 756	1483.7 422	20.758 09	75.106 983	1560.1 470	20.772 33	77.034 758	1600.7 318	20.779 34
93	74.872 950	1555.2 200	20.771 45	78.716 930	1636.1 459	20.785 19	80.759 605	1679.1 496	20.791 95
94	78.429 415	1630.0 929	20.784 20	82.500 385	1715.7 976	20.797 45	84.664 559	1761.3 591	20.803 97
95	82.154 812	1708.5 224	20.796 37	86.465 689	1799.2 777	20.809 15	88.758 329	1847.5 438	20.815 44
96	86.057 165	1790.6 772	20.807 99	90.621 582	1886.7 701	20.820 32	93.050 044	1937.8 957	20.826 38
97	90.144 881	1876.7 343	20.819 08	94.977 223	1978.4 678	20.830 97	97.549 275	2032.6 163	20.836 81
98	94.426 763	1966.8 792	20.829 68	99.542 214	2074.5 729	20.841 14	102.26 606	2131.9 170	20.846 76
99	98.912 034	2061.3 060	20.839 78	104.32 662	2175.2 972	20.850 84	107.21 091	2236.0 191	20.856 26
100	103.61 035	2160.2 180	20.849 43	109.34 098	2280.8 627	20.860 09	112.39 486	2345.1 549	20.865 32
	Value of Perpetual Ann.		21.052 63	- - - - - - - - - -		21.052 63	- - - - - - - - - -		21.052 63

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0475.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02375.			RATIO *of* INTEREST: *QUARTERLY*, 0.011875.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.2992 231	0.0202 819	0.0677 819	0.2950 641	0.0198 820	0.0673 820	0.2929 584	0.0196 813	0.0671 813
27	0.2856 546	0.0189 944	0.0664 944	0.2815 325	0.0186 129	0.0661 129	0.2794 464	0.0184 215	0.0659 215
28	0.2727 012	0.0178 101	0.0653 101	0.2686 215	0.0174 458	0.0649 458	0.2665 576	0.0172 631	0.0647 631
29	0.2603 352	0.0167 183	0.0642 183	0.2563 025	0.0163 701	0.0638 701	0.2542 632	0.0161 954	0.0636 954
30	0.2485 301	0.0157 095	0.0632 095	0.2445 486	0.0153 763	0.0628 763	0.2425 359	0.0152 092	0.0627 092
31	0.2372 603	0.0147 755	0.0622 755	0.2333 336	0.0144 565	0.0619 565	0.2313 495	0.0142 966	0.0617 966
32	0.2265 014	0.0139 093	0.0614 093	0.2226 329	0.0136 037	0.0611 037	0.2206 791	0.0134 505	0.0609 505
33	0.2162 305	0.0131 046	0.0606 046	0.2124 230	0.0128 116	0.0603 116	0.2105 008	0.0126 647	0.0601 647
34	0.2064 253	0.0123 557	0.0598 557	0.2026 814	0.0120 747	0.0595 747	0.2007 919	0.0119 338	0.0594 338
35	0.1970 647	0.0116 579	0.0591 579	0.1933 864	0.0113 882	0.0588 882	0.1915 309	0.0112 530	0.0587 530
36	0.1881 286	0.0110 068	0.0585 068	0.1845 177	0.0107 477	0.0582 477	0.1826 969	0.0106 180	0.0581 180
37	0.1795 977	0.0103 984	0.0578 984	0.1760 558	0.0101 495	0.0576 495	0.1742 705	0.0100 249	0.0575 249
38	0.1714 537	0.0098 293	0.0573 293	0.1679 819	0.0095 901	0.0570 901	0.1662 327	0.0094 703	0.0569 703
39	0.1636 789	0.0092 964	0.0567 964	0.1602 783	0.0090 664	0.0565 664	0.1585 656	0.0089 512	0.0564 512
40	0.1562 567	0.0087 967	0.0562 967	0.1529 279	0.0085 755	0.0560 755	0.1512 521	0.0084 648	0.0559 648
41	0.1491 711	0.0083 279	0.0558 279	0.1459 147	0.0081 150	0.0556 150	0.1442 760	0.0080 085	0.0555 085
42	0.1424 068	0.0078 876	0.0553 876	0.1392 231	0.0076 827	0.0551 827	0.1376 216	0.0075 802	0.0550 802
43	0.1359 492	0.0074 736	0.0549 736	0.1328 383	0.0072 764	0.0547 764	0.1312 741	0.0071 778	0.0546 778
44	0.1297 844	0.0070 842	0.0545 842	0.1267 464	0.0068 943	0.0543 943	0.1252 194	0.0067 993	0.0542 993
45	0.1238 992	0.0067 175	0.0542 175	0.1209 338	0.0065 346	0.0540 346	0.1194 439	0.0064 432	0.0539 432
46	0.1182 809	0.0063 720	0.0538 720	0.1153 878	0.0061 958	0.0536 958	0.1139 348	0.0061 078	0.0536 078
47	0.1129 173	0.0060 463	0.0535 463	0.1100 961	0.0058 766	0.0533 766	0.1086 799	0.0057 917	0.0532 917
48	0.1077 970	0.0057 390	0.0532 390	0.1050 471	0.0055 754	0.0530 754	0.1036 673	0.0054 937	0.0529 937
49	0.1029 088	0.0054 489	0.0529 489	0.1002 297	0.0052 912	0.0527 912	0.0988 859	0.0052 125	0.0527 125
50	0.0982 423	0.0051 749	0.0526 749	0.0956 332	0.0050 229	0.0525 229	0.0943 250	0.0049 471	0.0524 471
51	0.0937 874	0.0049 160	0.0524 160	0.0912 474	0.0047 695	0.0522 695	0.0899 745	0.0046 963	0.0521 963
52	0.0895 345	0.0046 711	0.0521 711	0.0870 628	0.0045 299	0.0520 299	0.0858 246	0.0044 594	0.0519 594
53	0.0854 745	0.0044 395	0.0519 395	0.0830 702	0.0043 033	0.0518 033	0.0818 661	0.0042 354	0.0517 354
54	0.0815 986	0.0042 203	0.0517 203	0.0792 606	0.0040 890	0.0515 890	0.0780 903	0.0040 235	0.0515 235
55	0.0778 984	0.0040 128	0.0515 128	0.0756 257	0.0038 861	0.0513 861	0.0744 885	0.0038 230	0.0513 230
56	0.0743 660	0.0038 162	0.0513 162	0.0721 575	0.0036 940	0.0511 940	0.0710 529	0.0036 332	0.0511 332
57	0.0709 938	0.0036 299	0.0511 299	0.0688 484	0.0035 121	0.0510 121	0.0677 758	0.0034 534	0.0509 534
58	0.0677 745	0.0034 533	0.0509 533	0.0656 910	0.0033 397	0.0508 397	0.0646 498	0.0032 831	0.0507 831
59	0.0647 012	0.0032 859	0.0507 859	0.0626 784	0.0031 763	0.0506 763	0.0616 680	0.0031 217	0.0506 217
60	0.0617 672	0.0031 271	0.0506 271	0.0598 040	0.0030 214	0.0505 214	0.0588 237	0.0029 688	0.0504 688
61	0.0589 663	0.0029 764	0.0504 764	0.0570 614	0.0028 744	0.0503 744	0.0561 106	0.0028 237	0.0503 237
62	0.0562 924	0.0028 334	0.0503 334	0.0544 446	0.0027 350	0.0502 350	0.0535 226	0.0026 861	0.0501 861
63	0.0537 398	0.0026 977	0.0501 977	0.0519 478	0.0026 027	0.0501 027	0.0510 540	0.0025 555	0.0500 555
64	0.0513 029	0.0025 687	0.0500 687	0.0495 654	0.0024 771	0.0499 771	0.0486 992	0.0024 316	0.0499 316
65	0.0489 765	0.0024 462	0.0499 462	0.0472 924	0.0023 579	0.0498 579	0.0464 531	0.0023 140	0.0498 140
66	0.0467 556	0.0023 298	0.0498 298	0.0451 235	0.0022 447	0.0497 447	0.0443 106	0.0022 023	0.0497 023
67	0.0446 354	0.0022 192	0.0497 192	0.0430 542	0.0021 371	0.0496 371	0.0422 669	0.0020 963	0.0495 963
68	0.0426 114	0.0021 141	0.0496 141	0.0410 797	0.0020 349	0.0495 349	0.0403 174	0.0019 955	0.0494 955
69	0.0406 791	0.0020 142	0.0495 142	0.0391 958	0.0019 378	0.0494 378	0.0384 578	0.0018 998	0.0493 998
70	0.0388 345	0.0019 192	0.0494 192	0.0373 983	0.0018 454	0.0493 454	0.0366 841	0.0018 088	0.0493 088
71	0.0370 735	0.0018 288	0.0493 288	0.0356 832	0.0017 577	0.0492 577	0.0349 921	0.0017 224	0.0492 224
72	0.0353 924	0.0017 428	0.0492 428	0.0340 468	0.0016 742	0.0491 742	0.0333 782	0.0016 402	0.0491 402
73	0.0337 875	0.0016 610	0.0491 610	0.0324 854	0.0015 949	0.0490 949	0.0318 387	0.0015 621	0.0490 621
74	0.0322 553	0.0015 832	0.0490 832	0.0309 956	0.0015 194	0.0490 194	0.0303 702	0.0014 878	0.0489 878
75	0.0307 927	0.0015 091	0.0490 091	0.0295 742	0.0014 476	0.0489 476	0.0289 694	0.0014 171	0.0489 171
76	0.0293 964	0.0014 386	0.0489 386	0.0282 179	0.0013 793	0.0488 793	0.0276 333	0.0013 499	0.0488 499
77	0.0280 634	0.0013 715	0.0488 715	0.0269 238	0.0013 143	0.0488 143	0.0263 588	0.0012 859	0.0487 859
78	0.0267 908	0.0013 076	0.0488 076	0.0256 891	0.0012 524	0.0487 524	0.0251 430	0.0012 251	0.0487 251
79	0.0255 759	0.0012 467	0.0487 467	0.0245 110	0.0011 935	0.0486 935	0.0239 834	0.0011 672	0.0486 672
80	0.0244 162	0.0011 888	0.0486 888	0.0233 870	0.0011 375	0.0486 375	0.0228 772	0.0011 121	0.0486 121
81	0.0233 090	0.0011 336	0.0486 336	0.0223 144	0.0010 841	0.0485 841	0.0218 220	0.0010 597	0.0485 597
82	0.0222 520	0.0010 810	0.0485 810	0.0212 911	0.0010 333	0.0485 333	0.0208 155	0.0010 098	0.0485 098
83	0.0212 430	0.0010 309	0.0485 309	0.0203 147	0.0009 850	0.0484 850	0.0198 555	0.0009 622	0.0484 622
84	0.0202 797	0.0009 832	0.0484 832	0.0193 831	0.0009 389	0.0484 389	0.0189 397	0.0009 170	0.0484 170
85	0.0193 601	0.0009 378	0.0484 378	0.0184 942	0.0008 950	0.0483 950	0.0180 661	0.0008 739	0.0483 739
86	0.0184 822	0.0008 944	0.0483 944	0.0176 460	0.0008 532	0.0483 532	0.0172 329	0.0008 329	0.0483 329
87	0.0176 441	0.0008 531	0.0483 531	0.0168 368	0.0008 134	0.0483 134	0.0164 381	0.0007 939	0.0482 939
88	0.0168 440	0.0008 138	0.0483 138	0.0160 646	0.0007 755	0.0482 755	0.0156 799	0.0007 567	0.0482 567
89	0.0160 802	0.0007 763	0.0482 763	0.0153 279	0.0007 394	0.0482 394	0.0149 567	0.0007 212	0.0482 212
90	0.0153 510	0.0007 405	0.0482 405	0.0146 250	0.0007 050	0.0482 050	0.0142 669	0.0006 875	0.0481 875
91	0.0146 549	0.0007 065	0.0482 065	0.0139 543	0.0006 722	0.0481 722	0.0136 088	0.0006 553	0.0481 553
92	0.0139 904	0.0006 740	0.0481 740	0.0133 143	0.0006 410	0.0481 410	0.0129 812	0.0006 247	0.0481 247
93	0.0133 560	0.0006 430	0.0481 430	0.0127 037	0.0006 112	0.0481 112	0.0123 824	0.0005 955	0.0480 955
94	0.0127 503	0.0006 135	0.0481 135	0.0121 212	0.0005 828	0.0480 828	0.0118 113	0.0005 677	0.0480 677
95	0.0121 721	0.0005 853	0.0480 853	0.0115 653	0.0005 558	0.0480 558	0.0112 665	0.0005 413	0.0480 413
96	0.0116 202	0.0005 584	0.0480 584	0.0110 349	0.0005 300	0.0480 300	0.0107 469	0.0005 160	0.0480 160
97	0.0110 933	0.0005 328	0.0480 328	0.0105 288	0.0005 054	0.0480 054	0.0102 512	0.0004 920	0.0479 920
98	0.0105 902	0.0005 084	0.0480 084	0.0100 460	0.0004 820	0.0479 820	0.0097 784	0.0004 691	0.0479 691
99	0.0101 100	0.0004 851	0.0479 851	0.0095 853	0.0004 597	0.0479 597	0.0093 274	0.0004 472	0.0479 472
100	0.0096 515	0.0004 629	0.0479 629	0.0091 457	0.0004 384	0.0479 384	0.0088 972	0.0004 264	0.0479 264
	Ratio of Perpetual Ann.		0.0475 000	- - - - - - - - - -		0.0475 000	- - - - - - - - - -		0.0475 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.05.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.025.			RATIO *of* INTEREST: *QUARTERLY*, 0.0125.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
¼	....	....	....	....	....	....	1.0125 000	0.2500 000	0.2469 14
½	....	....	....	1.0250 000	0.5000 000	0.4878 05	1.0251 563	0.5031 250	0.4907 79
¾	....	....	....	....	....	....	1.0379 707	0.7594 141	0.7316 33
1	1.0500 000	1.0000 000	0.9523 81	1.0506 250	1.0125 000	0.9637 12	1.0509 453	1.0189 067	0.9695 14
¼	....	....	....	....	....	....	1.0640 822	1.2816 431	1.2044 59
½	....	....	....	1.0768 906	1.5378 125	1.4280 12	1.0773 832	1.5476 636	1.4365 02
¾	....	....	....	....	....	....	1.0908 505	1.8170 094	1.6656 81
2	1.1025 000	2.0500 000	1.8594 10	1.1038 129	2.0762 578	1.8809 87	1.1044 861	2.0897 220	1.8920 31
¼	....	....	....	....	....	....	1.1182 922	2.3658 435	2.1155 86
½	....	....	....	1.1314 082	2.6281 643	2.3229 14	1.1322 708	2.6454 166	2.3363 81
¾	....	....	....	....	....	....	1.1464 242	2.9284 843	2 5544 51
3	1.1576 250	3.1525 000	2.7232 48	1.1596 934	3.1938 684	2.7540 63	1.1607 545	3.2150 904	2.7698 28
¼	....	....	....	....	....	....	1.1752 639	3.5052 790	2.9825 46
½	....	....	....	1.1886 858	3.7737 151	3.1746 95	1.1899 547	3.7990 950	3.1926 38
¾	....	....	....	....	....	....	1.2048 292	4.0965 837	3.4001 36
4	1.2155 063	4.3101 250	3.5459 51	1 2184 029	4.3680 580	3.5850 69	1.2198 895	4.3977 910	3.6050 73
¼	....	....	....	....	....	....	1.2351 382	4.7027 633	3.8074 80
½	....	....	....	1.2488 630	4.9772 594	3.9854 33	1.2505 774	5.0115 479	4.0073 87
¾	....	....	....	....	....	....	1.2662 096	5.3241 922	4.2048 27
5	1.2762 816	5.5256 313	4.3294 77	1.2800 845	5.6016 909	4.3760 32	1.2820 372	5.6407 446	4.3998 27
¼	....	....	....	....	....	....	1.2980 627	5.9612 539	4.5924 22
½	....	....	....	1.3120 867	6.2417 332	4.7571 04	1.3142 885	6.2857 696	4.7826 39
¾	....	....	....	....	....	....	1.3307 171	6.6143 417	4.9705 08
6	1.3400 956	6.8019 128	5.0756 92	1.3448 888	6.8977 765	5.1288 82	1.3473 511	6.9470 210	5.1560 57
¼	....	....	....	....	....	....	1.3641 929	7.2838 588	5.3393 15
½	....	....	....	1.3785 110	7.5702 209	5.4915 92	1.3812 454	7.6249 070	5.5203 11
¾	....	....	....	....	....	....	1.3985 109	7.9702 183	5.6990 73
7	1.4071 004	8.1420 085	5.7863 73	1.4129 738	8.2594 764	5.8454 56	1.4159 923	8.3198 461	5.8756 28
¼	....	....	....	....	....	....	1.4336 922	8.6738 441	6.0500 03
½	....	....	....	1.4482 982	8.9659 633	6.1906 89	1.4516 134	9.0322 672	6.2222 25
¾	....	....	....	....	....	....	1.4697 585	9.3951 705	6.3923 21
8	1.4774 554	9.5491 089	6.4632 13	1.4845 056	9.6901 124	6.5275 01	1.4881 305	9.7626 102	6.5603 17
¼	....	....	....	....	....	....	1.5067 321	10.134 643	6.7262 39
½	....	....	....	1.5216 183	10.432 365	6.8560 99	1.5255 663	10.511 326	6.8901 12
¾	....	....	....	....	....	....	1.5446 359	10.892 717	7.0519 63
9	1.5513 282	11.026 564	7.1078 22	1 5596 587	11.193 174	7.1766 82	1.5639 438	11.278 876	7.2118 15
¼	....	....	....	....	....	....	1.5834 931	11.669 862	7.3696 94
½	....	....	....	1.5986 502	11.973 004	7.4894 46	1.6032 868	12.065 736	7.5256 24
¾	....	....	....	....	....	....	1.6233 279	12.466 557	7.6796 28
10	1.6288 946	12.577 893	7.7217 35	1.6386 164	12.772 329	7.7945 81	1.6436 195	12.872 389	7.8317 32
¼	....	....	....	....	....	....	1.6641 647	13.283 294	7.9819 57
½	....	....	....	1 6795 819	13.591 637	8.0922 74	1.6849 668	13.699 335	8.1303 28
¾	....	....	....	....	....	....	1.7060 289	14.120 577	8.2768 67
11	1.7103 394	14.206 787	8.3064 14	1.7215 714	14.431 428	8.3827 07	1.7273 542	14.547 084	8.4215 97
¼	....	....	....	....	....	....	1.7489 461	14.978 923	8.5645 40
½	....	....	....	1.7646 107	15.292 214	8.6660 55	1.7708 080	15.416 159	8.7057 19
¾	....	....	....	....	....	....	1.7929 431	15.858 861	8.8451 54
12	1.7958 563	15.917 127	8.8632 52	1.8087 259	16.174 519	8.9424 93	1.8153 549	16.307 097	8.9828 68
¼	....	....	....	....	....	....	1.8380 468	16.760 936	9.1188 82
½	....	....	....	1.8539 441	17.078 882	9.2121 88	1.8610 224	17.220 447	9.2532 17
¾	....	....	....	....	....	....	1.8842 852	17.685 703	9.3858 93
13	1.8856 491	17.712 983	9.3935 73	1.9002 927	18.005 854	9.4753 06	1.9078 387	18.156 774	9.5169 32
¼	....	....	....	....	....	....	1.9316 867	18.633 734	9.6463 52
½	....	....	....	1.9478 000	18.956 000	9.7320 05	1.9558 328	19.116 656	9.7741 75
¾	....	....	....	....	....	....	1.9802 807	19.605 614	9.9004 20
14	1.9799 316	19.598 632	9.8986 41	1.9964 950	19.929 900	9.9824 44	2.0050 342	20.100 684	10.025 11
¼	....	....	....	....	....	....	2.0300 971	20.601 943	10.148 25
½	....	....	....	2.0464 074	20.928 148	10.226 77	2.0554 733	21.109 467	10.269 88
¾	....	....	....	....	....	....	2.0811 668	21.623 335	10.390 00
15	2.0789 282	21.578 564	10.379 66	2.0975 676	21.951 352	10.465 15	2.1071 813	22.143 627	10.508 65
¼	....	....	....	....	....	....	2.1335 211	22.670 422	10.625 82
½	....	....	....	2.1500 068	23.000 135	10.697 70	2.1601 901	23.203 803	10.741 55
¾	....	....	....	....	....	....	2.1871 925	23.743 850	10.855 85
16	2.1828 746	23.657 492	10.837 77	2.2037 569	24.075 139	10.924 59	2.2145 324	24.290 648	10.968 74
17	2.2920 183	25.840 366	11.274 07	2.3153 221	26.306 443	11.361 89	2.3273 525	26.547 050	11.406 54
18	2.4066 192	28.132 385	11.689 59	2.4325 353	28.650 706	11.778 13	2.4459 203	28.918 405	11.823 12
19	2.5269 502	30.539 004	12.085 32	2.5556 824	31.113 648	12.174 30	2.5705 285	31.410 570	12.219 50
20	2.6532 977	33.065 954	12.462 21	2.6850 638	33.701 277	12 551 39	2.7014 849	34.029 699	12.596 67
21	2.7859 626	35.719 252	12.821 15	2.8209 952	36.419 904	12.910 30	2.8391 130	36.782 260	12.955 55
22	2.9252 607	38.505 214	13.163 00	2.9638 081	39.276 162	13.251 92	2.9837 526	39.675 051	13.297 03
23	3.0715 238	41.430 475	13.488 57	3.1138 509	42.277 017	13.577 08	3.1357 608	42.715 217	13.621 96
24	3.2250 999	44.501 999	13.798 64	3.2714 896	45.429 791	13.886 58	3.2955 132	45.910 265	13.931 14
25	3.3863 549	47.727 099	14.093 94	3.4371 087	48.742 174	14.181 16	3.4634 043	49.268 085	14.225 33

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.05.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.025.			RATIO *of* INTEREST: *QUARTERLY*, 0.0125.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
¼	....	....	....	....	....	....	0.9876 543	4.0000 000	4.0500 000
½	....	....	....	0.9756 098	2.0000 000	2.0500 000	0.9754 611	1.9875 776	2.0375 776
¾	....	....	....	....	....	....	0.9634 183	1.3168 048	1.3668 048
1	0.9523 810	1.0000 000	1.0500 000	0.9518 145	0.9876 543	1.0376 543	0.9515 243	0.9814 441	1.0314 441
¼	....	....	....	....	....	....	0.9397 771	0.7802 485	0.8302 485
½	....	....	....	0.9285 994	0.6502 743	0.7002 743	0.9281 749	0.6461 353	0.6961 353
¾	....	....	....	....	....	....	0.9167 159	0.5503 549	0.6003 549
2	0.9070 295	0.4878 049	0.5378 049	0.9059 507	0.4816 358	0.5316 358	0.9053 984	0.4785 325	0 5285 325
¼	....	....	....	....	....	....	0.8942 207	0.4226 822	0.4726 822
½	....	....	....	0.8838 543	0.3804 938	0.4304 938	0.8831 810	0.3780 123	0.4280 123
¾	....	....	....	....	....	....	0.8722 775	0.3414 736	0.3914 736
3	0.8638 376	0.3172 085	0.3672 085	0.8622 969	0.3131 000	0.3631 000	0.8615 084	0.3110 332	0.3610 332
¼	....	....	....	....	....	....	0.8508 727	0.2852 840	0.3352 840
½	....	....	....	0.8412 652	0.2649 908	0.3149 908	0.8403 681	0.2632 206	0.3132 206
¾	....	....	....	....	....	....	0.8299 932	0.2441 058	0.2941 058
4	0.8227 025	0.2320 118	0.2820 118	0.8207 466	0.2289 347	0.2789 347	0.8197 464	0.2273 869	0.2773 869
¼	....	....	....	....	....	....	0.8096 260	0.2126 409	0.2626 409
½	....	....	....	0.8007 284	0.2009 138	0.2509 138	0.7996 306	0.1995 392	0.2495 392
¾	....	....	....	....	....	....	0.7897 587	0.1878 219	0.2378 219
5	0.7835 262	0.1809 748	0.2309 748	0.7811 984	0.1785 175	0.2285 175	0.7800 014	0.1772 816	0.2272 816
¼	....	....	....	....	....	....	0.7703 788	0.1677 500	0.2177 500
½	....	....	....	0.7621 447	0.1609 514	0.2109 514	0.7608 680	0.1590 895	0.2090 895
¾	....	....	....	....	....	....	0.7514 746	0.1511 866	0.2011 866
6	0.7462 154	0.1470 175	0.1970 175	0.7435 559	0.1449 742	0.1949 742	0.7421 970	0.1439 466	0.1939 466
¼	....	....	....	....	....	....	0.7330 342	0.1372 899	0.1872 899
½	....	....	....	0.7264 204	0.1320 965	0.1820 965	0.7239 843	0.1311 491	0.1811 491
¾	....	....	....	....	....	....	0.7150 463	0.1254 671	0.1754 671
7	0.7106 813	0.1228 198	0.1728 198	0.7077 272	0.1210 731	0.1710 731	0.7062 185	0.1201 945	0.1701 945
¼	....	....	....	....	....	....	0.6974 998	0.1152 891	0.1652 891
½	....	....	....	0.6904 656	0.1115 329	0.1615 329	0.6888 886	0.1107 142	0.1607 142
¾	....	....	....	....	....	....	0.6803 839	0.1064 377	0.1564 377
8	0.6768 394	0.1047 218	0.1547 218	0.6736 249	0.1031 980	0.1531 980	0.6719 841	0.1024 316	0.1524 316
¼	....	....	....	....	....	....	0.6636 880	0.0986 715	0.1486 715
½	....	....	....	0.6571 950	0.0958 555	0.1458 555	0.6554 943	0.0951 355	0.1451 355
¾	....	....	....	....	....	....	0.6474 018	0.0918 045	0.1418 045
9	0.6446 089	0.0906 901	0.1406 901	0.6411 659	0.0893 402	0.1393 402	0.6394 092	0.0886 613	0 1386 613
¼	....	....	....	....	....	....	0.6315 152	0.0856 908	0.1356 908
½	....	....	....	0.6255 277	0.0835 212	0.1335 212	0.6237 187	0.0828 793	0.1328 793
¾	....	....	....	....	....	....	0.6160 185	0.0802 146	0.1302 146
10	0.6139 132	0.0795 050	0.1295 050	0.6102 710	0.0782 943	0.1282 943	0.6084 134	0.0776 857	0.1276 857
¼	....	....	....	....	....	....	0.6009 020	0.0752 826	0.1252 826
½	....	....	....	0.5953 863	0.0735 747	0.1235 747	0.5934 835	0.0729 962	0.1229 962
¾	....	....	....	....	....	....	0.5861 565	0.0708 186	0.1208 186
11	0.5846 793	0.0703 889	0.1203 889	0.5808 647	0.0692 932	0.1192 932	0.5789 200	0.0687 423	0.1187 423
¼	....	....	....	....	....	....	0.5717 729	0.0667 605	0.1167 605
½	....	....	....	0.5666 973	0.0653 928	0.1153 928	0 5647 140	0.0648 670	0.1148 670
¾	....	....	....	....	....	....	0.5577 422	0.0630 562	0.1130 562
12	0.5568 375	0.0628 254	0.1128 254	0.5528 753	0.0618 256	0.1118 256	0.5508 565	0.0613 230	0.1113 230
¼	....	....	....	....	....	....	0.5440 558	0.0596 625	0.1096 625
½	....	....	....	0.5393 906	0.0585 518	0.1085 518	0.5373 390	0.0580 705	0.1080 705
¾	....	....	....	....	....	....	0.5307 052	0.0565 428	0.1065 428
13	0.5303 214	0.0564 558	0.1064 558	0.5262 347	0.0555 375	0.1055 375	0.5241 533	0.0550 759	0.1050 759
¼	....	....	....	....	....	....	0.5176 823	0.0536 661	0.1036 661
½	....	....	....	0.5133 997	0.0527 537	0.1027 537	0.5112 912	0.0523 104	0.1023 104
¾	....	....	....	....	....	....	0.5049 789	0.0510 058	0.1010 058
14	0.5050 679	0.0510 240	0.1010 240	0.5008 778	0.0501 759	0.1001 759	0.4987 446	0.0497 495	0.0997 495
¼	....	....	....	....	....	....	0.4925 873	0.0485 391	0.0985 391
½	....	....	....	0.4886 612	0.0477 825	0.0977 825	0.4865 060	0.0473 721	0.0973 721
¾	....	....	....	....	....	....	0.4804 997	0.0462 463	0.0962 463
15	0.4810 171	0.0463 423	0.0963 423	0.4767 427	0.0455 553	0.0955 553	0.4745 076	0.0451 597	0.0951 597
¼	....	....	....	....	....	....	0.4687 087	0.0441 103	0.0941 103
½	....	....	....	0.4651 148	0.0434 780	0.0934 780	0.4629 222	0.0430 964	0.0930 964
¾	....	....	....	....	....	....	0.4572 028	0.0421 162	0.0921 162
16	0.4581 115	0.0422 699	0.0922 699	0.4537 705	0.0415 366	0.0915 366	0.4515 626	0.0411 681	0.0911 681
17	0.4362 967	0.0386 991	0.0886 991	0.4319 054	0.0380 135	0.0880 135	0.4296 728	0.0376 690	0.0876 690
18	0.4155 207	0.0355 462	0.0855 462	0.4110 937	0.0349 032	0.0849 032	0.4088 441	0.0345 801	0.0845 801
19	0.3957 340	0.0327 450	0.0827 450	0.3912 849	0.0321 402	0.0821 402	0.3890 251	0.0318 364	0.0818 364
20	0.3768 895	0.0302 426	0.0802 426	0.3724 306	0.0296 725	0.0796 725	0.3701 668	0.0293 861	0.0793 861
21	0.3589 423	0.0279 961	0.0779 961	0.3544 848	0.0274 575	0.0774 575	0.3522 227	0.0271 871	0.0771 871
22	0.3418 499	0.0259 705	0.0759 705	0.3374 038	0.0254 607	0.0754 607	0.3351 484	0.0252 048	0.0752 048
23	0 3255 713	0.0241 368	0.0741 368	0.3211 458	0.0236 535	0.0736 535	0.3189 019	0.0234 109	0.0734 109
24	0.3100 680	0.0224 709	0.0724 709	0.3056 712	0.0220 120	0.0720 120	0.3034 429	0.0217 816	0.0717 816
25	0.2953 028	0.0209 525	0.0709 525	0.2909 422	0.0205 161	0.0705 161	0.2887 332	0.0202 971	0.0702 971

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.05.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.025.			RATIO *of* INTEREST: *QUARTERLY*, 0.0125.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	3.5556 727	51.113 454	14.375 18	3.6111 123	52.222 247	14.461 54	3.6398 486	52.796 971	14.505 26
27	3.7334 563	54.669 126	14.643 03	3.7939 249	55.878 408	14.728 42	3.8252 819	56.505 638	14.771 63
28	3.9201 291	58.402 583	14.898 13	3.9859 924	59.719 847	14.982 43	4.0201 622	60.403 243	15.025 08
29	4.1161 356	62.322 712	15.141 07	4.1877 832	63.755 664	15.224 20	4.2249 707	64.499 413	15.266 24
30	4.3219 424	66.438 648	15.372 45	4.3997 897	67.995 795	15.454 33	4.4402 132	68.804 265	15.495 71
31	4.5380 395	70.760 790	15.592 81	4.6225 291	72.450 582	15.673 37	4.6664 214	73.328 428	15.714 06
32	4.7649 415	75.298 829	15.802 68	4.8565 416	77.130 893	15.881 85	4.9041 538	78.083 076	15.921 82
33	5.0031 885	80.063 771	16.002 55	5.1024 072	82.048 144	16.080 28	5.1539 976	83.079 951	16.119 52
34	5.2533 480	85.066 959	16.192 90	5.3607 166	87.214 332	16.269 15	5.4165 697	88.331 394	16.307 63
35	5.5160 154	90.320 307	16.374 19	5.6321 029	92.642 057	16.448 93	5.6925 187	93.850 374	16.486 62
36	5.7918 161	95.836 323	16.546 85	5.9172 281	98.344 561	16.620 04	5.9825 260	99.650 519	16.656 93
37	6.0814 069	101.62 814	16.711 29	6 2167 877	104.33 575	16.782 91	6.2873 078	105.74 616	16.818 99
38	6.3854 773	107.70 955	16.867 89	6.5315 126	110.63 025	16.937 92	6.6076 168	112.15 234	16.973 19
39	6.7047 512	114.09 502	17.017 04	6.8621 704	117.24 341	17.085 47	6.9442 440	118.88 488	17.119 92
40	7.0399 887	120.79 977	17.159 09	7.2095 678	124.19 136	17.225 91	7.2980 209	125.96 042	17.259 54
41	7.3919 881	127.83 976	17.294 37	7.5745 522	131.49 104	17.359 58	7.6698 210	133.39 642	17.392 38
42	7.7615 876	135.23 175	17.423 21	7.9580 139	139.16 028	17.486 81	8.0605 626	141.21 125	17.518 79
43	8.1496 669	142.99 334	17.545 91	8.3608 883	147.21 777	17.607 91	8.4712 107	149.42 421	17.639 06
44	8.5571 503	151.14 301	17.662 77	8.7841 583	155.68 317	17.723 17	8.9027 794	158.05 559	17.753 51
45	8.9850 078	159.70 016	17.774 07	9.2288 563	164.57 713	17.832 88	9.3563 345	167.12 669	17.862 41
46	9.4342 582	168.68 516	17.880 07	9.6960 672	173.92 134	17.937 31	9.8329 961	176.65 992	17.966 03
47	9.9059 711	178.11 942	17.981 01	10.186 931	183.73 861	18.036 70	10.333 941	186 67 883	18.064 63
48	10.401 270	188.02 539	18.077 16	10.702 644	194 05 288	18.131 30	10.860 408	197.20 815	18.158 45
49	10.921 333	198.42 666	18.168 72	11.244 465	204.88 931	18.221 35	11.413 695	208.27 389	18.247 72
50	11.467 400	209.34 800	18.255 92	11.813 716	216.27 433	18.307 05	11.995 169	219.90 338	18.332 66
51	12.040 770	220.81 540	18.338 98	12.411 786	228.23 571	18.388 63	12.606 267	232.12 534	18.413 49
52	12.642 808	232.85 617	18.418 07	13.040 132	240.80 265	18.466 27	13.248 498	244.96 995	18.490 40
53	13.274 949	245.49 893	18.493 40	13.700 289	254.00 578	18.540 17	13.923 447	258.46 894	18.563 57
54	13.938 696	258.77 392	18.565 14	14.393 856	267.87 732	18.610 52	14.632 781	272.65 563	18.633 21
55	14.635 631	272.71 262	18.633 47	15.122 555	282.45 111	18.677 47	15.378 253	287.56 507	18.699 46
56	15.367 413	287.34 825	18.698 54	15.888 135	297.76 270	18.741 20	16.161 704	303.23 408	18.762 51
57	16.135 783	302.71 566	18.760 52	16.692 472	313.84 944	18.801 86	16.985 067	319.70 134	18.822 50
58	16.942 572	318.85 145	18.819 54	17.537 528	330.75 057	18.859 59	17.850 377	337.00 754	18.879 58
59	17.789 701	335.79 402	18.875 75	18.425 366	348.50 731	18.914 54	18.759 771	355.19 541	18.933 89
60	18.679 186	353.58 372	18.929 29	19.356 150	367.16 300	18.966 85	19.715 494	374.30 987	18.985 57
61	19.613 145	372.26 291	18.980 27	20.338 156	386.76 312	19.016 63	20.719 906	394.39 812	19.034 75
62	20.593 803	391.87 605	19.028 83	21.367 775	407.35 551	19.064 01	21.775 489	415.50 977	19.081 54
63	21.623 493	412.46 986	19.075 08	22.449 519	428.99 038	19.109 11	22.884 848	437.69 696	19.126 06
64	22.704 667	434.09 335	19.119 12	23.586 026	451.72 052	19.152 03	24.050 724	461.01 449	19.168 42
65	23.839 901	456.79 802	19.161 07	24.780 068	475.60 137	19.192 90	25.275 997	485.51 993	19.208 74
66	25.031 896	480.63 792	19.201 02	26.034 559	500.69 119	19.231 79	26.563 691	511.27 382	19.247 09
67	26.283 491	505.66 981	19.239 07	27.352 559	527.05 118	19.268 81	27.916 987	538.33 974	19.283 59
68	27.597 665	531.95 330	19.275 30	28.737 282	554.74 564	19.304 04	29.339 227	566.78 455	19.318 32
69	28.977 548	559.55 097	19.309 81	30.192 107	583.84 214	19.337 57	30.833 924	596.67 848	19.351 36
70	30.426 426	588.52 852	19.342 68	31.720 583	614.41 165	19.369 49	32.404 769	628.09 538	19.382 81
71	31.947 747	618.95 494	19.373 98	33.326 437	646.52 874	19.399 88	34.055 641	661.11 231	19.412 73
72	33.545 134	650.90 269	19.403 79	35.013 583	680.27 176	19.428 79	35.790 617	695.81 234	19.441 19
73	35.222 391	684.44 782	19.432 18	36.786 151	715.72 302	19.456 32	37.613 982	732.27 964	19.468 28
74	36.983 511	719.67 021	19.459 22	38.648 450	752.96 899	19.482 51	39.530 239	770.60 478	19.494 06
75	38.832 686	756.65 373	19.484 97	40.605 027	792.10 054	19.507 45	41.544 120	810.88 240	19.518 59
76	40.774 321	795.48 641	19.509 49	42.660 657	833.21 314	19.531 18	43.660 599	853.21 199	19.541 92
77	42.813 037	836.26 073	19.532 85	44.820 353	876.40 706	19.553 78	45.884 903	897.69 807	19.564 13
78	44.953 688	879.07 377	19.555 10	47.089 383	921.78 766	19.575 28	48.222 525	944.45 050	19.585 26
79	47.201 373	924.02 746	19.576 28	49.473 283	969.46 566	19.595 74	50.679 238	993.58 476	19.605 36
80	49.561 441	971.22 883	19.596 46	51.977 868	1019.5 574	19.615 22	53.261 109	1045.2 222	19.624 49
81	52.039 514	1020.7 903	19.615 68	54.609 248	1072.1 850	19.633 76	55.974 514	1099.4 903	19.642 69
82	54.641 489	1072.8 298	19.633 98	57.373 841	1127.4 768	19.651 41	58.826 154	1156.5 231	19.660 02
83	57.373 564	1127.4 713	19.651 41	60.278 392	1185.5 678	19.668 20	61.823 073	1216.4 615	19.676 50
84	60.242 242	1184.8 448	19.668 01	63.329 985	1246.5 997	19.684 19	64.972 670	1279.4 534	19.692 18
85	63.254 354	1245.0 871	19.683 82	66.536 066	1310.7 213	19.699 41	68.282 725	1345.6 545	19.707 10
86	66.417 072	1308.3 414	19.698 87	69.904 454	1378.0 891	19.713 89	71.761 411	1415.2 282	19.721 30
87	69.737 925	1374.7 585	19.713 21	73.443 367	1448.8 673	19.727 68	75.417 320	1488.3 464	19.734 81
88	73.224 822	1444.4 964	19.726 87	77.161 437	1523.2 287	19.740 80	79.259 481	1565.1 896	19.747 67
89	76.886 063	1517.7 213	19.739 87	81.067 735	1601.3 547	19.753 29	83.297 382	1645.9 476	19.759 90
90	80.730 366	1594.6 073	19.752 26	85.171 789	1683.4 358	19.765 18	87.540 995	1730.8 199	19.771 54
91	84.766 884	1675.3 377	19.764 06	89.483 611	1769.6 722	19.776 50	92.000 801	1820.0 160	19.782 61
92	89.005 228	1760.1 046	19.775 29	94.013 719	1860.2 744	19.787 26	96.687 812	1913.7 562	19.793 15
93	93.455 490	1849.1 098	19.785 99	98.773 163	1955.4 633	19.797 52	101.61 361	2012.2 721	19.803 18
94	98.128 264	1942.5 653	19.796 18	103.77 355	2055.4 711	19.807 27	106.79 034	2115.8 069	19.812 72
95	103.03 468	2040.6 935	19.805 89	109.02 709	2160.5 418	19.816 56	112.23 082	2224.6 163	19 821 80
96	108.18 641	2143.7 282	19.815 13	114.54 659	2270.9 317	19.825 39	117.94 845	2338.9 690	19.830 44
97	113.59 573	2251.9 147	19.823 94	120.34 551	2386.9 102	19.833 81	123.95 738	2459.1 475	19.838 65
98	119.27 552	2365.5 104	19.832 32	126.43 800	2508.7 600	19.841 82	130.27 243	2585.4 485	19.846 47
99	125.23 930	2484.7 859	19.840 30	132.83 892	2636.7 785	19.849 44	136.90 920	2718.1 840	19.853 92
100	131.50 126	2610.0 252	19.847 91	139.56 389	2771.2 779	19.856 70	143.88 408	2857.8 817	16.861 02
	Value of Perpetual Ann.		20.000 00	- - - - - - - - - -		20.000 00	- - - - - - - - - -		20.000 00

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.05.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.025.			RATIO *of* INTEREST: *QUARTERLY*, 0.0125.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.2812 407	0.0195 643	0.0695 643	0.2769 230	0.0191 489	0.0691 489	0.2747 367	0.0189 405	0.0689 405
27	0.2678 483	0.0182 919	0.0682 919	0.2635 793	0.0178 960	0.0678 960	0.2614 186	0.0176 973	0.0676 973
28	0.2550 936	0.0171 225	0.0671 225	0.2508 786	0.0167 449	0.0667 449	0.2487 462	0.0165 554	0.0665 554
29	0.2429 463	0.0160 455	0.0660 455	0.2387 898	0.0156 849	0.0656 849	0.2366 880	0.0155 040	0.0655 040
30	0.2313 775	0.0150 514	0.0650 514	0.2272 836	0.0147 068	0.0647 068	0.2252 144	0.0145 340	0.0645 340
31	0.2203 595	0.0141 321	0.0641 321	0.2163 318	0.0138 025	0.0638 025	0.2142 970	0.0136 373	0.0636 373
32	0.2098 662	0.0132 804	0.0632 804	0.2059 077	0.0129 650	0.0629 650	0.2039 088	0.0128 069	0.0628 069
33	0.1998 725	0.0124 900	0.0624 900	0.1959 859	0.0121 880	0.0621 880	0.1940 241	0.0120 366	0.0620 366
34	0.1903 548	0.0117 554	0.0617 554	0.1865 422	0.0114 660	0.0614 660	0.1846 187	0.0113 210	0.0613 210
35	0.1812 903	0.0110 717	0.0610 717	0.1775 536	0.0107 942	0.0607 942	0.1756 692	0.0106 553	0.0606 553
36	0.1726 574	0.0104 345	0.0604 345	0.1689 980	0.0101 683	0.0601 683	0.1671 535	0.0100 351	0.0600 351
37	0.1644 356	0.0098 398	0.0598 398	0.1608 548	0.0095 844	0.0595 844	0.1590 506	0.0094 566	0.0594 566
38	0.1566 054	0.0092 842	0.0592 842	0.1531 039	0.0090 391	0.0590 391	0.1513 405	0.0089 164	0.0589 164
39	0.1491 480	0.0087 646	0.0587 646	0.1457 265	0.0085 293	0.0585 293	0.1440 042	0.0084 115	0.0584 115
40	0.1420 457	0.0082 782	0.0582 782	0.1387 046	0.0080 521	0.0580 521	0.1370 234	0.0079 391	0.0579 391
41	0.1352 816	0.0078 223	0.0578 223	0.1320 210	0.0076 051	0.0576 051	0.1303 811	0.0074 965	0.0574 965
42	0.1288 396	0.0073 947	0.0573 947	0.1256 595	0.0071 860	0.0571 860	0.1240 608	0.0070 816	0.0570 816
43	0.1227 044	0.0069 933	0.0569 933	0.1196 045	0.0067 927	0.0567 927	0.1180 469	0.0066 924	0.0566 924
44	0.1168 613	0.0066 163	0.0566 163	0.1138 413	0.0064 233	0.0564 233	0.1123 245	0.0063 269	0.0563 269
45	0.1112 965	0.0062 617	0.0562 617	0.1083 558	0.0060 762	0.0560 762	0.1068 795	0.0059 835	0.0559 835
46	0.1059 967	0.0059 282	0.0559 282	0.1031 346	0.0057 497	0.0557 497	0.1016 984	0.0056 606	0.0556 606
47	0.1009 492	0.0056 142	0.0556 142	0.0981 650	0.0054 425	0.0554 425	0.0967 685	0.0053 568	0.0553 568
48	0.0961 421	0.0053 184	0.0553 184	0.0934 349	0.0051 532	0.0551 532	0.0920 776	0.0050 708	0.0550 708
49	0.0915 639	0.0050 396	0.0550 396	0.0889 326	0.0048 807	0.0548 807	0.0876 140	0.0048 014	0.0548 014
50	0.0872 037	0.0047 767	0.0547 767	0.0846 474	0.0046 238	0.0546 238	0.0833 669	0.0045 475	0.0545 475
51	0.0830 512	0.0045 287	0.0545 287	0.0805 686	0.0043 814	0.0543 814	0.0793 256	0.0043 080	0.0543 080
52	0.0790 964	0.0042 945	0.0542 945	0.0766 864	0.0041 528	0.0541 528	0.0754 803	0.0040 821	0.0540 821
53	0.0753 299	0.0040 733	0.0540 733	0.0729 912	0.0039 369	0.0539 369	0.0718 213	0.0038 689	0.0538 689
54	0.0717 427	0.0038 644	0.0538 644	0.0694 740	0.0037 331	0.0537 331	0.0683 397	0.0036 676	0.0536 676
55	0.0683 264	0.0036 669	0.0536 669	0.0661 264	0.0035 404	0.0535 404	0.0650 269	0.0034 775	0.0534 775
56	0.0650 728	0.0034 801	0.0534 801	0.0629 401	0.0033 584	0.0533 584	0.0618 747	0.0032 978	0.0532 978
57	0.0619 741	0.0033 034	0.0533 034	0.0599 072	0.0031 862	0.0531 862	0.0588 752	0.0031 279	0.0531 279
58	0.0590 229	0.0031 363	0.0531 363	0.0570 206	0.0030 234	0.0530 234	0.0560 212	0.0029 673	0.0529 673
59	0.0562 123	0.0029 780	0.0529 780	0.0542 730	0.0028 694	0.0528 694	0.0533 056	0.0028 154	0.0528 154
60	0.0535 355	0.0028 282	0.0528 282	0.0516 578	0.0027 236	0.0527 236	0.0507 215	0.0026 716	0.0526 716
61	0.0509 862	0.0026 863	0.0526 863	0.0491 687	0.0025 856	0.0525 856	0.0482 628	0.0025 355	0.0525 355
62	0.0485 583	0.0025 518	0.0525 518	0.0467 994	0.0024 549	0.0524 549	0.0459 232	0.0024 067	0.0524 067
63	0.0462 460	0.0024 244	0.0524 244	0.0445 444	0.0023 311	0.0523 311	0.0436 970	0.0022 847	0.0522 847
64	0.0440 438	0.0023 037	0.0523 037	0.0423 980	0.0022 138	0.0522 138	0.0415 788	0.0021 691	0.0521 691
65	0.0419 465	0.0021 892	0.0521 892	0.0403 550	0.0021 026	0.0521 026	0.0395 632	0.0020 596	0.0520 596
66	0.0399 490	0.0020 806	0.0520 806	0.0384 105	0.0019 972	0.0519 972	0.0376 454	0.0019 559	0.0519 559
67	0.0380 467	0.0019 776	0.0519 776	0.0365 597	0.0018 973	0.0518 973	0.0358 205	0.0018 576	0.0518 576
68	0.0362 349	0.0018 799	0.0518 799	0.0347 980	0.0018 026	0.0518 026	0.0340 841	0.0017 643	0.0517 643
69	0.0345 095	0.0017 871	0.0517 871	0.0331 212	0.0017 128	0.0517 128	0.0324 318	0.0016 759	0.0516 759
70	0.0328 662	0.0016 992	0.0516 992	0.0315 253	0.0016 276	0.0516 276	0.0308 597	0.0015 921	0.0515 921
71	0.0313 011	0.0016 156	0.0516 156	0.0300 062	0.0015 467	0.0515 467	0.0293 637	0.0015 126	0.0515 126
72	0.0298 106	0.0015 363	0.0515 363	0.0285 603	0.0014 700	0.0514 700	0.0279 403	0.0014 372	0.0514 372
73	0.0283 910	0.0014 610	0.0514 610	0.0271 841	0.0013 972	0.0513 972	0.0265 859	0.0013 656	0.0513 656
74	0.0270 391	0.0013 895	0.0513 895	0.0258 743	0.0013 281	0.0513 281	0.0252 971	0.0012 977	0.0512 977
75	0.0257 515	0.0013 216	0.0513 216	0.0246 275	0.0012 625	0.0512 625	0.0240 708	0.0012 332	0.0512 332
76	0.0245 252	0.0012 571	0.0512 571	0.0234 408	0.0012 002	0.0512 002	0.0229 039	0.0011 720	0.0511 720
77	0.0233 574	0.0011 958	0.0511 958	0.0223 113	0.0011 410	0.0511 410	0.0217 937	0.0011 140	0.0511 140
78	0.0222 451	0.0011 376	0.0511 376	0.0212 362	0.0010 848	0.0510 848	0.0207 372	0.0010 588	0.0510 588
79	0.0211 858	0.0010 822	0.0510 822	0.0202 129	0.0010 315	0.0510 315	0.0197 319	0.0010 065	0.0510 065
80	0.0201 770	0.0010 296	0.0510 296	0.0192 390	0.0009 808	0.0509 808	0.0187 754	0.0009 567	0.0509 567
81	0.0192 162	0.0009 796	0.0509 796	0.0183 119	0.0009 327	0.0509 327	0.0178 653	0.0009 095	0.0509 095
82	0.0183 011	0.0009 321	0.0509 321	0.0174 295	0.0008 869	0.0508 869	0.0169 992	0.0008 647	0.0508 647
83	0.0174 296	0.0008 869	0.0508 869	0.0165 897	0.0008 435	0.0508 435	0.0161 752	0.0008 221	0.0508 221
84	0.0165 996	0.0008 440	0.0508 440	0.0157 903	0.0008 022	0.0508 022	0.0153 911	0.0007 816	0.0507 816
85	0.0158 092	0.0008 032	0.0508 032	0.0150 294	0.0007 629	0.0507 629	0.0146 450	0.0007 431	0.0507 431
86	0.0150 564	0.0007 643	0.0507 643	0.0143 052	0.0007 256	0.0507 256	0.0139 351	0.0007 066	0.0507 066
87	0.0143 394	0.0007 274	0.0507 274	0.0136 159	0.0006 902	0.0506 902	0.0132 596	0.0006 719	0.0506 719
88	0.0136 566	0.0006 923	0.0506 923	0.0129 598	0.0006 565	0.0506 565	0.0126 168	0.0006 389	0.0506 389
89	0.0130 063	0.0006 589	0.0506 589	0.0123 354	0.0006 245	0.0506 245	0.0120 052	0.0006 076	0.0506 076
90	0.0123 869	0.0006 271	0.0506 271	0.0117 410	0.0005 940	0.0505 940	0.0114 232	0.0005 778	0.0505 778
91	0.0117 971	0.0005 969	0.0505 969	0.0111 752	0.0005 651	0.0505 651	0.0108 695	0.0005 494	0.0505 494
92	0.0112 353	0.0005 681	0.0505 681	0.0106 367	0.0005 376	0.0505 376	0.0103 426	0.0005 225	0.0505 225
93	0.0107 003	0.0005 408	0.0505 408	0.0101 242	0.0005 114	0.0505 114	0.0098 412	0.0004 970	0.0504 970
94	0.0101 907	0.0005 148	0.0505 148	0.0096 364	0.0004 865	0.0504 865	0.0093 641	0.0004 726	0.0504 726
95	0.0097 055	0.0004 900	0.0504 900	0.0091 720	0.0004 628	0.0504 628	0.0089 101	0.0004 495	0.0504 495
96	0.0092 433	0.0004 665	0.0504 665	0.0087 301	0.0004 403	0.0504 403	0.0084 783	0.0004 275	0.0504 275
97	0.0088 031	0.0004 441	0.0504 441	0.0083 094	0.0004 190	0.0504 190	0.0080 673	0.0004 066	0.0504 066
98	0.0083 840	0.0004 227	0.0504 227	0.0079 090	0.0003 986	0.0503 986	0.0076 762	0.0003 868	0.0503 868
99	0.0079 847	0.0004 024	0.0504 024	0.0075 279	0.0003 793	0.0503 793	0.0073 041	0.0003 679	0.0503 679
100	0.0076 045	0.0003 831	0.0503 831	0.0071 652	0.0003 608	0.0503 608	0.0069 500	0.0003 499	0.0503 499
	Ratio of Perpetual Ann.		0.0500 000	- - - - - - - - - -		0.0500 000	- - - - - - - - - -		0.0500 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0525.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02625			RATIO *of* INTEREST: *QUARTERLY*, 0.013125.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
$\frac{1}{4}$	....	....	....	....	....	....	1.0131 250	0.2500 000	0.2467 61
$\frac{1}{2}$	....	....	....	1.0262 500	0.5000 000	0.4872 11	1.0264 223	0 5032 813	0.4903 26
$\frac{3}{4}$	....	....	....	....	....	....	1.0398 941	0.7598 868	0.7307 35
1	1.0525 000	1.0000 000	0.9501 19	1.0531 891	1.0131 250	0.9619 59	1.0535 427	1.0198 603	0.9680 29
$\frac{1}{4}$	....	....	....	....	....	....	1.0673 704	1.2832 460	1.2022 50
$\frac{1}{2}$	....	....	....	1.0808 353	1.5397 195	1.4245 64	1.0813 797	1.5500 886	1.4334 36
$\frac{3}{4}$	....	....	....	....	....	....	1.0955 728	1.8204 335	1.6616 27
2	1.1077 563	2.0525 000	1.8528 44	1.1092 072	2.0801 372	1.8753 37	1.1099 522	2.0943 267	1.8868 62
$\frac{1}{4}$	....	....	....	....	....	....	1.1245 203	2.3718 147	2.1091 79
$\frac{1}{2}$	....	....	....	1.1383 239	2.6347 408	2.3145 79	1.1392 796	2.6529 448	2.3286 16
$\frac{3}{4}$	....	....	....	....	....	....	1.1542 326	2.9377 647	2.5452 10
3	1.1659 135	3.1602 563	2.7105 41	1.1682 049	3.2039 027	2.7425 86	1.1693 820	3.2263 229	2.7589 98
$\frac{1}{4}$	....	....	....	....	....	....	1.1847 301	3.5186 684	2.9700 17
$\frac{1}{2}$	....	....	....	1.1988 703	3.7880 052	3.1596 46	1.2002 797	3.8148 509	3.1783 02
$\frac{3}{4}$	....	....	....	....	....	....	1.2160 333	4.1149 208	3.3838 83
4	1.2271 239	4.3261 697	3.5254 55	1.2303 406	4.3874 403	3.5660 37	1.2319 938	4.4189 291	3.5868 11
$\frac{1}{4}$	....	....	....	....	....	....	1.2481 637	4.7269 276	3.7871 06
$\frac{1}{2}$	....	....	....	1.2626 371	5.0026 106	3.9620 34	1.2645 451	5.0389 546	3.9848 05
$\frac{3}{4}$	....	....	....	....	....	....	1.2811 430	5.3551 050	4.1799 43
5	1.2915 479	5.5532 936	4.2997 19	1.2957 813	5.6339 291	4.3479 01	1.2979 580	5.6753 907	4.3725 53
$\frac{1}{4}$	....	....	....	....	....	....	1.3149 937	5.9998 802	4.5626 68
$\frac{1}{2}$	....	....	....	1.3297 955	6.2818 198	4.7238 99	1.3322 530	6.3286 287	4.7503 21
$\frac{3}{4}$	....	....	....	....	....	....	1.3497 388	6.6616 919	4.9355 41
6	1.3593 542	6.8448 415	5.0353 63	1.3647 027	6.9467 175	5.0902 79	1.3674 541	6.9991 266	5.1183 63
$\frac{1}{4}$	....	....	....	....	....	....	1.3854 020	7.3409 901	5.2988 16
$\frac{1}{2}$	....	....	....	1.4005 261	7.6290 689	5.4472 88	1.4035 854	7.6873 406	5.4769 31
$\frac{3}{4}$	....	....	....	....	....	....	1.4220 074	8.0382 370	5.6527 39
7	1.4307 203	8.2041 957	5.7343 11	1.4372 899	8.3293 319	5.7951 65	1.4406 713	8.3937 388	5.8262 69
$\frac{1}{4}$	....	....	....	....	....	....	1.4595 801	8.7539 067	5.9975 51
$\frac{1}{2}$	....	....	....	1.4750 188	9.0479 769	6.1341 43	1.4787 371	9.1188 017	6.1666 15
$\frac{3}{4}$	....	....	....	....	....	....	1.4981 455	9.4884 860	6.3334 88
8	1.5058 331	9.6349 160	6.3983 95	1.5137 380	9.7854 863	6.4644 52	1.5178 087	9.8630 223	6.4981 99
$\frac{1}{4}$	....	....	....	....	....	....	1.5377 299	10.242 475	6.6607 76
$\frac{1}{2}$	....	....	....	1.5534 737	10.542 355	6.7863 11	1.5579 126	10.626 907	6.8212 47
$\frac{3}{4}$	....	....	....	....	....	....	1.5783 602	11.016 385	6.9796 39
9	1.5848 893	11.140 749	7.0293 54	1 5942 523	11.319 092	7.0999 38	1.5990 762	11.410 975	7.1359 80
$\frac{1}{4}$	....	....	....	....	....	....	1.6200 641	11.810 744	7.2902 95
$\frac{1}{2}$	....	....	....	1.6361 015	12.116 218	7.4055 42	1.6413 274	12 215 760	7.4426 10
$\frac{3}{4}$	....	....	....	....	....	....	1.6628 698	12.626 092	7.5929 53
10	1.6680 960	12.725 638	7.6288 40	1.6790 491	12.934 269	7.7033 30	1.6846 950	13.041 810	7.7413 48
$\frac{1}{4}$	....	....	....	....	....	....	1.7068 066	13.462 983	7.8878 20
$\frac{1}{2}$	....	....	....	1.7231 242	13.773 794	7.9935 00	1.7292 085	13.889 685	8.0323 95
$\frac{3}{4}$	....	....	....	....	....	....	1.7519 043	14 321 987	8.1750 97
11	1.7556 711	14.393 734	8.1984 23	1.7683 562	14.635 356	8.2762 49	1.7748 981	14.759 963	8.3159 50
$\frac{1}{4}$	....	....	....	....	....	....	1.7981 936	15.203 688	8.4549 78
$\frac{1}{2}$	....	....	....	1.8147 755	15.519 534	8.5517 65	1.8217 947	15.653 236	8.5922 05
$\frac{3}{4}$	....	....	....	....	....	....	1.8457 060	16.108 685	8.7276 55
12	1.8478 438	16.149 405	8.7395 94	1.8624 134	16.426 922	8.8202 34	1.8699 308	16.570 111	8.8613 50
$\frac{1}{4}$	....	....	....	....	....	....	1.8944 737	17.037 594	8.9933 15
$\frac{1}{2}$	....	....	....	1.9113 017	17.358 128	9.0818 36	1.9193 387	17.511 212	9.1235 68
$\frac{3}{4}$	....	....	....	....	....	....	1.9445 300	17.991 047	9.2521 33
13	1.9448 556	17.997 249	9.2537 71	1.9614 734	18.313 779	9.3367 46	1.9700 519	18.477 180	9.3790 34
$\frac{1}{4}$	....	....	....	....	....	....	1.9959 089	18.969 693	9.5042 90
$\frac{1}{2}$	....	....	....	2.0129 621	19.294 516	9.5851 36	2.0221 052	19.468 670	9.6279 23
$\frac{3}{4}$	....	....	....	....	....	....	2.0486 453	19.974 196	9.7499 55
14	2.0469 605	19.942 105	9.7423 01	2.0658 023	20.300 997	9.8271 73	2.0755 338	20.486 357	9.8704 06
$\frac{1}{4}$	....	....	....	....	....	....	2.1027 751	21.005 241	9.9892 97
$\frac{1}{2}$	....	....	....	2.1200 296	21.333 898	10.063 02	2.1303 741	21.530 935	10.106 65
$\frac{3}{4}$	....	....	....	....	....	....	2.1583 352	22.063 528	10.222 48
15	2.1544 259	21.989 065	10.206 46	2.1756 804	22.393 913	10.292 83	2.1866 634	22.603 112	10.336 81
$\frac{1}{4}$	....	....	....	....	....	....	2.2153 633	23.149 778	10.449 65
$\frac{1}{2}$	....	....	....	2.2327 920	23.481 753	10.516 77	2.2444 400	23.703 619	10.561 40
$\frac{3}{4}$	....	....	....	....	....	....	2.2738 983	24.264 729	10.670 98
16	2.2675 333	24.143 491	10.647 47	2.2914 028	24.598 149	10.734 97	2.3037 432	24.833 203	10.779 50
17	2.3865 788	26 411 025	11.066 48	2.4132 804	26.919 627	11.154 79	2.4270 917	27.182 699	11.199 70
18	2.5118 742	28.797 603	11.464 59	2.5416 405	29.364 581	11.553 40	2.5570 447	29.657 994	11.598 54
19	2.6437 476	31.309 478	11.842 84	2.6768 280	31.939 581	11.931 88	2.6939 557	32.265 822	11.977 12
20	2.7825 443	33.953 225	12.202 22	2.8192 060	34.651 542	12.291 24	2.8381 973	35.013 281	12.336 45
21	2.9286 279	36.735 769	12.543 68	2.9691 569	37.507 750	12.632 46	2.9901 619	37.907 846	12.677 52
22	3.0823 809	39.664 397	12.868 10	3.1270 836	40.515 877	12.956 44	3.1502 631	40.957 393	13.001 26
23	3.2442 059	42.746 778	13.176 35	3.2934 102	43.684 004	13.264 06	3.3189 366	44.170 222	13.308 55
24	3.4145 267	45.990 984	13.469 21	3.4685 836	47.020 640	13.556 15	3.4966 414	47.555 074	13.600 22
25	3.5937 893	49.405 511	13.747 47	3.6530 743	50.534 749	13.833 48	3.6838 609	51.121 159	13.877 06

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0525.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02625.			RATIO *of* INTEREST: *QUARTERLY*, 0.013125.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
½	....	....	....	....	....	....	0.9870 450	4.0000 000	4.0525 000
½	....	....	....	0.9744 214	2.0000 000	2.0525 000	0.9742 579	1.9869 606	2.0394 606
½	....	....	....	....	....	....	0.9616 364	1.3159 855	1.3684 855
1	0.9501 188	1.0000 000	1.0525 000	0.9494 971	0.9870 450	1.0395 450	0.9491 784	0.9805 264	1.0330 264
½	....	....	....	....	....	....	0.9368 819	0.7792 737	0.8317 737
½	....	....	....	0.9252 104	0.6494 690	0.7019 690	0.9247 446	0.6451 245	0.6976 245
½	....	....	....	....	....	....	0.9127 646	0.5493 197	0.6018 197
2	0.9027 257	0.4872 107	0.5397 107	0.9015 448	0.4807 375	0.5332 375	0.9009 397	0.4774 804	0.5299 804
½	....	....	....	....	....	....	0.8892 681	0.4216 181	0.4741 181
½	....	....	....	0.8784 846	0.3795 440	0.4320 440	0.8777 477	0.3769 397	0.4294 397
½	....	....	....	....	....	....	0.8663 765	0.3403 949	0.3928 949
3	0.8576 966	0.3164 300	0.3689 300	0.8560 142	0.3121 193	0.3646 193	0.8551 526	0.3099 504	0.3624 504
½	....	....	....	....	....	....	0.8440 741	0.2841 984	0.3366 984
½	....	....	....	0.8341 187	0.2639 912	0.3164 912	0.8331 392	0.2621 334	0.3146 334
½	....	....	....	....	....	....	0.8223 459	0.2430 181	0.2955 181
4	0.8149 137	0.2311 514	0.2836 514	0.8127 830	0.2279 286	0.2804 286	0.8116 924	0.2262 992	0.2787 992
½	....	....	....	....	....	....	0.8011 770	0.2115 539	0.2640 539
½	....	....	....	0.7919 932	0.1998 956	0.2523 956	0.7907 977	0.1984 539	0.2509 539
½	....	....	....	....	....	....	0.7805 530	0.1867 377	0.2392 377
5	0.7742 644	0.1800 733	0.2325 733	0.7717 352	0.1774 960	0.2299 960	0.7704 409	0.1761 993	0.2286 993
½	....	....	....	....	....	....	0.7604 598	0.1666 700	0.2191 700
½	....	....	....	0.7519 953	0.1591 895	0.2116 895	0.7506 082	0.1580 121	0.2105 121
½	....	....	....	....	....	....	0.7408 841	0.1501 120	0.2026 120
6	0.7356 435	0.1460 954	0.1985 954	0.7327 603	0.1439 529	0.1964 529	0.7312 860	0.1428 750	0 1953 750
½	....	....	....	....	....	....	0.7218 122	0.1362 214	0.1887 214
½	....	....	....	0.7140 174	0.1310 776	0.1835 776	0.7124 611	0.1300 831	0.1825 831
½	....	....	....	....	....	....	0.7032 312	0.1244 054	0.1769 054
7	0.6989 487	0.1218 889	0.1743 889	0.6957 538	0.1200 577	0.1725 577	0.6941 209	0.1191 364	0.1716 364
½	....	....	....	....	....	....	0.6851 286	0.1142 347	0.1667 347
½	....	....	....	0.6779 574	0.1105 219	0.1630 219	0.6762 527	0.1096 635	0.1621 635
½	....	....	....	....	....	....	0.6674 919	0.1053 909	0.1578 909
8	0.6640 842	0.1037 892	0.1562 892	0.6606 163	0.1021 922	0.1546 922	0.6588 445	0.1013 888	0.1538 888
½	....	....	....	....	....	....	0.6503 093	0.0976 327	0.1501 327
½	....	....	....	0.6437 187	0.0948 555	0.1473 555	0.6418 846	0.0941 008	0.1466 008
½	....	....	....	....	....	....	0.6335 689	0.0907 739	0.1432 739
9	0.6309 589	0.0897 606	0.1422 606	0.6272 533	0.0883 463	0.1408 463	0.6253 611	0.0876 349	0.1401 349
½	....	....	....	....	....	....	0.6172 595	0.0846 687	0.1371 687
½	....	....	....	0.6112 090	0.0825 340	0.1350 340	0.6092 630	0.0818 615	0.1343 615
½	....	....	....	....	....	....	0.6013 700	0.0792 011	0.1317 011
10	0.5994 859	0.0785 815	0.1310 815	0.5955 752	0.0773 140	0.1298 140	0.5935 792	0.0766 765	0.1291 765
½	....	....	....	....	....	....	0.5858 895	0.0742 777	0.1267 777
½	....	....	....	0.5803 412	0.0726 016	0.1251 016	0.5782 993	0.0719 959	0.1244 959
½	....	....	....	....	....	....	0.5708 074	0.0698 227	0.1223 227
11	0.5695 828	0.0694 747	0.1219 747	0.5654 970	0.0683 277	0.1208 277	0.5634 126	0.0677 508	0.1202 508
½	....	....	....	....	....	....	0.5561 136	0.0657 735	0.1182 735
½	....	....	....	0.5510 324	0.0644 349	0.1169 349	0.5489 092	0.0638 846	0.1163 846
½	....	....	....	....	....	....	0.5417 981	0.0620 783	0.1145 783
12	0.5411 713	0.0619 218	0.1144 218	0.5369 377	0.0608 757	0.1133 757	0.5347 791	0.0603 496	0.1128 496
½	....	....	....	....	....	....	0.5278 589	0.0586 937	0.1111 937
½	....	....	....	0.5232 037	0.0576 099	0.1101 099	0.5210 128	0.0571 063	0.1096 063
½	....	....	....	....	....	....	0.5142 631	0.0555 832	0.1080 832
13	0.5141 770	0.0555 640	0.1080 640	0.5098 208	0.0546 037	0.1071 037	0.5076 008	0.0541 208	0.1066 208
½	....	....	....	....	....	....	0.5010 249	0.0527 157	0.1052 157
½	....	....	....	0.4967 804	0.0518 282	0.1043 282	0.4945 341	0.0513 646	0.1038 646
½	....	....	....	....	....	....	0.4881 274	0.0500 646	0.1025 646
14	0.4885 292	0.0501 452	0.1026 452	0.4840 734	0.0492 587	0.1017 587	0.4818 038	0.0488 130	0.1013 130
½	....	....	....	....	....	....	0.4755 620	0.0476 072	0.1001 072
½	....	....	....	0.4716 915	0.0468 738	0.0993 738	0.4694 011	0.0464 448	0.0989 448
½	....	....	....	....	....	....	0.4633 201	0.0453 237	0.0978 237
15	0.4641 607	0.0454 771	0.0979 771	0.4596 263	0.0446 550	0.0971 550	0.4573 122	0.0442 417	0.0967 417
½	....	....	....	....	....	....	0.4513 932	0.0431 970	0.0956 970
½	....	....	....	0.4478 697	0.0425 863	0.0950 863	0.4455 454	0.0421 877	0.0946 877
½	....	....	....	....	....	....	0.4397 734	0.0412 121	0.0937 121
16	0.4410 079	0.0414 190	0.0939 190	0.4364 139	0.0406 535	0.0931 535	0 4340 761	0.0402 687	0.0927 687
17	0.4190 098	0.0378 630	0.0903 630	0.4143 739	0.0371 476	0.0896 476	0.4120 138	0.0367 881	0.0892 881
18	0.3981 091	0.0347 251	0.0872 251	0.3934 467	0.0340 546	0.0865 546	0.3910 765	0.0337 177	0.0862 177
19	0.3782 510	0.0319 392	0.0844 392	0.3735 765	0.0313 091	0.0838 091	0.3712 013	0.0309 925	0.0834 925
20	0.3593 833	0.0294 524	0.0819 524	0.3547 098	0.0288 587	0.0813 587	0.3523 363	0.0285 606	0.0810 606
21	0.3414 568	0.0272 214	0.0797 214	0.3367 959	0.0266 612	0.0791 612	0.3344 301	0.0263 798	0.0788 798
22	0.3244 245	0.0252 115	0.0777 115	0.3197 868	0.0246 817	0.0771 817	0.3174 338	0.0244 156	0.0769 156
23	0.3082 418	0.0233 936	0.0758 936	0.3036 366	0.0228 917	0.0753 917	0.3013 013	0.0226 397	0.0751 397
24	0.2928 664	0.0217 434	0.0742 434	0.2883 021	0.0212 673	0.0737 673	0.2859 887	0.0210 282	0.0735 282
25	0.2782 578	0.0202 407	0.0727 407	0.2737 420	0.0197 884	0.0722 884	0.2714 544	0.0195 614	0.0720 614

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0525.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02625.			RATIO *of* INTEREST: *QUARTERLY*, 0.013125.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	3.7824 633	52.999 300	14.011 85	3.8473 779	54.235 770	14.096 81	3.8811 046	54.878 183	14.139 84
27	3.9810 426	56.781 763	14.263 04	4.0520 163	58.133 644	14.346 84	4.0889 093	58.836 368	14.389 26
28	4.1900 473	60.762 806	14.501 70	4.2675 393	62.238 843	14.584 25	4.3078 404	63.006 484	14.626 00
29	4.4100 248	64.952 853	14.728 46	4.4945 257	66.562 394	14.809 66	4.5384 937	67.399 879	14.850 72
30	4.6415 511	69.362 878	14.943 90	4.7335 853	71.115 910	15.023 69	4.7814 967	72.009 462	15.064 02
31	4.8852 325	74.004 429	15.148 60	4.9853 603	75.911 624	15.226 91	5.0375 108	76.904 968	15.266 46
32	5.1417 072	78.889 662	15.343 09	5.2505 269	80.962 417	15.419 87	5.3072 326	82.042 525	15.458 63
33	5.4116 469	84.031 369	15.527 87	5.5297 975	86.281 857	15.603 08	5.5913 960	87.455 161	15.641 03
34	5.6957 583	89.443 016	15.703 44	5.8239 223	91.884 233	15.777 04	5.8907 742	93.157 604	15.814 15
35	5.9947 856	95.138 774	15.870 25	6.1336 912	97.784 595	15.942 21	6.2061 820	99.165 371	15.978 48
36	6.3095 119	101.13 356	16.028 75	6.4599 365	103.99 879	16.099 04	6.5384 775	105.49 481	16.134 47
37	6.6407 613	107.44 307	16.179 33	6.8035 345	110.54 351	16.247 95	6.8885 651	112.16 314	16.282 51
38	6.9894 012	114.08 383	16.322 40	7.1654 081	117.43 634	16.389 34	7.2573 972	119.18 852	16.423 04
39	7.3563 448	121.07 323	16.458 34	7.5465 294	124.69 580	16.523 60	7.6459 776	126 59 005	16.556 42
40	7.7425 529	128.42 958	16.587 50	7.9479 223	132.34 138	16.651 07	8.0553 636	134.38 788	16.683 03
41	8.1490 369	136.17 213	16.710 21	8.3706 648	140.39 361	16.772 10	8.4866 693	142.60 322	16.803 20
42	8.5768 613	144.32 117	16.826 80	8.8158 926	148.87 414	16.887 02	8.9410 682	151.25 844	16.917 27
43	9.0271 466	152.89 803	16.937 58	9.2848 017	157.80 575	16.996 14	9.4197 969	160.37 708	17.025 54
44	9.5010 718	161.92 518	17.042 83	9.7786 516	167.21 241	17.099 74	9.9241 579	169.98 396	17.128 30
45	9.9998 780	171.42 625	17.142 83	10.298 769	177.11 941	17.198 12	10.455 524	180.10 522	17.225 84
46	10.524 872	181.42 613	17.237 85	10.846 551	187.55 335	17.291 52	11.015 340	190.76 839	17.318 43
47	11.077 427	191.95 100	17.328 12	11.423 469	198.54 226	17.380 21	11.605 131	202.00 250	17.406 31
48	11.658 992	203.02 843	17.413 89	12.031 072	210.11 566	17.464 42	12.226 501	213.83 811	17.489 72
49	12.271 089	214.68 742	17.495 38	12.670 994	222.30 464	17.544 37	12.881 140	226.30 741	17.568 89
50	12.915 322	226.95 851	17.572 81	13.344 952	235.14 194	17.620 29	13.570 831	239.44 440	17.644 05
51	13.593 376	239.87 383	17.646 38	14.054 757	248.66 205	17.692 38	14.297 449	253.28 475	17.715 39
52	14.307 028	253.46 720	17.716 27	14.802 317	262.90 127	17.760 82	15.062 973	267.86 615	17.783 09
53	15.058 147	267.77 423	17.782 68	15.589 638	277.89 787	17.825 81	15.869 485	283.22 828	17.847 35
54	15.848 700	282.83 238	17.845 78	16.418 836	293.69 212	17.887 51	16.719 179	299.41 294	17.908 35
55	16.680 757	298.68 108	17.905 73	17.292 139	310.32 645	17.946 10	17.614 369	316.46 417	17.966 25
56	17.556 496	315.36 184	17.962 69	18.211 892	327.84 555	18.001 73	18.557 489	334.42 836	18.021 21
57	18.478 212	332.91 833	18.016 80	19.180 565	346.29 647	18.054 55	19.551 105	353.35 441	18.073 37
58	19.448 319	351.39 655	18.068 22	20.200 761	365.72 878	18.104 70	20.597 925	373.29 381	18.122 88
59	20.469 355	370.84 486	18.117 08	21.275 221	386.19 468	18.152 32	21.700 793	394.30 081	18.169 88
60	21.543 997	391.31 422	18.163 49	22.406 830	407.74 914	18.197 54	22.862 711	416.43 259	18.214 49
61	22.675 056	412.85 822	18.207 59	23.598 628	430.45 006	18.240 47	24.086 842	439.74 936	18.256 83
62	23.865 497	435.53 327	18.249 50	24.853 817	454.35 842	18.281 23	25.376 515	464.31 458	18.297 01
63	25.118 435	459.39 877	18.289 31	26.175 768	479.53 844	18.319 94	26.735 242	490.19 508	18.335 16
64	26.437 153	484.51 720	18.327 13	27.568 033	506.05 777	18.356 69	28.166 718	517.46 129	18.371 37
65	27.825 104	510.95 436	18.363 07	29.034 351	533.98 763	18.391 58	29.674 839	546.18 741	18.405 74
66	29.285 922	538.77 946	18.397 22	30.578 660	563.40 306	18.424 71	31.263 709	576.45 160	18.438 36
67	30.823 433	568.06 538	18.429 66	32.205 111	594.38 306	18.456 17	32.937 651	608.33 622	18.469 33
68	32.441 663	598.88 882	18.460 48	33.918 070	627.01 086	18.486 04	34.701 221	641.92 802	18.498 71
69	34 144 850	631.33 048	18.489 77	35.722 141	661.37 411	18.514 40	36.559 217	677.31 742	18.526 60
70	35.937 455	665.47 533	18.517 60	37.622 168	697.56 510	18.541 33	38.516 695	714.60 371	18.553 09
71	37.824 171	701.41 278	18.544 04	39.623 256	735.68 106	18.566 90	40.578 982	753.88 536	18.578 22
72	39.809 940	739.23 696	18.569 15	41.730 780	775.82 437	18.591 18	42.751 683	795.27 026	18.602 08
73	41.899 962	779.04 690	18.593 02	43.950 401	818.10 287	18.614 23	45.040 728	838.87 101	18.624 72
74	44.099 710	820.94 686	18.615 70	46.288 081	862.63 012	18.636 12	47.452 329	884.80 626	18.646 21
75	46.414 945	865.04 657	18.637 24	48.750 101	909.52 573	18.656 90	49.993 053	933.20 101	18.666 61
76	48.851 729	911.46 151	18.657 71	51.343 073	958.91 568	18.676 63	52.669 814	984.18 694	18.685 98
77	51.416 445	960.31 324	18.677 16	54.073 963	1010.9 326	18.695 37	55.489 897	1037.9 028	18.704 36
78	54.115 809	1011.7 297	18.695 64	56.950 106	1065.7 163	18.713 16	58.460 974	1094.4 947	18.721 80
79	56.956 888	1065.8 455	18.713 20	59.979 229	1123.4 139	18.730 05	61.591 130	1154.1 168	18.738 36
80	59.947 125	1122.8 024	18.729 88	63.169 468	1184.1 803	18.746 09	64.888 884	1216.9 311	18.754 08
81	63.094 349	1182.7 495	18.745 73	66.529 393	1248.1 789	18.761 32	68.363 207	1283.1 087	18.769 00
82	66.406 803	1245.8 439	18.760 79	70.068 029	1315.5 815	18.775 78	72.023 556	1352.8 296	18.783 15
83	69.893 160	1312.2 507	18.775 09	73.794 882	1386.5 692	18.789 50	75.879 889	1426.2 836	18.796 58
84	73.562 551	1382.1 438	18.788 69	77.719 962	1461.3 326	18.802 54	79.942 701	1503.6 705	18.809 35
85	77.424 584	1455.7 064	18.801 60	81.853 814	1540.0 727	18.814 91	84.223 046	1585.2 009	18.821 46
86	81.489 375	1533.1 310	18.813 88	86.207 542	1623.0 008	18.826 67	88.732 573	1671.0 966	18.832 96
87	85.767 567	1614.6 203	18.825 54	90.792 840	1710.3 398	18.837 82	93.483 551	1761.5 915	18.843 86
88	90.270 365	1700.3 879	18.836 61	95.622 026	1802.3 243	18.848 42	98.488 910	1856.9 316	18.854 22
89	95.009 559	1790.6 583	18.847 14	100.70 807	1899.2 014	18.858 48	103.76 223	1957.3 766	18.864 05
90	99.997 561	1885.6 678	18.857 14	106.06 464	2001.2 312	18.868 03	109.31 798	2063.1 996	18.873 38
91	105.24 743	1985.6 654	18.866 64	111.70 612	2108.6 880	18.877 10	115.17 115	2174.6 886	18.882 25
92	110.77 292	2090.9 128	18.875 67	117.64 766	2221.8 602	18.885 72	121.33 772	2292.1 471	18.890 64
93	116.58 850	2201.6 857	18.884 24	123.90 523	2341.0 520	18.893 89	127.83 447	2415.8 947	18.898 62
94	122.70 940	2318.2 742	18.892 39	130.49 563	2466.5 835	18.901 67	134.67 907	2546.2 680	18.906 19
95	129.15 164	2440.9 836	18.900 14	137.43 658	2598.7 919	18.909 03	141.89 015	2683.6 218	18.913 38
96	135.93 210	2570.1 353	18.907 49	144.74 670	2738.0 323	18.916 03	149.48 732	2828.3 299	18.920 20
97	143.06 854	2706.0 674	18.914 48	152.44 564	2884.6 788	18.922 67	157.49 127	2980.7 861	18.926 68
98	150.57 964	2849.1 359	18.921 12	160.55 408	3039.1 253	18.928 98	165.92 377	3141.4 052	18.932 82
99	158.48 507	2999.7 156	18.927 43	169.09 380	3201.7 867	18.934 97	174.80 778	3310.6 243	18.938 65
100	166.80 553	3158.2 006	18.933 43	178.08 774	3373.0 998	18.940 66	184.16 745	3488.9 038	18.944 19
	Value of Perpetual Ann.		19.047 62	- - - - - - - - - -		19.047 62	- - - - - - - - - -		19.047 62

Years.	RATIO of INTEREST: ANNUALLY, 0.0525.			RATIO of INTEREST: HALF-YEARLY, 0.02625.			RATIO of INTEREST: QUARTERLY, 0.013125.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.2643 780	0.0188 682	0.0713 682	0.2599 173	0.0184 380	0.0709 380	0.2576 586	0.0182 222	0.0707 222
27	0.2511 905	0.0176 113	0.0701 113	0.2467 907	0.0172 017	0.0697 017	0.2445 640	0.0169 963	0.0694 963
28	0.2386 608	0.0164 574	0.0689 574	0.2343 271	0.0160 671	0.0685 671	0.2321 349	0.0158 714	0.0683 714
29	0.2267 561	0.0153 958	0.0678 958	0.2224 929	0.0150 235	0.0675 235	0.2203 374	0.0148 368	0.0673 368
30	0.2154 452	0.0144 169	0.0669 169	0.2112 564	0.0140 616	0.0665 616	0.2091 395	0.0138 834	0.0663 834
31	0.2046 986	0.0135 127	0.0660 127	0.2005 873	0.0131 732	0.0656 732	0.1985 107	0.0130 031	0.0655 031
32	0.1944 879	0.0126 759	0.0651 759	0.1904 571	0.0123 514	0.0648 514	0.1884 221	0.0121 888	0.0646 888
33	0.1847 866	0.0119 003	0.0644 003	0.1808 385	0.0115 899	0.0640 899	0.1788 462	0.0114 344	0.0639 344
34	0.1755 693	0.0111 803	0.0636 803	0.1717 056	0.0108 833	0.0633 833	0.1697 570	0.0107 345	0.0632 345
35	0.1668 116	0.0105 110	0.0630 110	0.1630 339	0.0102 266	0.0627 266	0.1611 297	0.0100 842	0.0625 842
36	0.1584 909	0.0098 879	0.0623 879	0.1548 003	0.0096 155	0.0621 155	0.1529 408	0.0094 791	0.0619 791
37	0.1505 851	0.0093 073	0.0618 073	0.1469 824	0.0090 462	0.0615 462	0.1451 681	0.0089 156	0.0614 156
38	0.1430 738	0.0087 655	0.0612 655	0.1395 594	0.0085 153	0.0610 153	0.1377 904	0.0083 901	0.0608 901
39	0.1359 371	0.0082 593	0.0607 593	0.1325 112	0.0080 195	0.0605 195	0.1307 877	0.0078 995	0.0603 995
40	0.1291 564	0.0077 864	0.0602 864	0.1258 190	0.0075 562	0.0600 562	0.1241 409	0.0074 411	0.0599 411
41	0.1227 139	0.0073 436	0.0598 436	0.1194 648	0.0071 228	0.0596 228	0.1178 319	0.0070 125	0.0595 125
42	0.1165 927	0.0069 290	0.0594 290	0.1134 315	0.0067 171	0.0592 171	0.1118 434	0.0066 112	0.0591 112
43	0.1107 770	0.0065 403	0.0590 403	0.1077 029	0.0063 369	0.0588 369	0.1061 594	0.0062 353	0.0587 353
44	0.1052 513	0.0061 757	0.0586 757	0.1022 636	0.0059 805	0.0584 805	0.1007 642	0.0058 829	0.0583 829
45	0.1000 012	0.0058 334	0.0583 334	0.0970 990	0.0056 459	0.0581 459	0.0956 432	0.0055 523	0.0580 523
46	0.0950 130	0.0055 119	0.0580 119	0.0921 952	0.0053 318	0.0578 318	0.0907 825	0.0052 420	0.0577 420
47	0.0902 737	0.0052 097	0.0577 097	0.0875 391	0.0050 367	0.0575 367	0.0861 688	0.0049 504	0.0574 504
48	0.0857 707	0.0049 254	0.0574 254	0.0831 181	0.0047 593	0.0572 593	0.0817 895	0.0046 764	0.0571 764
49	0.0814 924	0.0046 579	0.0571 579	0.0789 204	0.0044 983	0.0569 983	0.0776 329	0.0044 188	0.0569 188
50	0.0774 274	0.0044 061	0.0569 061	0.0749 347	0.0042 528	0.0567 528	0.0736 875	0.0041 763	0.0566 763
51	0.0735 652	0.0041 689	0.0566 689	0.0711 503	0.0040 215	0.0565 215	0.0699 425	0.0039 481	0.0564 481
52	0.0698 957	0.0039 453	0.0564 453	0.0675 570	0.0038 037	0.0563 037	0.0663 880	0.0037 332	0.0562 332
53	0.0664 092	0.0037 345	0.0562 345	0.0641 452	0.0035 984	0.0560 984	0.0630 140	0.0035 307	0.0560 307
54	0.0630 967	0.0035 357	0.0560 357	0.0609 057	0.0034 049	0.0559 049	0.0598 115	0.0033 399	0.0558 399
55	0.0599 493	0.0033 481	0.0558 481	0.0578 297	0.0032 224	0.0557 224	0.0567 718	0.0031 599	0.0556 599
56	0.0569 590	0.0031 710	0.0556 710	0.0549 092	0.0030 502	0.0555 502	0.0538 866	0.0029 902	0.0554 902
57	0.0541 178	0.0030 037	0.0555 037	0.0521 361	0.0028 877	0.0553 877	0.0511 480	0.0028 300	0.0553 300
58	0.0514 183	0.0028 458	0.0553 458	0.0495 031	0.0027 343	0.0552 343	0.0485 486	0.0026 789	0.0551 789
59	0.0488 535	0.0026 965	0.0551 965	0.0470 030	0.0025 894	0.0550 894	0.0460 813	0.0025 361	0.0550 361
60	0.0464 166	0.0025 555	0.0550 555	0.0446 292	0.0024 525	0.0549 525	0.0437 393	0.0024 013	0.0549 013
61	0.0441 013	0.0024 221	0.0549 221	0.0423 753	0.0023 231	0.0548 231	0.0415 164	0.0022 740	0.0547 740
62	0.0419 015	0.0022 960	0.0547 960	0.0402 353	0.0022 009	0.0547 009	0.0394 065	0.0021 537	0.0546 537
63	0.0398 114	0.0021 768	0.0546 768	0.0382 033	0.0020 853	0.0545 853	0.0374 038	0.0020 400	0.0545 400
64	0.0378 256	0.0020 639	0.0545 639	0.0362 739	0.0019 761	0.0544 761	0.0355 029	0.0019 325	0.0544 325
65	0.0359 388	0.0019 571	0.0544 571	0.0344 420	0.0018 727	0.0543 727	0.0336 986	0.0018 309	0.0543 309
66	0.0341 461	0.0018 560	0.0543 560	0.0327 025	0.0017 749	0.0542 749	0.0319 860	0.0017 348	0.0542 348
67	0.0324 429	0.0017 604	0.0542 604	0.0310 510	0.0016 824	0.0541 824	0.0303 604	0.0016 438	0.0541 438
68	0.0308 246	0.0016 698	0.0541 698	0.0294 823	0.0015 949	0.0540 949	0.0288 174	0.0015 578	0.0540 578
69	0.0292 870	0.0015 840	0.0540 840	0.0279 938	0.0015 120	0.0540 120	0.0273 529	0.0014 764	0.0539 764
70	0.0278 261	0.0015 027	0.0540 027	0.0265 801	0.0014 336	0.0539 336	0.0259 628	0.0013 994	0.0538 994
71	0.0264 381	0.0014 257	0.0539 257	0.0252 377	0.0013 593	0.0538 593	0.0246 433	0.0013 265	0.0538 265
72	0.0251 194	0.0013 527	0.0538 527	0.0239 631	0.0012 890	0.0537 890	0.0233 909	0.0012 574	0.0537 574
73	0.0238 664	0.0012 836	0.0537 836	0.0227 529	0.0012 223	0.0537 223	0.0222 021	0.0011 921	0.0536 921
74	0.0226 759	0.0012 181	0.0537 181	0.0216 038	0.0011 592	0.0536 592	0.0210 738	0.0011 302	0.0536 302
75	0.0215 448	0.0011 560	0.0536 560	0.0205 128	0.0010 995	0.0535 995	0.0200 028	0.0010 716	0.0535 716
76	0.0204 701	0.0010 971	0.0535 971	0.0194 768	0.0010 428	0.0535 428	0.0189 862	0.0010 161	0.0535 161
77	0.0194 490	0.0010 413	0.0535 413	0.0184 932	0.0009 892	0.0534 892	0.0180 213	0.0009 635	0.0534 635
78	0.0184 789	0.0009 884	0.0534 884	0.0175 592	0.0009 383	0.0534 383	0.0171 054	0.0009 137	0.0534 137
79	0.0175 571	0.0009 382	0.0534 382	0.0166 724	0.0008 901	0.0533 901	0.0162 361	0.0008 665	0.0533 665
80	0.0166 814	0.0008 906	0.0533 906	0.0158 304	0.0008 445	0.0533 445	0.0154 110	0.0008 217	0.0533 217
81	0.0158 493	0.0008 455	0.0533 455	0.0150 309	0.0008 012	0.0533 012	0.0146 278	0.0007 794	0.0532 794
82	0.0150 587	0.0008 027	0.0533 027	0.0142 718	0.0007 601	0.0532 601	0.0138 843	0.0007 392	0.0532 392
83	0.0143 076	0.0007 620	0.0532 620	0.0135 511	0.0007 212	0.0532 212	0.0131 787	0.0007 011	0.0532 011
84	0.0135 939	0.0007 235	0.0532 235	0.0128 667	0.0006 843	0.0531 843	0.0125 090	0.0006 650	0.0531 650
85	0.0129 158	0.0006 870	0.0531 870	0.0122 169	0.0006 493	0.0531 493	0.0118 732	0.0006 308	0.0531 308
86	0.0122 715	0.0006 523	0.0531 523	0.0115 999	0.0006 161	0.0531 161	0.0112 698	0.0005 984	0.0530 984
87	0.0116 594	0.0006 193	0.0531 193	0.0110 141	0.0005 847	0.0530 847	0.0106 971	0.0005 677	0.0530 677
88	0.0110 778	0.0005 881	0.0530 881	0.0104 578	0.0005 548	0.0530 548	0.0101 534	0.0005 384	0.0530 384
89	0.0105 253	0.0005 585	0.0530 585	0.0099 297	0.0005 265	0.0530 265	0.0096 374	0.0005 109	0.0530 109
90	0.0100 002	0.0005 303	0.0530 303	0.0094 282	0.0004 997	0.0529 997	0.0091 476	0.0004 847	0.0529 847
91	0.0095 014	0.0005 036	0.0530 036	0.0089 521	0.0004 742	0.0529 742	0.0086 827	0.0004 598	0.0529 598
92	0.0090 275	0.0004 783	0.0529 783	0.0085 000	0.0004 501	0.0529 501	0.0082 415	0.0004 363	0.0529 363
93	0.0085 772	0.0004 542	0.0529 542	0.0080 707	0.0004 272	0.0529 272	0.0078 226	0.0004 139	0.0529 139
94	0.0081 493	0.0004 314	0.0529 314	0.0076 631	0.0004 054	0.0529 054	0.0074 251	0.0003 927	0.0528 927
95	0.0077 428	0.0004 097	0.0529 097	0.0072 761	0.0003 848	0.0528 848	0.0070 477	0.0003 726	0.0528 726
96	0.0073 566	0.0003 891	0.0528 891	0.0069 086	0.0003 652	0.0528 652	0.0066 895	0.0003 536	0.0528 536
97	0.0069 897	0.0003 695	0.0528 695	0.0065 597	0.0003 467	0.0528 467	0.0063 496	0.0003 355	0.0528 355
98	0.0066 410	0.0003 510	0.0528 510	0.0062 284	0.0003 290	0.0528 290	0.0060 269	0.0003 183	0.0528 183
99	0.0063 097	0.0003 334	0.0528 334	0.0059 139	0.0003 123	0.0528 123	0.0057 206	0.0003 021	0.0528 021
100	0.0059 950	0.0003 166	0.0528 166	0.0056 152	0.0002 965	0.0527 965	0.0054 298	0.0002 866	0.0527 866
	Ratio of Perpetual Ann.		0.0525 000	- - - - - - - - - -		0.0525 000	- - - - - - - - - -		0.0525 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.055.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.0275.			RATIO *of* INTEREST: *QUARTERLY*, 0.01375.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
½	....	....	....	....	....	....	1.0137 500	0.2500 000	0.2466 09
¾	....	....	....	1.0275 000	0.5000 000	0.4866 18	1.0276 891	0.5034 375	0 4898 73
1	1.0550 000	1.0000 000	0.9478 67	....	....	....	1.0418 198	0.7603 598	0.7298 38
				1.0557 563	1.0137 500	0.9602 12	1.0561 448	1.0208 147	0.9665 48
1¼	....	....	....	....	....	....	1.0706 668	1.2848 509	1.2000 47
1½	....	....	....	1.0847 895	1.5416 281	1.4211 31	1.0853 885	1.5525 176	1.4303 80
1¾	....	....	....	....	....	....	1.1003 126	1.8238 647	1.6575 88
2	1.1130 250	2.0550 000	1.8463 20	1.1146 213	2.0840 229	1.8697 14	1.1154 419	2.0989 429	1.8817 14
2¼	....	....	....	....	....	....	1.1307 792	2.3778 033	2.1028 01
2½	....	....	....	1.1452 733	2.6413 335	2.3062 91	1.1463 274	2.6604 981	2.3208 89
2¾	....	....	....	....	....	....	1.1620 894	2.9470 500	2.5360 18
3	1.1742 414	3.1680 250	2.6979 33	1.1767 684	3.2139 702	2.7311 83	1.1780 681	3.2376 023	2.7432 30
3¼	....	....	....	....	....	....	1.1942 666	3.5321 194	2.9575 64
3½	....	....	....	1.2091 295	3.8023 544	3.1447 04	1.2106 877	3.8306 860	3.1640 58
3¾	....	....	....	....	....	....	1.2273 347	4.1333 579	3.3677 51
4	1.2388 247	4.3422 664	3.5051 50	1.2423 806	4.4069 191	3.5471 57	1.2442 105	4.4401 916	3.5686 82
4¼	....	....	....	....	....	....	1.2613 184	4.7512 442	3.7668 87
4½	....	....	....	1.2765 460	5.0281 094	3.9388 39	1.2786 616	5.0665 739	3.9624 04
4¾	....	....	....	....	....	....	1.2962 432	5.3862 392	4.1552 69
5	1.3069 600	5.5810 910	4.2702 84	1.3116 510	5.6663 824	4.3200 38	1.3140 665	5.7103 000	4.3455 18
5¼	....	....	....	....	....	....	1.3321 349	6.0388 167	4.5331 87
5½	....	....	....	1.3477 214	6.3222 079	4.6910 35	1.3504 518	6.3718 504	4.7183 10
5¾	....	....	....	....	....	....	1.3690 205	6.7094 633	4.9009 23
6	1.3788 428	6.8880 510	4.9955 30	1.3847 838	6.9960 686	5.0521 02	1.3878 445	7.0517 185	5.0810 58
6¼	....	....	....	....	....	....	1.4069 274	7.3986 796	5.2587 50
6½	....	....	....	1.4228 653	7.6884 605	5.4035 05	1.4262 726	7.7504 114	5.4340 32
6¾	....	....	....	....	....	....	1.4458 839	8.1069 796	5.6069 37
7	1.4546 792	8.2668 938	5.6829 67	1.4619 941	8.3998 932	5.7455 04	1.4657 648	8.4684 505	5.7774 96
7¼	....	....	....	....	....	....	1.4859 190	8.8348 917	5.9457 42
7½	....	....	....	1.5021 990	9.1308 903	6.0783 49	1.5063 504	9.2063 715	6.1117 06
7¾	....	....	....	....	....	....	1 5270 628	9.5829 591	6.2754 19
8	1.5346 865	9.7215 730	6.3345 66	1.5435 094	9.8819 897	6.4022 87	1.5480 599	9.9647 248	6.4369 12
8¼	....	....	....	....	....	....	1.5693 457	10.351 740	6.5962 14
8½	....	....	....	1.5859 559	10.653 744	6.7175 54	1.5909 242	10.744 076	6.7533 55
8¾	....	....	....	....	....	....	1.6127 994	11.141 807	6.9083 65
9	1.6190 943	11.256 260	6.9521 95	1 6295 697	11.446 722	7.0243 83	1.6349 754	11.545 007	7.0612 73
9¼	....	....	....	....	....	....	1.6574 563	11.953 751	7.2121 06
9½	....	....	....	1.6743 829	12.261 507	7.3230 01	1.6802 463	12.368 115	7.3608 94
9¾	....	....	....	....	....	....	1.7033 497	12.788 177	7.5076 64
10	1.7081 445	12.875 354	7.5376 26	1.7204 284	13.098 699	7.6136 26	1.7267 708	13.214 014	7.6524 42
10¼	....	....	....	....	....	....	1.7505 139	13.645 707	7.7952 58
10½	....	....	....	1.7677 402	13.958 913	7.8964 73	1.7745 834	14.083 335	7.9361 36
10¾	....	....	....	....	....	....	1.7989 840	14.526 981	8.0751 03
11	1.8020 924	14.583 498	8.0925 36	1.8163 531	14.842 783	8.1717 50	1.8237 200	14.976 727	8.2121 86
11¼	....	....	....	....	....	....	1.8487 961	15.432 657	8.3474 09
11½	....	....	....	1.8663 028	15.750 960	8.4396 59	1.8742 171	15.894 856	8.4807 98
11¾	....	....	....	....	....	....	1.8999 876	16.363 410	8.6123 78
12	1.9012 075	16.385 591	8.6185 18	1.9176 261	16.684 111	8.7003 98	1.9261 124	16.838 407	8.7421 73
12¼	....	....	....	....	....	....	1.9525 964	17.319 935	8.8702 07
12½	....	....	....	1.9703 608	17.642 924	8.9541 59	1.9794 446	17.808 084	8.9965 05
12¾	....	....	....	....	....	....	2.0066 620	18.302 946	9.1210 90
13	2.0057 739	18.286 798	9.1170 78	2.0245 457	18.628 104	9.2011 28	2.0342 536	18.804 611	9.2439 86
13¼	....	....	....	....	....	....	2.0622 246	19.313 174	9.3652 14
13½	....	....	....	2.0802 208	19.640 377	9.4414 87	2.0905 802	19.828 731	9.4847 98
13¾	....	....	....	....	....	....	2.1193 257	20.351 376	9.6027 60
14	2.1160 915	20.292 572	9.5896 48	2.1374 268	20.680 488	9.6754 13	2.1484 664	20 831 207	9.7191 22
14¼	....	....	....	....	....	....	2.1780 078	21.418 324	9.8339 06
14½	....	....	....	2.1962 061	21.749 201	9.9030 78	2.2079 554	21.962 826	9.9471 33
14¾	....	....	....	....	....	....	2.2383 148	22.514 815	10.058 82
15	2.2324 765	22.408 663	10.037 58	2.2566 017	22.847 304	10.124 65	2.2690 916	23.074 393	10.169 00
15¼	....	....	....	....	....	....	2.3002 916	23.641 666	10.277 68
15½	....	....	....	2.3186 583	23.975 605	10.340 29	2.3319 206	24.216 739	10.384 89
15¾	....	....	....	....	....	....	2.3639 846	24.799 719	10.490 64
16	2.3552 627	24.641 140	10.462 16	2.3824 214	25.134 934	10.550 16	2.3964 893	25.390 715	10.594 96
17	2.4848 021	26.996 403	10.864 61	2.5152 563	27.550 114	10.953 20	2.5310 398	27.837 087	10.996 28
18	2.6214 663	29.481 205	11.246 07	2.6554 975	30.099 955	11.334 96	2.6731 445	30.420 810	11.380 16
19	2.7656 469	32.102 671	11.607 65	2.8035 581	32.791 965	11.696 55	2 8232 277	33.149 595	11.741 74
20	2.9177 575	34.868 318	11.950 38	2.9598 740	35.634 072	12.039 05	2.9817 373	36.031 587	12.084 09
21	3.0782 342	37.786 076	12.275 24	3.1249 055	38.634 645	12.363 46	3.1491 464	39.075 388	12.408 25
22	3.2475 370	40.864 310	12.583 17	3.2991 385	41.802 518	12.670 74	3.3259 546	42.290 083	12.715 17
23	3.4261 516	44.111 847	12.875 04	3.4830 861	45.147 010	12.961 79	3.5126 897	45.685 257	13.005 78
24	3.6145 899	47.537 998	13.151 70	3.6772 899	48.677 998	13.237 46	3.7099 090	49.271 072	13.280 94
25	3.8133 923	51.152 588	13.413 93	3.8823 218	52.405 850	13.498 58	3.9182 011	53.058 202	13.541 47

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.055.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.0275.			RATIO *of* INTEREST: *QUARTERLY*, 0.01375.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
¼	....	....	....	....	....	....	0.9864 365	4.0000 000	4.0550 000
½	....	....	....	0.9732 360	2.0000 000	2.0550 000	0.9730 570	1.9863 440	2.0413 440
¾	....	....	....	....	....	....	0.9598 589	1.3151 668	1.3701 668
1	0.9478 673	1.0000 000	1.0550 000	0.9471 883	0.9864 365	1.0414 365	0.9468 398	0.9796 097	1.0346 097
¼	....	....	....	....	....	....	0.9339 974	0.7783 005	0.8333 005
½	....	....	....	0.9218 378	0.6486 649	0.7036 649	0.9213 291	0.6441 151	0.6991 151
¾	....	....	....	....	....	....	0 9088 326	0.5482 863	0.6032 863
2	0.8984 524	0.4866 180	0.5416 180	0.8971 658	0.4798 412	0.5348 412	0.8965 058	0.4764 304	0.5314 304
¼	....	....	....	....	....	....	0.8843 459	0.4205 562	0.4755 562
½	....	....	....	0.8731 540	0.3785 966	0.4335 966	0.8723 511	0.3758 695	0.4308 695
¾	....	....	....	....	....	....	0.8605 190	0.3393 189	0.3943 189
3	0.8516 136	0.3156 541	0.3706 541	0.8497 849	0.3111 417	0.3661 417	0.8488 473	0.3088 705	0.3638 705
¼	....	....	....	....	....	....	0.8373 340	0.2831 161	0.3381 161
½	....	....	....	0.8270 413	0.2629 950	0.3179 950	0.8259 768	0.2610 499	0.3160 499
¾	....	....	....	....	....	....	0.8147 737	0.2419 340	0.2969 340
4	0.8072 167	0.2302 945	0.2852 945	0.8049 064	0.2269 159	0.2819 159	0.8037 225	0.2252 155	0.2802 155
¼	....	....	....	....	....	....	0.7928 212	0.2104 712	0.2654 712
½	....	....	....	0.7833 639	0.1988 819	0.2538 819	0.7820 678	0 1973 721	0.2523 721
¾	....	....	....	....	....	....	0.7714 602	0.1856 583	0.2406 583
5	0.7651 344	0.1791 764	0.2341 764	0.7623 979	0.1764 794	0.2314 794	0.7609 965	0.1751 222	0.2301 222
¼	....	....	....	....	....	....	0.7506 747	0.1655 954	0.2205 954
½	....	....	....	0.7419 931	0.1581 726	0.2131 726	0.7404 929	0.1569 403	0.2119 403
¾	....	....	....	....	....	....	0.7304 493	0.1490 432	0.2040 432
6	0.7252 458	0.1451 790	0.2001 790	0.7221 344	0.1429 374	0.1979 374	0.7205 418	0.1418 094	0.1958 094
¼	....	....	....	....	....	....	0.7107 687	0 1351 593	0.1901 593
½	....	....	....	0.7028 072	0.1300 651	0.1850 651	0.7011 282	0.1290 254	0.1840 254
¾	....	....	....	....	....	....	0.6916 185	0.1233. 505	0.1783 505
7	0.6874 368	0.1209 644	0.1759 644	0.6839 972	0.1190 491	0.1740 491	0.6822 377	0.1180 854	0.1730 854
¼	....	....	....	....	....	....	0.6729 842	0.1131 876	0.1681 876
½	....	....	....	0.6656 908	0.1095 183	0.1645 183	0.6638 561	0.1086 204	0.1636 204
¾	....	....	....	....	....	....	0.6548 519	0.1043 519	0.1593 519
8	0.6515 989	0.1028 640	0.1578 640	0.6478 742	0.1011 942	0.1561 942	0.6459 699	0.1003 540	0.1553 540
¼	....	....	....	....	....	....	0.6372 082	0.0966 021	0.1516 021
½	....	....	....	0.6305 345	0.0938 628	0.1488 628	0.6285 655	0.0930 745	0.1480 745
¾	....	....	....	....	....	....	0.6200 399	0.0897 520	0.1447 520
9	0.6176 291	0.0888 395	0.1438 395	0.6136 589	0.0873 613	0.1423 613	0.6116 300	0.0866 175	0.1416 175
¼	....	....	....	....	....	....	0.6033 342	0.0836 557	0.1386 557
½	....	....	....	0.5972 350	0.0815 560	0.1365 560	0.5951 509	0.0808 531	0.1358 531
¾	....	....	....	....	....	....	0.5870 785	0.0781 972	0.1331 972
10	0.5854 306	0.0776 678	0.1326 678	0.5812 505	0.0763 435	0.1313 435	0.5791 156	0.0756 772	0.1306 772
¼	....	....	....	....	....	....	0.5712 608	0.0732 831	0.1282 831
½	....	....	....	0.5656 940	0.0716 388	0.1266 388	0.5635 126	0.0710 059	0.1260 059
¾	....	....	....	....	....	....	0.5558 693	0.0688 374	0.1238 374
11	0.5549 105	0.0685 707	0.1235 707	0.5505 537	0.0673 728	0.1223 728	0.5483 298	0.0667 703	0.1217 703
¼	....	....	....	....	....	....	0.5408 925	0.0647 977	0.1197 977
½	....	....	....	0.5358 188	0.0634 882	0.1184 882	0.5335 561	0.0629 134	0.1179 134
¾	....	....	....	....	....	....	0.5263 192	0.0611 120	0.1161 120
12	0.5259 815	0.0610 292	0.1160 292	0.5214 781	0.0599 373	0.1149 373	0.5191 805	0.0593 880	0.1143 880
¼	....	....	....	....	....	....	0.5121 386	0.0577 368	0.1127 368
½	....	....	....	0.5075 212	0.0566 800	0.1116 800	0.5051 922	0.0561 543	0.1111 543
¾	....	....	....	....	....	....	0.4983 400	0.0546 360	0.1096 360
13	0.4985 607	0.0546 843	0.1096 843	0.4939 380	0.0536 823	0.1086 823	0.4915 808	0.0531 784	0.1081 784
¼	....	....	....	....	....	....	0.4849 133	0.0517 781	0.1067 781
½	....	....	....	0.4807 182	0.0509 155	0.1059 155	0.4783 361	0.0504 319	0.1054 319
¾	....	....	....	....	....	....	0.4718 482	0.0491 367	0.1041 367
14	0.4725 694	0.0492 791	0.1042 791	0.4678 523	0.0483 548	0.1033 548	0.4654 483	0.0478 900	0.1028 900
¼	....	....	....	....	....	....	0.4591 352	0.0466 890	0.1016 890
½	....	....	....	0.4553 307	0.0459 787	0.1009 787	0.4529 077	0.0455 315	0.1005 315
¾	....	....	....	....	....	....	0.4467 647	0.0444 152	0.0994 152
15	0.4479 330	0.0446 256	0.0996 256	0.4431 442	0.0437 688	0.0987 688	0.4407 050	0.0433 381	0.0983 381
¼	....	....	....	....	....	....	0.4347 275	0.0422 982	0.0972 982
½	....	....	....	0.4312 839	0.0417 091	0.0967 091	0.4288 312	0.0412 937	0.0962 937
¾	....	....	....	....	....	....	0.4230 146	0.0403 230	0.0953 230
16	0.4245 811	0.0405 825	0.0955 825	0.4197 410	0.0397 853	0.0947 853	0.4172 770	0.0393 845	0.0943 845
17	0.4024 465	0.0370 420	0.0920 420	0.3975 738	0.0362 975	0.0912 975	0.3950 945	0.0359 233	0.0909 233
18	0.3814 659	0.0339 200	0.0889 200	0.3765 773	0.0332 226	0.0882 226	0.3740 913	0.0328 722	0.0878 722
19	0.3615 791	0.0311 501	0.0861 501	0.3566 896	0.0304 953	0.0854 953	0.3542 045	0.0301 663	0.0851 663
20	0.3427 290	0.0286 793	0.0836 793	0.3378 522	0.0280 630	0.0830 630	0.3353 749	0.0277 534	0.0827 534
21	0.3248 616	0.0264 648	0.0814 648	0.3200 097	0.0258 835	0.0808 835	0.3175 464	0.0255 916	0.0805 916
22	0.3079 257	0.0244 712	0.0794 712	0.3031 094	0.0239 220	0.0789 220	0.3006 656	0.0236 462	0.0786 462
23	0.2918 727	0.0226 696	0.0776 696	0.2871 017	0.0221 499	0.0771 499	0.2846 821	0.0218 889	0.0768 889
24	0.2766 565	0.0210 358	0.0760 358	0.2719 394	0.0205 432	0.0755 432	0.2695 484	0.0202 959	0.0752 959
25	0.2622 337	0.0195 494	0.0745 494	0.2575 778	0.0190 818	0.0740 818	0.2552 192	0.0188 472	0.0738 472

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.055.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.0275.			RATIO *of* INTEREST: *QUARTERLY*, 0.01375.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	4.0231 289	54.965 981	13.662 50	4.0987 855	56.341 554	13.745 92	4.1381 878	57.057 959	13.788 15
27	4.2444 010	58.989 109	13.898 10	4.3273 184	60.496 698	13.980 18	4.3705 255	61.282 282	14.021 72
28	4.4778 431	63.233 510	14.121 42	4.5685 934	64.883 517	14.209 08	4.6159 078	65.743 779	14.242 87
29	4.7241 244	67.711 354	14.333 10	4.8233 211	69.514 928	14.412 25	4.8750 671	70.455 765	14.452 26
30	4.9839 513	72.435 478	14.533 74	5.0922 514	74.404 570	14.611 33	5.1487 768	75.432 306	14.650 53
31	5.2580 686	77.419 429	14.723 93	5.3761 762	79.566 840	14.799 89	5.4378 539	80.688 253	14.838 25
32	5.5472 624	82.677 498	14.904 20	5.6759 316	85.016 939	14.978 50	5.7431 612	86.239 294	15.016 00
33	5.8523 618	88.224 760	15.075 07	5.9924 003	90.770 914	15.147 67	6.0656 099	92.101 997	15.184 29
34	6.1742 417	94.077 122	15.237 03	6.3265 141	96.845 710	15.307 91	6.4061 624	98.293 861	15.343 64
35	6.5138 250	100.25 136	15.390 55	6.6792 568	103.25 921	15.459 69	6.7658 351	104.83 337	15.494 52
36	6.8720 854	106.76 519	15.536 07	7.0516 671	110.03 031	15.603 45	7.1457 017	111.74 003	15.637 38
37	7.2500 501	113.63 727	15.674 00	7.4448 416	117.17 894	15.739 62	7.5468 957	119.03 447	15.772 64
38	7.6488 028	120.88 732	15.804 74	7.8599 380	124.72 615	15.868 59	7.9706 147	126.73 845	15.900 71
39	8.0694 870	128.53 613	15.928 66	8.2981 787	132.69 416	15.990 76	8.4181 234	134.87 497	16.021 98
40	8.5133 088	136.60 561	16.046 12	8.7608 540	141.10 644	16.106 47	8.8907 573	143.46 831	16.136 80
41	8.9815 408	145.11 892	16.157 46	9.2493 264	149.98 775	16.216 07	9.3899 272	152.54 413	16.245 51
42	9.4755 255	154.10 046	16.263 00	9.7650 341	159.36 426	16.319 89	9.9171 228	162.12 951	16.348 44
43	9.9966 794	163.57 599	16.363 03	10.309 496	169.26 356	16.418 22	10.473 918	172.25 305	16.445 90
44	10.546 497	173.57 267	16.457 85	10.884 315	179.71 481	16.511 36	11.061 974	182.94 498	16.538 19
45	11.126 554	184.11 917	16.547 75	11.491 183	190.74 879	16.599 58	11.683 046	194.23 721	16.625 56
46	11.738 515	195.24 572	16.632 92	12.131 889	202.39 797	16.683 14	12.338 939	206.16 343	16.708 29
47	12.384 133	206.98 423	16.713 66	12.808 317	214.69 667	16.762 29	13.031 759	218.75 925	16.786 63
48	13.065 260	219.36 837	16.790 20	13.522 461	227.68 111	16.837 25	13.763 425	232.06 226	16.860 79
49	13.783 849	232.43 363	16.862 75	14.276 423	241.38 950	16.908 26	14.536 169	246.11 217	16.931 02
50	14.541 961	246.21 748	16.931 52	15.072 422	255.86 222	16.975 52	15.352 300	260.95 091	16.997 51
51	15.341 769	260.75 944	16.996 70	15.912 804	271.14 189	17.039 23	16.214 252	276.62 276	17.060 47
52	16.185 566	276.10 121	17.058 48	16.800 042	287.27 350	17.099 57	17.124 598	293.17 451	17.120 08
53	17.075 773	292.28 677	17.117 05	17.736 750	304.30 454	17.156 72	18.086 055	310.65 555	17.176 52
54	18.014 940	309.36 255	17.172 55	18.725 684	322.28 517	17.210 86	19.101 493	329.11 806	17.229 97
55	19.005 762	327.37 749	17.225 17	19.769 758	341.26 833	17.262 14	20.173 943	348.61 714	17.280 56
56	20.051 079	346.38 325	17.275 04	20.872 046	361.30 993	17.310 71	21.306 605	369.21 100	17.328 48
57	21.153 888	366.43 433	17.322 32	22.035 793	382.46 896	17.356 71	22.502 860	390.96 110	17.373 84
58	22.317 352	387.58 821	17.367 12	23.264 426	404.80 775	17.400 29	23.766 279	413.93 235	17.416 79
59	23.544 806	409.90 557	17.409 60	24.561 563	428.39 206	17.441 56	25.100 632	438.19 332	17.457 46
60	24.839 770	433.45 037	17.449 85	25.931 024	453.29 134	17.480 66	26.509 903	463.81 641	17.495 97
61	26.205 958	458.29 014	17.488 01	27.376 841	479.57 892	17.517 69	27.998 296	490.87 811	17.532 43
62	27.647 285	484.49 610	17.524 18	28.903 271	507.33 219	17.552 76	29.570 255	519.45 918	17.566 95
63	29.167 886	512.14 339	17.558 47	30.514 809	536.63 288	17.585 98	31.230 471	549.64 493	17.599 64
64	30.772 120	541.31 127	17.590 96	32.216 200	567.56 727	17.617 45	32.983 900	581.52 546	17.630 59
65	32.464 587	572.08 339	17.621 77	34.012 454	600.22 644	17.647 25	34 835 775	615.19 591	17.659 89
66	34.250 139	604.54 798	17.650 96	35.908 861	634.70 657	17.675 49	36.791 623	650.75 678	17.687 64
67	36.133 896	638.79 812	17.678 64	37.911 005	671.10 918	17.702 23	38.857 282	688.31 421	17.713 91
68	38.121 261	674.93 201	17 704 87	40.024 780	709.54 146	17.727 56	41.038 916	727.98 030	17.738 78
69	40.217 930	713.05 327	17.729 74	42.256 412	750.11 658	17.751 54	43.343 038	769.87 343	17.762 33
70	42.429 916	753.27 120	17.753 30	44.612 471	792.95 401	17.774 27	45.776 525	814.11 864	17.784 63
71	44.763 562	795.70 112	17.775 64	47.099 895	838.17 991	17.795 79	48.346 639	860.84 799	17.805 75
72	47.225 538	840.46 468	17.796 82	49.720 008	885.92 743	17.816 18	51.061 052	910.20 095	17.825 74
73	49.822 963	887.69 024	17.816 89	52.498 544	936.33 717	17.835 49	53.927 865	962.32 482	17.844 67
74	52.563 226	937.51 320	17.835 91	55.425 666	989.55 757	17.853 78	56.955 635	1017.3 752	17.862 59
75	55.454 204	990.07 643	17.853 95	58.515 993	1045.7 453	17.871 10	60.153 398	1075.5 163	17.879 56
76	58.504 185	1045.5 306	17.871 04	61.778 626	1105.0 659	17.887 51	63.530 699	1136.9 218	17.895 63
77	61.721 915	1104.0 348	17.887 24	65.223 170	1167.6 940	17.903 05	67.097 618	1201.7 749	17.910 84
78	65.116 620	1165.7 567	17.902 60	68.859 770	1233.8 140	17.917 78	70.864 801	1270.2 691	17.925 25
79	68.698 034	1230.8 734	17.917 16	72.699 132	1303.6 206	17.931 72	74.843 492	1342.6 089	17.938 89
80	72.476 426	1299.5 714	17.930 95	76.752 563	1377.3 193	17.944 93	79.045 565	1419.0 103	17.951 80
81	76.462 630	1372.0 478	17.944 03	81.031 998	1455.1 272	17.957 44	83.483 564	1499.7 012	17.964 03
82	80.668 074	1448.5 104	17.956 43	85.550 039	1537.2 734	17.969 29	88.170 732	1584.9 224	17.975 61
83	85.104 818	1529.1 785	17.968 18	90.319 988	1623.9 998	17.980 52	93.121 061	1674.9 284	17.986 57
84	89.785 583	1614.2 833	17 979 32	95.355 892	1715.5 617	17.991 14	98.349 325	1769.9 877	17.996 95
85	94.723 791	1704.0 689	17.989 87	100.67 258	1812.2 287	18.001 21	103.87 113	1870.3 842	18.006 78
86	99.933 599	1798.7 927	17.999 88	106.28 570	1914.2 855	18.010 75	109.70 295	1976.4 174	18.016 08
87	105.42 995	1898.7 263	18.009 36	112.21 180	2022.0 327	18.019 79	115.86 221	2088.4 037	18.024 89
88	111.22 859	2004.1 563	18.018 35	118.46 831	2135.7 874	18.028 34	122.36 727	2206.6 776	18.033 23
89	117.34 617	2115.3 848	18.026 88	125.07 365	2255.8 846	18.036 45	129.23 755	2331.5 919	18.041 13
90	123.80 021	2232.7 310	18.034 95	132.04 729	2382.6 780	18.044 13	136.49 357	2463.5 195	18.048 61
91	130.60 922	2356.5 312	18.042 61	139.40 975	2516.5 410	18.051 40	144.15 698	2602.8 541	18.055 69
92	137.79 272	2487.1 404	18.049 87	147.18 272	2657.8 676	18.058 29	152.25 064	2750.0 117	18.062 40
93	145.37 132	2624.9 332	18.056 75	155.38 908	2807.0 741	18.064 81	160.79 873	2905.4 314	18.068 75
94	153.36 675	2770.3 045	18.063 27	164.05 299	2964.5 998	18.070 99	169.82 674	3069.5 771	18.074 76
95	161.80 192	2923.6 712	18.069 45	173.19 997	3130.9 085	18.076 84	179.36 163	3242.9 387	18.080 45
96	170.70 102	3085.4 732	18.075 31	182.85 695	3306.4 900	18.082 39	189.43 186	3426.0 337	18.085 84
97	180.08 958	3256.1 742	18.080 86	193.05 236	3491.8 612	18.087 64	200.06 747	3619.4 085	18.090 94
98	189.99 451	3436.2 638	18.086 12	203.81 624	3687.5 680	18.092 61	211.30 022	3823.6 404	18.095 77
99	200.44 420	3626.2 583	18.091 11	215.18 027	3894.1 867	18.097 32	223.16 363	4039.3 387	18.100 35
100	211.46 864	3826.7 025	18.095 84	227.17 792	4112.3 257	18.101 78	235.69 311	4267.1 475	18.104 68
	Value of Perpetual Ann.		18.181 82	- - - - - - - - - -		18.181 82	- - - - - - - - - -		18.181 82

Years.	RATIO of INTEREST: ANNUALLY, 0.055.			RATIO of INTEREST: HALF-YEARLY, 0.0275.			RATIO of INTEREST: QUARTERLY, 0.01375.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.2485 628	0.0181 931	0.0731 931	0.2439 747	0.0177 489	0.0727 489	0.2416 517	0.0175 260	0.0725 260
27	0.2356 045	0.0169 523	0.0719 523	0.2310 900	0.0165 298	0.0715 298	0.2288 054	0.0163 179	0.0713 179
28	0.2233 218	0.0158 144	0.0708 144	0.2188 858	0.0154 122	0.0704 122	0 2166 421	0.0152 106	0.0702 106
29	0.2116 794	0.0147 686	0.0697 686	0.2073 260	0.0143 854	0.0693 854	0.2051 254	0.0141 933	0.0691 933
30	0.2006 440	0.0138 054	0.0688 054	0.1963 768	0.0134 400	0.0684 400	0.1942 209	0.0132 569	0.0682 569
31	0.1901 839	0.0129 167	0.0679 167	0.1860 058	0.0125 680	0.0675 680	0.1838 961	0.0123 934	0.0673 934
32	0.1802 691	0.0120 952	0.0670 952	0.1761 825	0.0117 623	0.0667 623	0.1741 201	0.0115 956	0.0665 956
33	0.1708 712	0.0113 347	0.0663 347	0.1668 780	0.0110 167	0.0660 167	0.1648 639	0.0108 575	0.0658 575
34	0.1619 632	0.0106 296	0.0656 296	0.1580 649	0.0103 257	0.0653 257	0.1560 997	0.0101 736	0.0651 736
35	0.1535 196	0.0099 749	0.0649 749	0.1497 173	0.0096 844	0.0646 844	0.1478 014	0.0095 389	0.0645 389
36	0.1455 162	0.0093 663	0.0643 663	0.1418 104	0.0090 884	0.0640 884	0.1399 443	0.0089 493	0.0639 493
37	0.1379 301	0.0087 999	0.0637 999	0.1343 212	0.0085 340	0.0635 340	0.1325 048	0.0084 009	0.0634 009
38	0.1307 394	0.0082 722	0.0632 722	0.1272 275	0.0080 176	0.0630 176	0.1254 608	0.0078 903	0.0628 903
39	0.1239 236	0.0077 799	0.0627 799	0.1205 084	0.0075 361	0.0625 361	0.1187 913	0.0074 143	0.0624 143
40	0.1174 631	0.0073 203	0.0623 203	0.1141 441	0.0070 868	0.0620 868	0.1124 764	0.0069 702	0.0619 702
41	0.1113 395	0.0068 909	0.0618 909	0.1081 160	0.0066 672	0.0616 672	0.1064 971	0.0065 555	0.0615 555
42	0.1055 350	0.0064 893	0.0614 893	0.1024 052	0.0062 749	0.0612 749	0.1008 357	0.0061 679	0.0611 679
43	0.1000 332	0.0061 134	0.0611 134	0.0969 980	0.0059 079	0.0609 079	0.0954 753	0.0058 054	0.0608 054
44	0.0948 182	0.0057 613	0.0607 613	0.0918 753	0.0055 644	0.0605 644	0.0903 998	0.0054 661	0.0604 661
45	0.0898 751	0.0054 313	0.0604 313	0.0870 232	0.0052 425	0.0602 425	0.0855 941	0.0051 483	0.0601 483
46	0.0851 897	0.0051 218	0.0601 218	0.0824 274	0.0049 408	0.0599 408	0.0810 439	0.0048 505	0.0598 505
47	0.0807 485	0.0048 313	0.0598 313	0.0780 743	0.0046 577	0.0596 577	0.0767 356	0.0045 712	0.0595 712
48	0.0765 388	0.0045 585	0.0595 585	0.0739 510	0.0043 921	0.0593 921	0.0726 563	0.0043 092	0.0593 092
49	0.0725 487	0.0043 023	0 0593 023	0.0700 456	0.0041 427	0.0591 427	0.0687 939	0.0040 632	0.0590 632
50	0.0687 665	0.0040 615	0.0590 615	0.0663 463	0.0039 084	0.0589 084	0.0651 368	0.0038 321	0.0588 321
51	0.0651 815	0.0038 350	0.0588 350	0.0628 425	0.0036 881	0.0586 881	0.0616 741	0.0036 150	0.0586 150
52	0.0617 834	0.0036 219	0.0586 219	0.0595 237	0.0034 810	0.0584 810	0.0583 955	0.0034 109	0.0584 109
53	0.0585 625	0.0034 213	0.0584 213	0.0563 801	0.0032 862	0.0582 862	0.0552 912	0.0032 190	0.0582 190
54	0.0555 095	0.0032 325	0.0582 325	0.0534 026	0.0031 028	0.0581 028	0.0523 519	0.0030 384	0.0580 384
55	0.0526 156	0.0030 546	0.0580 546	0.0505 823	0.0029 302	0.0579 302	0.0495 689	0.0028 685	0.0578 685
56	0.0498 726	0.0028 870	0.0578 870	0.0479 110	0.0027 677	0.0577 677	0.0469 338	0.0027 085	0.0577 085
57	0.0472 726	0.0027 290	0.0577 290	0.0453 807	0.0026 146	0.0576 146	0.0444 388	0.0025 578	0.0575 578
58	0.0448 082	0.0025 801	0.0575 801	0.0429 841	0.0024 703	0.0574 703	0.0420 764	0.0024 159	0.0574 159
59	0.0424 722	0 0024 396	0.0574 396	0.0407 140	0.0023 343	0.0573 343	0.0398 396	0.0022 821	0.0572 821
60	0.0402 580	0.0023 071	0.0573 071	0.0385 638	0.0022 061	0.0572 061	0.0377 218	0.0021 560	0.0571 560
61	0.0381 593	0.0021 820	0.0571 820	0.0365 272	0.0020 852	0.0570 852	0.0357 165	0.0020 372	0.0570 372
62	0.0361 699	0.0020 640	0.0570 640	0.0345 982	0.0019 711	0.0569 711	0.0338 178	0.0019 251	0.0569 251
63	0.0342 843	0.0019 526	0.0569 526	0.0327 710	0.0018 635	0.0568 635	0.0320 200	0.0018 194	0.0568 194
64	0.0324 969	0.0018 474	0.0568 474	0.0310 403	0.0017 619	0.0567 619	0.0303 178	0.0017 196	0.0567 196
65	0.0308 028	0.0017 480	0.0567 480	0.0294 010	0.0016 660	0.0566 660	0.0287 061	0.0016 255	0.0566 255
66	0.0291 970	0.0016 541	0.0566 541	0.0278 483	0.0015 755	0.0565 755	0.0271 801	0.0015 367	0.0565 367
67	0.0276 748	0.0015 654	0.0565 654	0.0263 776	0.0014 901	0.0564 901	0.0257 352	0.0014 528	0.0564 528
68	0.0262 321	0.0014 816	0.0564 816	0.0249 845	0.0014 094	0.0564 094	0.0243 671	0.0013 737	0.0563 737
69	0.0248 645	0.0014 024	0.0564 024	0.0236 650	0.0013 331	0.0563 331	0.0230 718	0.0012 989	0.0562 989
70	0.0235 683	0.0013 275	0.0563 275	0.0224 153	0.0012 611	0.0562 611	0.0218 453	0.0012 283	0.0562 283
71	0.0223 396	0.0012 568	0.0562 568	0.0212 315	0.0011 931	0.0561 931	0.0206 840	0.0011 616	0.0561 616
72	0.0211 750	0.0011 898	0.0561 898	0.0201 102	0.0011 288	0.0561 288	0.0195 844	0.0010 987	0.0560 987
73	0.0200 711	0.0011 265	0.0561 265	0.0190 481	0.0010 680	0.0560 680	0.0185 433	0.0010 392	0.0560 392
74	0.0190 247	0.0010 667	0.0560 667	0.0180 422	0.0010 106	0.0560 106	0.0175 575	0.0009 829	0.0559 829
75	0.0180 329	0.0010 100	0.0560 100	0.0170 893	0.0009 563	0.0559 563	0.0166 242	0.0009 298	0.0559 298
76	0.0170 928	0.0009 565	0.0559 565	0.0161 868	0.0009 049	0.0559 049	0.0157 404	0.0008 796	0.0558 796
77	0.0162 017	0.0009 058	0.0559 058	0.0153 320	0.0008 564	0.0558 564	0.0149 037	0.0008 321	0.0558 321
78	0.0153 571	0.0008 578	0.0558 578	0.0145 223	0.0008 105	0.0558 105	0.0141 114	0.0007 872	0.0557 872
79	0.0145 565	0.0008 124	0.0558 124	0.0137 553	0.0007 671	0.0557 671	0.0133 612	0.0007 448	0.0557 448
80	0.0137 976	0.0007 695	0.0557 695	0.0130 289	0.0007 260	0.0557 260	0.0126 509	0.0007 047	0.0557 047
81	0.0130 783	0.0007 288	0.0557 288	0.0123 408	0.0006 872	0.0556 872	0.0119 784	0.0006 668	0.0556 668
82	0.0123 965	0.0006 904	0.0556 904	0.0116 891	0.0006 505	0.0556 505	0.0113 416	0.0006 309	0.0556 309
83	0.0117 502	0.0006 539	0.0556 539	0.0110 717	0.0006 158	0.0556 158	0.0107 387	0.0005 970	0.0555 970
84	0.0111 376	0.0006 195	0.0556 195	0.0104 870	0.0005 829	0.0555 829	0.0101 678	0.0005 650	0.0555 650
85	0.0105 570	0.0005 868	0.0555 868	0.0099 332	0.0005 518	0.0555 518	0.0096 273	0.0005 346	0.0555 346
86	0.0100 066	0.0005 559	0.0555 559	0.0094 086	0.0005 224	0.0555 224	0.0091 155	0.0005 060	0.0555 060
87	0.0094 850	0.0005 267	0.0555 267	0.0089 117	0.0004 946	0.0554 946	0.0086 309	0.0004 788	0.0554 788
88	0.0089 905	0.0004 990	0.0554 990	0.0084 411	0.0004 682	0.0554 682	0.0081 721	0.0004 532	0.0554 532
89	0.0085 218	0.0004 727	0.0554 727	0.0079 953	0.0004 433	0.0554 433	0.0077 377	0.0004 289	0.0554 289
90	0.0080 775	0.0004 479	0.0554 479	0.0075 730	0.0004 197	0.0554 197	0.0073 264	0.0004 059	0.0554 059
91	0.0076 564	0.0004 244	0.0554 244	0.0071 731	0.0003 974	0.0553 974	0.0069 369	0.0003 842	0.0553 842
92	0.0072 573	0.0004 021	0.0554 021	0.0067 943	0.0003 762	0.0553 762	0.0065 681	0.0003 636	0.0553 636
93	0.0068 789	0.0003 810	0.0553 810	0.0064 355	0.0003 562	0.0553 562	0.0062 190	0.0003 442	0.0553 442
94	0.0065 203	0.0003 610	0.0553 610	0.0060 956	0.0003 373	0.0553 373	0.0058 884	0.0003 258	0.0553 258
95	0.0061 804	0.0003 420	0.0553 420	0.0057 737	0.0003 194	0.0553 194	0.0055 753	0 0003 084	0.0553 084
96	0.0058 582	0.0003 241	0.0553 241	0.0054 688	0.0003 024	0.0553 024	0.0052 789	0.0002 919	0.0552 919
97	0.0055 528	0.0003 071	0.0553 071	0.0051 799	0.0002 864	0.0552 864	0.0049 983	0.0002 763	0.0552 763
98	0.0052 633	0.0002 910	0.0552 910	0.0049 064	0.0002 712	0.0552 712	0.0047 326	0.0002 615	0.0552 615
99	0.0049 889	0.0002 758	0.0552 758	0.0046 473	0.0002 568	0.0552 568	0.0044 810	0.0002 476	0.0552 476
100	0.0047 288	0.0002 613	0.0552 613	0.0044 018	0.0002 432	0.0552 432	0.0042 428	0.0002 343	0.0552 343
∴	Ratio of Perpetual Ann.		0.0550 000	- - - - - - - - - -		0.0550 000	- - - - - - - - - -		0.0550 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0575.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02875.			RATIO *of* INTEREST: *QUARTERLY*, 0.014375.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
$\frac{1}{4}$	....	....	....	....	....	....	1.0143 750	0.2500 000	0.2464 57
$\frac{1}{2}$	....	....	....	1.0287 500	0.5000 000	0.4860 27	1.0289 566	0.5035 938	0.4894 22
$\frac{3}{4}$	....	....	....	....	....	....	1.0437 479	0.7608 329	0.7289 43
1	1.0575 000	1.0000 000	0.9456 27	1.0583 265	1.0143 750	0.9584 71	1.0587 518	1.0217 699	0.9650 70
$\frac{1}{4}$	....	....	....	....	....	....	1.0739 713	1.2864 578	1.1978 51
$\frac{1}{2}$	....	....	....	1.0887 535	1.5435 383	1.4177 11	1 0894 097	1.5549 507	1.4273 33
$\frac{3}{4}$	....	....	....	....	....	....	1.1050 699	1.8273 031	1 6535 63
2	1.1183 063	2.0575 000	1.8398 36	1.1200 551	2.0879 150	1.8641 18	1.1209 553	2.1035 706	1.8765 87
$\frac{1}{4}$	....	....	....	....	....	....	1.1370 690	2.3838 094	2.0964 51
$\frac{1}{2}$	....	....	....	1.1522 567	2.6479 426	2.2980 49	1.1534 144	2.6680 766	2.3131 99
$\frac{3}{4}$	....	....	....	....	....	....	1.1699 947	2.9564 302	2.5268 75
3	1.1826 089	3.1758 063	2.6854 24	1.1853 841	3.2240 709	2.7198 53	1.1868 134	3.2489 289	2.7375 23
$\frac{1}{4}$	....	....	....	....	....	....	1.2038 739	3.5456 323	2.9451 86
$\frac{1}{2}$	....	....	....	1.2194 639	3.8167 630	3.1298 70	1.2211 795	3.8466 007	3.1499 05
$\frac{3}{4}$	....	....	....	....	....	....	1.2387 340	4.1518 956	3.3517 25
4	1.2506 089	4.3584 151	3.4850 35	1.2545 235	4.4264 949	3.5284 27	1.2565 408	4.4615 791	3.5506 84
$\frac{1}{4}$	....	....	....	....	....	....	1.2746 036	4.7757 143	3.7468 23
$\frac{1}{2}$	....	....	....	1.2905 910	5.0537 566	3.9158 47	1.2929 260	5.0943 652	3.9401 83
$\frac{3}{4}$	....	....	....	....	....	....	1.3115 118	5.4175 967	4.1308 03
5	1.3225 189	5.6090 240	4.2411 68	1.3276 955	5.6990 522	4.2924 39	1.3303 648	5.7454 747	4.3187 21
$\frac{1}{4}$	....	....	....	....	....	....	1.3494 888	6.0780 659	4.5039 76
$\frac{1}{2}$	....	....	....	1.3658 667	6.3628 999	4.6585 07	1.3688 877	6.4154 381	4.6866 06
$\frac{3}{4}$	....	....	....	....	....	....	1.3885 654	6.7576 600	4.8666 48
6	1.3985 637	6.9315 429	4.9561 87	1.4051 354	7.0458 333	5.0143 45	1.4085 261	7.1048 014	5.0441 39
$\frac{1}{4}$	....	....	....	....	....	....	1.4287 736	7.4569 329	5.2191 14
$\frac{1}{2}$	....	....	....	1.4455 331	7.7484 010	5.3602 38	1.4493 123	7.8141 263	5.3916 10
$\frac{3}{4}$	....	....	....	....	....	....	1.4701 461	8.1764 544	5.5616 61
7	1.4789 811	8.3301 066	5.6323 28	1.4870 921	8.4711 675	5.6964 64	1.4912 795	8.5439 909	5.7293 02
$\frac{1}{4}$	....	....	....	....	....	....	1.5127 166	8.9168 108	5.8945 68
$\frac{1}{2}$	....	....	....	1.5298 460	9.2147 136	6.0232 95	1.5344 619	9.2949 899	6.0574 91
$\frac{3}{4}$	....	....	....	....	....	....	1.5565 198	9.6786 054	6.2181 06
8	1.5640 225	9.8090 877	6.2717 05	1.5738 291	9.9796 366	6.3409 91	1.5788 948	10.067 735	6.3764 45
$\frac{1}{4}$	....	....	....	....	....	....	1.6015 914	10.462 459	6.5325 39
$\frac{1}{2}$	....	....	....	1.6190 767	10.766 551	6.6498 09	1.6246 143	10.862 857	6.6864 22
$\frac{3}{4}$	....	....	....	....	....	....	1.6479 681	11.269 010	6.8381 24
9	1.6539 538	11.373 110	6.8763 17	1.6656 251	11.576 089	6.9499 97	1.6716 576	11.681 002	6.9876 76
$\frac{1}{4}$	....	....	....	....	....	....	1.6956 877	12.098 917	7.1351 09
$\frac{1}{2}$	....	....	....	1.7135 119	12.408 902	7.2417 95	1.7200 632	12.522 839	7.2804 53
$\frac{3}{4}$	....	....	....	....	....	....	1.7447 891	12.952 855	7.4237 36
10	1.7490 562	13.027 064	7.4480 54	1.7627 753	13.265 658	7.5254 39	1.7698 705	13.389 052	7.5649 90
$\frac{1}{4}$	....	....	....	....	....	....	1.7953 124	13.831 520	7.7042 41
$\frac{1}{2}$	....	....	....	1.8134 551	14.147 046	7.8011 56	1.8211 200	14.280 348	7.8415 19
$\frac{3}{4}$	....	....	....	....	....	....	1.8472 986	14.735 628	7.9768 52
11	1.8496 269	14.776 120	7.9887 03	1.8655 920	15.053 773	8.0691 67	1.8738 535	15.197 452	8.1102 67
$\frac{1}{4}$	....	....	....	....	....	....	1.9007 901	15.665 916	8.2417 91
$\frac{1}{2}$	....	....	....	1.9192 277	15.986 569	8.3296 88	1.9281 140	16.141 113	8.3714 52
$\frac{3}{4}$	....	....	....	....	....	....	1.9558 306	16.623 142	8.4992 74
12	1.9559 805	16.625 747	8.4999 56	1.9744 055	16.946 183	8.5829 29	1.9839 457	17.112 099	8.6252 86
$\frac{1}{4}$	....	....	....	....	....	....	2.0124 649	17.608 086	8.7495 12
$\frac{1}{2}$	....	....	....	2.0311 697	17.933 386	8.8290 93	2.0413 941	18.111 202	8.8719 77
$\frac{3}{4}$	....	....	....	....	....	....	2.0707 392	18.621 551	8.9927 07
13	2.0684 493	18.581 728	8.9834 10	2.0895 658	18.948 971	9.0683 77	2.1005 060	19.139 235	9.1117 26
$\frac{1}{4}$	....	....	....	....	....	....	2.1307 008	19.664 362	9.2290 58
$\frac{1}{2}$	....	....	....	2.1496 408	19.993 754	9.3009 74	2.1613 296	20.197 037	9.3447 28
$\frac{3}{4}$	....	....	....	....	....	....	2.1923 987	20.737 369	9.4587 58
14	2.1873 852	20.650 177	9.4405 77	2.2114 430	21.068 574	9.5270 71	2.2239 145	21.285 469	9.5711 72
$\frac{1}{4}$	....	....	....	....	....	....	2.2558 832	21.841 448	9.6819 94
$\frac{1}{2}$	....	....	....	2.2750 220	22.174 295	9.7468 49	2.2883 116	22.405 419	9.7912 45
$\frac{3}{4}$	....	....	....	....	....	....	2.3212 060	22.977 496	9.8989 47
15	2.3131 598	22.837 562	9.8728 86	2.3404 289	23.311 806	9.9604 85	2.3545 734	23.557 798	10.005 12
$\frac{1}{4}$	....	....	....	....	....	....	2.3884 204	24.146 441	10.109 80
$\frac{1}{2}$	....	....	....	2.4077 162	24.482 021	10.168 15	2.4227 539	24.743 546	10.212 98
$\frac{3}{4}$	....	....	....	....	....	....	2.4575 810	25.349 235	10.314 71
16	2.4461 665	25.150 722	10.281 69	2.4769 380	25.685 879	10.370 01	2.4929 087	25.963 630	10.414 99
17	2.5868 211	27.596 888	10.668 26	2.6214 093	28.198 423	10.756 97	2.6393 715	28.510 809	10.802 12
18	2.7355 633	30.183 710	11.033 82	2.7743 071	30 857 515	11.122 60	2.7944 393	31.207 640	11.167 76
19	2.8928 582	32.919 273	11.379 50	2.9361 229	33.671 703	11.468 08	2.9586 175	34.062 913	11.513 12
20	3.0591 975	35.812 131	11.706 38	3.1073 769	36.650 033	11.794 52	3.1324 415	37.085 940	11.839 31
21	3.2351 014	38.871 329	12.015 49	3.2886 195	39.802 078	12.102 97	3.3164 780	40.286 574	12.147 40
22	3.4211 197	42.106 430	12.307 79	3.4804 334	43.137 971	12.394 43	3.5113 270	43.675 251	12.438 39
23	3.6178 341	45.527 550	12.584 20	3.6834 351	46.668 436	12.669 81	3.7176 236	47.263 020	12.713 23
24	3.8258 596	49.145 384	12 845 58	3.8982 772	50.404 820	12.930 03	3.9360 406	51.061 575	12.972 83
25	4.0458 465	52.971 243	13.092 75	4.1256 503	54.359 135	13.175 90	4.1672 899	55.083 303	13.218 02

Years.	RATIO of INTEREST: ANNUALLY, 0.0575.			RATIO of INTEREST: HALF-YEARLY, 0.02875.			RATIO of INTEREST: QUARTERLY, 0.014375.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
½	....	....	....	....	....	....	0.9858 287	4.0000 000	4.0575 000
1	0.9456 265	1.0000 000	1.0575 000	0.9720 535	2.0000 000	2.0575 000	0.9718 583	1.9857 276	2.0432 276
				0.9448 879	0.9858 287	1.0433 287	0.9580 858	1.3143 409	1.3718 409
							0.9445 083	0.9786 939	1.0361 939
1½	....	....	....	....	....	....	0.9311 235	0.7773 283	0.8348 283
2	0.8942 094	0.4860 268	0.5435 268	0.9184 816	0.6478 621	0.7053 621	0.9179 282	0.6431 072	0.7006 072
				0.8928 132	0.4789 467	0.5364 467	0.9049 201	0.5472 546	0.6047 546
							0.8920 963	0.4753 821	0.5328 821
2½	....	....	....	....	....	....	0.8794 541	0.4194 966	0.4769 966
3	0.8455 881	0.3148 807	0.3723 807	0.8678 621	0.3776 517	0.4351 517	0.8669 911	0.3748 018	0.4323 018
				0.8436 084	0.3101 669	0.3676 669	0.8547 047	0.3382 458	0.3957 458
							0.8425 924	0.3077 938	0.3652 938
3½	....	....	....	....	....	....	0.8306 518	0.2820 372	0.3395 372
4	0.7996 106	0.2294 412	0.2869 412	0.8200 325	0.2620 021	0.3195 021	0.8188 804	0.2599 698	0.3174 698
				0.7971 154	0.2259 123	0.2834 123	0.8072 758	0.2408 538	0.2983 538
							0.7958 357	0.2241 359	0.2816 359
4½	....	....	....	....	....	....	0.7845 577	0.2093 928	0.2668 928
5	0.7561 329	0.1782 841	0.2357 841	0.7748 388	0.1978 726	0.2553 726	0.7734 395	0.1962 953	0.2537 953
				0.7531 848	0.1754 678	0.2329 678	0.7624 783	0.1845 847	0.2420 847
							0.7516 735	0.1740 500	0.2315 500
5½	....	....	....	....	....	....	0.7410 213	0.1645 260	0.2220 260
6	0.7150 192	0.1442 680	0.2017 680	0.7321 359	0.1571 610	0.2146 610	0.7305 201	0.1558 740	0.2133 740
				0.7116 751	0.1419 279	0.1994 279	0.7201 677	0.1479 820	0.2054 820
							0.7099 620	0.1407 499	0.1982 499
6½	....	....	....	....	....	....	0.6999 009	0.1341 034	0.1916 034
7	0.6761 412	0.1200 465	0.1775 465	0.6917 863	0.1290 589	0.1865 589	0.6899 824	0.1279 734	0.1854 734
				0.6724 533	0.1180 475	0.1755 475	0.6802 045	0.1223 024	0.1798 024
							0.6705 651	0.1170 413	0.1745 413
7½	....	....	....	....	....	....	0.6610 623	0.1121 477	0.1696 477
8	0.6393 770	0.1019 463	0.1594 463	0.6536 605	0.1085 221	0.1660 221	0.6516 942	0.1075 848	0.1650 848
				0.6353 930	0.1002 040	0.1577 040	0.6424 589	0.1033 207	0.1608 207
							0.6333 544	0.0993 272	0.1568 272
8½	....	....	....	....	....	....	0.6243 790	0.0955 798	0.1530 798
9	0.6046 118	0.0879 267	0.1454 267	0.6176 360	0.0928 803	0.1503 803	0.6155 307	0.0920 568	0.1495 568
				0.6003 752	0.0863 850	0.1438 850	0.6068 079	0.0887 389	0.1462 389
							0.5982 086	0.0856 091	0.1431 091
9½	....	....	....	....	....	....	0.5897 312	0.0826 520	0.1401 520
10	0.5717 369	0.0767 633	0.1342 633	0.5835 967	0.0805 873	0.1380 873	0.5813 740	0.0798 541	0.1373 541
				0.5672 873	0.0753 826	0.1328 826	0.5731 352	0.0772 031	0.1347 031
							0.5650 131	0.0747 437	0.1322 437
10½	....	....	....	....	....	....	0.5570 061	0.0722 987	0.1297 987
11	0.5406 496	0.0676 768	0.1251 768	0.5514 335	0.0706 861	0.1281 861	0.5491 126	0.0700 263	0.1275 263
				0.5360 229	0.0664 285	0.1239 285	0.5413 310	0.0678 627	0.1253 627
							0.5336 596	0.0658 005	0.1233 005
11½	....	....	....	....	....	....	0.5260 970	0.0638 328	0.1213 328
12	0.5112 526	0.0601 477	0.1176 477	0.5210 429	0.0625 525	0.1200 525	0.5186 415	0.0619 536	0.1194 536
				0.5064 816	0.0590 103	0.1165 103	0.5112 917	0.0601 571	0.1176 571
							0.5040 461	0.0584 382	0.1159 382
12½	....	....	....	....	....	....	0.4969 031	0.0567 921	0.1142 921
13	0.4834 539	0.0538 163	0.1113 163	0.4923 272	0.0557 619	0.1132 619	0.4898 613	0.0552 144	0.1127 144
				0.4785 683	0.0527 733	0.1102 733	0.4829 193	0.0537 012	0.1112 012
							0.4760 757	0.0522 487	0.1097 487
13½	....	....	....	....	....	....	0.4693 291	0.0508 534	0.1083 534
14	0.4571 669	0.0484 257	0.1059 257	0.4651 940	0.0500 156	0.1075 156	0.4626 782	0.0495 122	0.1070 122
				0.4521 934	0.0474 641	0.1049 641	0.4561 214	0.0482 223	0.1057 223
							0.4496 576	0.0469 804	0.1044 804
14½	....	....	....	....	....	....	0.4432 854	0.0457 845	0.1032 845
15	0.4323 091	0.0437 875	0.1012 875	0.4395 562	0.0450 973	0.1025 973	0.4370 034	0.0446 320	0.1021 320
				0.4272 721	0.0428 967	0.1003 967	0.4308 105	0.0435 209	0.1010 209
							0.4247 054	0.0424 488	0.0999 488
15½	....	....	....	....	....	....	0.4186 868	0.0414 140	0.0989 140
16	0.4088 029	0.0397 603	0.0972 603	0.4153 313	0.0408 463	0.0983 463	0.4127 534	0.0404 146	0.0979 146
				0.4037 243	0.0389 319	0.0964 319	0.4069 042	0.0394 489	0.0969 489
							0.4011 378	0.0385 154	0.0960 154
17	0.3865 749	0.0362 360	0.0937 360	0.3814 742	0.0354 630	0.0929 630	0.3788 781	0.0350 744	0.0925 744
18	0.3655 554	0.0331 305	0.0906 305	0.3604 504	0.0324 070	0.0899 070	0.3578 535	0.0320 434	0.0895 434
19	0.3456 789	0.0303 773	0.0878 773	0.3405 852	0.0296 985	0.0871 985	0.3379 957	0.0293 574	0.0868 574
20	0.3268 831	0.0279 235	0.0854 235	0.3218 149	0.0272 851	0.0847 851	0.3192 398	0.0269 644	0.0844 644
21	0.3091 093	0.0257 259	0.0832 259	0.3040 790	0.0251 243	0.0826 243	0.3015 247	0.0248 222	0.0823 222
22	0.2923 019	0.0237 493	0.0812 493	0.2873 205	0.0231 814	0.0806 814	0.2847 926	0.0228 963	0.0803 963
23	0.2764 085	0.0219 647	0.0794 647	0.2714 858	0.0214 278	0.0789 278	0.2689 890	0.0211 582	0.0786 582
24	0.2613 792	0.0203 478	0.0778 478	0.2565 236	0.0198 394	0.0773 394	0.2540 624	0.0195 842	0.0770 842
25	0.2471 671	0.0188 782	0.0763 782	0.2423 860	0.0183 962	0.0758 962	0.2399 641	0.0181 543	0.0756 543

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.0575.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.02875.			RATIO *of* INTEREST: *QUARTERLY*, 0.014375.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	4.2784 827	57.017 090	13.326 47	4.3662 853	58.544 092	13.408 22	4.4121 256	59.341 315	13.449 60
27	4.5244 954	61.295 573	13.547 49	4.6209 557	62.973 142	13.627 73	4.6713 458	63.849 492	13.668 33
28	4.7846 539	65.820 068	13.756 49	4.8904 801	67.660 524	13.835 15	4.9457 956	68.622 532	13.874 92
29	5.0597 715	70.604 722	13.954 13	5.1757 250	72.621 305	14.031 14	5.2363 698	73.675 997	14.070 05
30	5.3507 084	75.664 493	14.141 02	5.4776 073	77.871 431	14.216 32	5.5440 158	79.026 362	14.254 35
31	5.6583 741	81.015 202	14.317 75	5.7970 973	83.427 779	14.391 30	5.8697 365	84.691 070	14.428 43
32	5.9837 306	86.673 576	14.484 87	6.1352 221	89.308 210	14.556 64	6.2145 939	90 688 590	14.592 84
33	6.3277 951	92.657 307	14.642 91	6.4930 685	95.531 626	14.712 86	6.5797 123	97.038 475	14.748 13
34	6.6916 433	98.985 102	14.792 35	6.8717 868	102.11 803	14.860 48	6.9662 821	103.76 143	14.894 81
35	7.0764 128	105.67 674	14.933 66	7.2725 945	109.08 860	14.999 96	7.3755 635	110.87 936	15.033 34
36	7.4833 066	112.75 316	15.067 29	7.6967 800	116.46 574	15.131 75	7.8088 909	118.41 549	15.164 19
37	7.9135 967	120.23 646	15.193 66	8.1457 067	124.27 316	15.256 28	8.2676 770	126.39 438	15.287 78
38	8.3686 285	128.15 006	15.313 15	8.6208 178	132.53 596	15.373 94	8.7534 176	134.84 205	15.404 50
39	8.8498 247	136.51 869	15.426 15	9.1236 404	141.28 070	15.485 12	9.2676 964	143.78 602	15.514 75
40	9.3586 896	145.36 851	15.533 00	9.6557 910	150.53 550	15.590 18	9.8121 900	153.25 548	15.618 89
41	9.8968 142	154.72 720	15.634 04	10.218 980	160.33 009	15.689 44	10.388 673	163.28 128	15.717 24
42	10.465 881	164.62 402	15.729 59	10.815 018	170.69 597	15.783 23	10.999 026	173.89 611	15.810 14
43	11.067 669	175.08 990	15.819 94	11.445 821	181.66 645	15.871 86	11.645 239	185.13 459	15.897 88
44	11.704 060	186.15 757	15.905 38	12.113 416	193.27 681	15.955 60	12.329 417	197.03 334	15.980 75
45	12.377 044	197.86 163	15.986 18	12.819 950	205.56 435	16.034 72	13.053 792	209.63 117	16.059 02
46	13.088 724	210.23 867	16.062 58	13.567 694	218.56 859	16.109 48	13.820 725	222.96 914	16.132 95
47	13.841 325	223.32 740	16.134 83	14.359 051	232.33 132	16.180 13	14.632 717	237.09 074	16.202 78
48	14.637 201	237.16 872	16.203 15	15.196 565	246.89 678	16.246 89	15.492 416	252.04 201	16.268 73
49	15.478 841	251.80 592	16.267 75	16.082 928	262.31 180	16.309 95	16.402 622	267.87 169	16.331 02
50	16.368 874	267.28 476	16.328 84	17.020 990	278.62 592	16.369 55	17.366 305	284.63 140	16.389 86
51	17.310 084	283.65 364	16.386 61	18.013 766	295.89 158	16.425 86	18.386 607	302.37 577	16.445 44
52	18.305 414	300.96 372	16.441 24	19.064 447	314.16 430	16.479 07	19.466 852	321.16 265	16.497 92
53	19.357 975	319.26 913	16.492 90	20.176 411	333.50 280	16.529 34	20.610 564	341.05 329	16.547 50
54	20.471 059	338.62 711	19.541 75	21.353 231	353.96 924	16.576 85	21.821 471	362.11 254	16.594 32
55	21.648 145	359.09 817	16.587 94	22.598 692	375.62 943	16.621 73	23.103 521	384.40 907	16.638 55
56	22.892 913	380.74 631	16.631 62	23.916 796	398.55 298	16.664 14	24.460 894	408.01 555	16.680 32
57	24.209 256	403.63 923	16.672 93	25.311 781	422.81 358	16.704 22	25.898 015	433.00 895	16.719 77
58	25.601 288	427.84 848	16.711 99	26.788 130	448.48 921	16.742 09	27.419 569	459.47 076	16.757 04
59	27.073 362	453.44 977	16.748 93	28.350 589	475.66 242	16.777 87	29.030 517	487.48 725	16.792 23
60	28.630 080	480.52 313	16.783 86	30.004 182	504.42 055	16.811 68	30.736 111	517.14 976	16.825 48
61	30.276 310	509.15 321	16.816 88	31.754 222	534.85 604	16.843 62	32.541 912	548.55 500	16.856 88
62	32.017 197	539.42 952	16.848 12	33.606 337	567.06 673	16.873 80	34.453 807	581.80 534	16.886 53
63	33.858 186	571.44 672	16.877 65	35.566 479	601.15 616	16.902 32	36.478 029	617.00 920	16.914 54
64	35.805 032	605.30 491	16.905 58	37.640 950	637.23 391	16.929 27	38.621 178	654.28 136	16.941 00
65	37.863 821	641.10 994	16.931 99	39.836 417	675.41 595	16.954 74	40.890 240	693.74 331	16.965 99
66	40.040 991	678.97 376	16.956 97	42.159 938	715.82 501	16.978 80	43.292 614	735.52 373	16.989 59
67	42.343 348	719.01 475	16.980 58	44.618 982	758.59 100	17.001 53	45.836 132	779.75 882	17.011 88
68	44.778 091	761.35 810	17.002 92	47.221 454	803.85 138	17.023 01	48.529 086	826.59 280	17.032 94
69	47.352 831	806.13 619	17.024 03	49.975 719	851.75 164	17.043 31	51.380 255	876.17 836	17.052 82
70	50.075 619	853.48 902	17.044 00	52.890 631	902.44 576	17.062 49	54.398 936	928.67 715	17.071 60
71	52.954 967	903.56 464	17.062 89	55.975 560	956.09 670	17.080 61	57.594 970	984.26 035	17.089 34
72	55.999 877	956.51 961	17.080 74	59 240 422	1012.8 769	17.097 73	60.978 776	1043.1 092	17.106 10
73	59.219 870	1012.5 195	17.097 63	62.695 712	1072.9 689	17.113 91	64.561 387	1105.4 154	17.121 93
74	62.625 013	1071.7 394	17.113 60	66.352 538	1136.5 659	17.129 20	68.354 483	1171.3 823	17.136 88
75	66.225 951	1134.3 644	17.128 70	70.222 653	1203.8 722	17.143 64	72.370 430	1241.2 249	17.151 00
76	70.033 943	1200.5 903	17.142 98	74.318 499	1275.1 043	17.157 29	76.622 320	1315.1 708	17.164 32
77	74.060 895	1270.6 243	17.156 48	78.653 242	1350.4 912	17.170 19	81 124 017	1393.4 612	17.176 92
78	78.319 396	1344.6 852	17.169 25	83.240 815	1430.2 750	17.182 38	85.890 197	1476.3 512	17.188 82
79	82.822 762	1423.0 046	17.181 32	88.095 965	1514.7 124	17.193 89	90.936 308	1564.1 113	17.200 06
80	87.585 070	1505.8 273	17.192 74	93.234 300	1604.0 748	17.204 77	96.279 072	1657.0 273	17.210 67
81	92.621 212	1593.4 124	17.203 54	98.672 336	1698.6 493	17.215 05	101.93 564	1755.4 024	17.220 69
82	97.946 932	1686.0 336	17.213 75	104.42 755	1798.7 401	17.224 77	107.92 454	1859.5 572	17.230 16
83	103.57 888	1783.9 805	17.223 40	110.51 845	1904.6 688	17.233 94	114.26 529	1969.8 312	17.239 10
84	109.53 467	1887.5 594	17.232 53	116.96 462	2016.7 759	17.242 62	120.97 858	2086.5 840	17.247 55
85	115.83 291	1997.0 941	17.241 16	123.78 676	2135.4 219	17.250 81	128.08 629	2210.1 963	17.255 53
86	122 49 330	2112.9 270	17.249 33	131.00 682	2260.9 881	17.258 55	135.61 158	2341.0 710	17.263 06
87	129.53 667	2235.4 203	17.257 05	138.64 799	2393.8 782	17.265 87	143.57 900	2479.6 348	17.270 18
88	136.98 502	2364.9 570	17.264 35	146.73 485	2534.5 192	17.272 78	152.01 452	2626.3 395	17.276 90
89	144.86 166	2501.9 420	17.271 25	155.29 339	2683.3 634	17.279 31	160.94 565	2781.6 634	17.283 25
90	153.19 121	2646.8 036	17.277 78	164.35 112	2840.8 891	17.285 49	170.40 149	2946.1 128	17.289 25
91	161.99 970	2799.9 948	17.283 95	173.93 716	3007.6 028	17.291 32	180.41 288	3120.2 239	17.294 91
92	171.31 469	2961.9 946	17.289 79	184.08 232	3184.0 403	17.296 83	191.01 245	3304.5 644	17.300 26
93	181.16 528	3133.3 092	17.295 31	194.81 921	3370.7 688	17.302 04	202.23 477	3499.7 351	17.305 31
94	191.58 228	3314.4 745	17.300 53	206.18 234	3568.3 885	17 306 96	214.11 642	3706.3 725	17.310 08
95	202.59 827	3506.0 568	17.305 46	218.20 825	3777.5 347	17.311 61	226.69 614	3925.1 503	17.314 59
96	214.24 767	3708.6 551	17.310 13	230.93 558	3998.8 797	17.316 00	240.01 494	4156.7 815	17.318 84
97	226.56 691	3922.9 027	17.314 54	244.40 526	4233.1 350	17.320 15	254.11 624	4402.0 216	17.322 87
98	239.59 450	4149.4 696	17.318 72	258.66 058	4481.0 536	17.324 07	269.04 602	4661.6 699	17.326 66
99	253.37 119	4389.0 641	17.322 66	273.74 737	4743.4 324	17.327 77	284.85 295	4936.5 730	17.330 25
100	267.94 003	4642.4 353	17.326 40	289.71 411	5021.1 149	17.331 27	301.58 856	5227.6 272	17.333 64
	Value of Perpetual Annu.		17.391 30	- - - - - - - - - -		17.391 30	- - - - - - - - - -		17.391 30

Years.	RATIO of INTEREST: ANNUALLY, 0.0575.			RATIO of INTEREST: HALF-YEARLY, 0.02875.			RATIO of INTEREST: QUARTERLY, 0.014375.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.2337 277	0.0175 386	0.0750 386	0.2290 276	0.0170 811	0.0745 811	0.2266 481	0.0168 517	0.0743 517
27	0.2210 191	0.0163 144	0.0738 144	0.2164 055	0.0158 798	0.0733 798	0.2140 711	0.0156 618	0.0731 618
28	0.2090 015	0.0151 929	0.0726 929	0.2044 789	0.0147 797	0.0722 797	0.2021 919	0.0145 725	0.0720 725
29	0.1976 374	0.0141 634	0.0716 634	0.1932 096	0.0137 701	0.0712 701	0.1909 720	0.0135 729	0.0710 729
30	0.1868 911	0.0132 162	0.0707 162	0.1825 615	0.0128 417	0.0703 417	0.1803 746	0.0126 540	0.0701 540
31	0.1767 292	0.0123 434	0.0698 434	0.1725 001	0.0119 864	0 0694 864	0.1703 654	0.0118 076	0.0693 076
32	0.1671 198	0.0115 375	0.0690 375	0.1629 933	0.0111 972	0.0686 972	0.1609 116	0.0110 267	0.0685 267
33	0.1580 329	0.0107 925	0.0682 925	0.1540 104	0.0104 677	0.0679 677	0.1519 823	0.0103 052	0.0678 052
34	0.1494 401	0 0101 025	0.0676 025	0.1455 226	0.0097 926	0.0672 926	0.1435 486	0.0096 375	0.0671 375
35	0.1413 145	0.0094 628	0.0669 628	0.1375 025	0.0091 669	0.0666 669	0.1355 828	0.0090 188	0.0665 188
36	0.1336 308	0.0088 689	0.0663 689	0.1299 245	0.0085 862	0.0650 862	0.1280 592	0.0084 448	0.0659 448
37	0.1263 648	0.0083 169	0.0658 169	0.1227 641	0.0080 468	0.0655 468	0.1209 530	0.0079 117	0.0654 117
38	0.1194 939	0.0078 034	0.0653 034	0.1159 983	0.0075 451	0.0650 451	0.1142 411	0.0074 161	0.0649 161
39	0.1129 966	0.0073 250	0.0648 250	0.1096 054	0.0070 781	0.0645 781	0.1079 017	0.0069 548	0.0644 548
40	0.1068 526	0.0068 791	0.0643 791	0.1035 648	0.0066 430	0.0641 430	0.1019 140	0.0065 251	0.0640 251
41	0.1010 426	0.0064 630	0.0639 630	0.0978 571	0.0062 371	0.0637 371	0.0962 587	0.0061 244	0.0636 244
42	0.0955 486	0.0060 744	0.0635 744	0.0924 640	0.0058 584	0.0633 584	0.0909 171	0.0057 506	0.0632 506
43	0.0903 533	0.0057 114	0.0632 114	0.0873 681	0.0055 046	0.0630 046	0.0858 720	0.0054 015	0.0629 015
44	0.0854 404	0.0053 718	0.0628 718	0.0825 531	0.0051 739	0.0626 739	0.0811 068	0.0050 753	0.0625 753
45	0.0807 947	0.0050 540	0.0625 540	0.0780 034	0.0048 647	0.0623 647	0.0766 061	0.0047 703	0.0622 703
46	0.0764 016	0.0047 565	0.0622 565	0.0737 045	0.0045 752	0.0620 752	0.0723 551	0.0044 849	0.0619 849
47	0.0722 474	0.0044 777	0.0619 777	0.0696 425	0.0043 043	0.0618 043	0.0683 400	0.0042 178	0.0617 178
48	0.0683 191	0.0042 164	0.0617 164	0.0658 043	0.0040 503	0.0615 503	0.0645 477	0.0039 676	0.0614 676
49	0.0646 043	0.0039 713	0.0614 713	0.0621 777	0.0038 123	0.0613 123	0.0609 659	0.0037 331	0.0612 331
50	0.0610 916	0.0037 413	0.0612 413	0.0587 510	0.0035 890	0.0610 890	0.0575 828	0.0035 133	0.0610 133
51	0.0577 698	0.0035 254	0.0610 254	0.0555 131	0.0033 796	0.0608 796	0.0543 874	0.0033 071	0.0608 071
52	0.0546 286	0.0033 227	0.0608 227	0.0524 537	0.0031 830	0.0606 830	0.0513 694	0.0031 137	0.0606 137
53	0.0516 583	0.0031 322	0.0606 322	0.0495 628	0.0029 985	0.0604 985	0.0485 188	0.0029 321	0.0604 321
54	0 0488 495	0.0029 531	0.0604 531	0.0468 313	0.0028 251	0.0603 251	0.0458 264	0.0027 616	0.0602 616
55	0.0461 933	0.0027 848	0.0602 848	0.0442 503	0.0026 622	0.0601 622	0.0432 834	0.0026 014	0.0601 014
56	0.0436 816	0.0026 264	0.0601 264	0.0418 116	0.0025 091	0.0600 091	0.0408 816	0.0024 509	0.0599 509
57	0.0413 065	0.0024 775	0.0599 775	0 0395 073	0.0023 651	0.0598 651	0.0386 130	0.0023 094	0.0598 094
58	0.0390 605	0.0023 373	0.0598 373	0.0373 300	0.0022 297	0.0597 297	0.0364 703	0.0021 764	0.0596 764
59	0.0369 367	0.0022 053	0.0597 053	0.0352 726	0.0021 023	0.0596 023	0.0344 465	0.0020 513	0.0595 513
60	0.0349 283	0.0020 811	0.0595 811	0.0333 287	0.0019 825	0.0594 825	0.0325 350	0.0019 337	0.0594 337
61	0.0330 291	0.0019 640	0.0594 640	0.0314 919	0.0018 697	0.0593 697	0.0307 296	0.0018 230	0.0593 230
62	0.0312 332	0.0018 538	0.0593 538	0.0297 563	0.0017 635	0.0592 635	0.0290 244	0.0017 188	0.0592 188
63	0.0295 350	0.0017 499	0.0592 499	0.0281 164	0.0016 635	0.0591 635	0.0274 138	0 0016 207	0.0591 207
64	0.0279 290	0.0016 521	0.0591 521	0.0265 668	0.0015 693	0.0590 693	0.0258 925	0.0015 284	0.0590 284
65	0.0264 104	0.0015 598	0.0590 598	0.0251 027	0.0014 806	0.0589 806	0.0244 557	0.0014 415	0.0589 415
66	0.0249 744	0.0014 728	0.0589 728	0.0237 192	0.0013 970	0.0588 970	0.0230 986	0.0013 596	0.0588 596
67	0.0236 165	0.0013 908	0.0588 908	0.0224 120	0.0013 182	0.0588 182	0.0218 169	0.0012 824	0.0587 824
68	0.0223 323	0.0013 134	0.0588 134	0.0211 768	0.0012 440	0.0587 440	0.0206 062	0.0012 098	0.0587 098
69	0.0211 181	0.0012 405	0.0587 405	0.0200 097	0.0011 741	0.0586 741	0.0194 627	0.0011 413	0.0586 413
70	0.0199 698	0.0011 717	0.0586 717	0.0189 069	0.0011 081	0.0586 081	0.0183 827	0.0010 768	0.0585 768
71	0.0188 840	0.0011 067	0.0586 067	0.0178 649	0.0010 459	0.0585 459	0.0173 626	0.0010 160	0.0585 160
72	0.0178 572	0.0010 455	0.0585 455	0.0168 804	0.0009 873	0.0584 873	0.0163 991	0.0009 587	0.0584 587
73	0.0168 862	0.0009 876	0.0584 876	0.0159 501	0.0009 320	0.0584 320	0.0154 891	0.0009 046	0.0584 046
74	0.0159 681	0.0009 331	0.0584 331	0.0150 710	0.0008 798	0.0583 798	0.0146 296	0.0008 537	0.0583 537
75	0.0150 998	0.0008 816	0.0583 816	0.0142 404	0.0008 307	0.0583 307	0.0138 178	0.0008 057	0.0583 057
76	0.0142 788	0.0008 329	0.0583 329	0.0134 556	0.0007 842	0.0582 842	0.0130 510	0.0007 604	0.0582 604
77	0.0135 024	0.0007 870	0.0582 870	0.0127 140	0.0007 405	0.0582 405	0.0123 268	0.0007 176	0.0582 176
78	0.0127 682	0.0007 437	0.0582 437	0.0120 133	0.0006 992	0.0581 992	0.0116 428	0.0006 773	0.0581 773
79	0.0120 740	0.0007 027	0.0582 027	0.0113 513	0.0006 602	0.0581 602	0.0109 967	0.0006 393	0.0581 393
80	0.0114 175	0.0006 641	0.0581 641	0.0107 257	0.0006 234	0.0581 234	0.0103 865	0.0006 035	0.0581 035
81	0.0107 967	0.0006 276	0.0581 276	0.0101 346	0.0005 887	0.0580 887	0.0098 101	0.0005 697	0.0580 697
82	0.0102 096	0.0005 931	0.0580 931	0.0095 760	0.0005 559	0.0580 559	0.0092 657	0.0005 378	0.0580 378
83	0.0096 545	0.0005 605	0.0580 605	0.0090 483	0.0005 250	0.0580 250	0.0087 516	0.0005 077	0.0580 077
84	0.0091 295	0.0005 298	0.0580 298	0.0085 496	0.0004 958	0.0579 958	0.0082 659	0.0004 793	0.0579 793
85	0.0086 331	0.0005 007	0.0580 007	0.0080 784	0.0004 683	0.0579 683	0.0078 072	0.0004 524	0.0579 524
86	0.0081 637	0.0004 733	0.0579 733	0.0076 332	0.0004 423	0.0579 423	0.0073 740	0.0004 272	0.0579 272
87	0.0077 198	0.0004 473	0.0579 473	0 0072 125	0.0004 177	0.0579 177	0.0069 648	0.0004 033	0.0579 033
88	0.0073 001	0.0004 228	0.0579 228	0.0068 150	0.0003 946	0.0578 946	0.0065 783	0.0003 808	0.0578 808
89	0.0069 031	0.0003 997	0.0578 997	0.0064 394	0.0003 727	0 0578 727	0.0062 133	0.0003 595	0.0578 595
90	0.0065 278	0.0003 778	0.0578 778	0.0060 845	0.0003 520	0.0578 520	0.0058 685	0.0003 394	0.0578 394
91	0.0061 729	0.0003 571	0.0578 571	0.0057 492	0.0003 325	0.0578 325	0.0055 428	0.0003 205	0.0578 205
92	0.0058 372	0.0003 376	0.0578 376	0.0054 324	0.0003 141	0.0578 141	0.0052 353	0.0003 026	0.0578 026
93	0.0055 198	0.0003 192	0.0578 192	0 0051 330	0.0002 967	0.0577 967	0.0049 447	0.0002 857	0.0577 857
94	0.0052 197	0.0003 017	0.0578 017	0.0048 501	0.0002 802	0.0577 802	0.0046 704	0.0002 698	0.0577 698
95	0.0049 359	0.0002 852	0.0577 852	0.0045 828	0.0002 647	0.0577 647	0.0044 112	0.0002 548	0.0577 548
96	0.0046 675	0.0002 696	0.0577 696	0.0043 302	0.0002 501	0.0577 501	0.0041 664	0.0002 406	0.0577 406
97	0.0044 137	0.0002 549	0.0577 549	0.0040 916	0.0002 362	0.0577 362	0.0039 352	0.0002 272	0.0577 272
98	0 0041 737	0.0002 410	0.0577 410	0.0038 661	0.0002 232	0.0577 232	0.0037 168	0.0002 145	0.0577 145
99	0.0039 468	0.0002 278	0.0577 278	0.0036 530	0.0002 108	0.0577 108	0.0035 106	0.0002 026	0.0577 026
100	0.0037 322	0.0002 154	0.0577 154	0.0034 517	0.0001 992	0.0576 992	0.0033 158	0.0001 913	0.0576 913
	Ratio of Perpetual Ann.		0.0575 000	- - - - - - - - - -		0.0575 000	- - - - - - - - - -		0.0575 000

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.06.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.03.			RATIO *of* INTEREST: *QUARTERLY*, 0.015.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
½	....	....	....	....	....	....	1.0150 000	0.2500 000	0.2463 05
	....	....	....	1.0300 000	0.5000 000	0.4854 37	1.0302 250	0.5037 500	0.4889 71
	....	....	....	....	....	....	1.0456 784	0.7613 063	0.7280 50
1	1.0600 000	1.0000 000	0.9433 96	1.0609 000	1.0150 000	0.9567 35	1.0613 636	1.0227 258	0.9635 96
½	....	....	....	....	....	....	1.0772 840	1.2880 667	1.1956 61
	....	....	....	1.0927 270	1.5454 500	1.4143 06	1.0934 433	1.5573 877	1.4242 97
	....	....	....	....	....	....	1.1098 449	1.8307 484	1.6495 53
2	1.1236 000	2.0600 000	1.8333 93	1.1255 088	2.0918 135	1.8585 49	1.1264 926	2.1032 098	1.8714 81
½	....	....	....	....	....	....	1.1433 900	2.3898 329	2.0901 29
	....	....	....	1.1592 741	2.6545 679	2.2898 54	1.1605 408	2.6756 804	2.3055 46
	....	....	....	....	....	....	1.1779 489	2.9658 156	2.5177 79
3	1.1910 160	3.1836 000	2.6730 12	1.1940 523	3.2342 049	2.7085 96	1.1956 182	3.2603 028	2.7268 76
½	....	....	....	....	....	....	1.2135 524	3.5592 074	2.9328 83
	....	....	....	1.2298 739	3.8312 311	3.1151 42	1.2317 557	3.8625 955	3.1358 45
	....	....	....	....	....	....	1.2502 321	4.1705 345	3.3358 08
4	1.2624 770	4.3746 160	3.4651 06	1.2667 701	4.4461 680	3.5098 46	1.2689 855	4.4830 924	3.5328 16
½	....	....	....	....	....	....	1.2880 203	4.8003 388	3.7269 12
	....	....	....	1.3047 732	5.0795 530	3.8930 55	1.3073 406	5.1223 437	3.9181 40
	....	....	....	....	....	....	1.3269 507	5.4491 790	4.1065 42
5	1.3382 256	5.6370 930	4.2123 64	1.3439 164	5.7319 397	4.2651 01	1.3468 550	5.7809 168	4.2921 60
½	....	....	....	....	....	....	1.3670 578	6.1176 305	4.4750 34
	....	....	....	1.3842 339	6.4038 983	4.6263 12	1.3875 637	6.4593 950	4.6552 06
	....	....	....	....	....	....	1.4083 772	6.8062 860	4.8327 15
6	1.4185 191	6.9753 185	4.9173 24	1.4257 609	7.0960 148	4.9770 02	1.4295 028	7.1583 800	5.0076 01
½	....	....	....	....	....	....	1.4509 454	7.5157 560	5.1799 03
	....	....	....	1.4685 337	7.8088 950	5.3174 78	1.4727 095	7.8784 920	5.3496 58
	....	....	....	....	....	....	1.4948 002	8.2466 695	5.5169 04
7	1.5036 303	8.3938 376	5.5823 82	1.5125 897	8.5431 620	5.6480 37	1.5172 222	8.6203 695	5.6816 79
½	....	....	....	....	....	....	1.5399 805	8.9996 750	5.8440 19
	....	....	....	1.5579 674	9.2994 570	5.9689 68	1.5630 802	9.3846 705	6.0039 59
	....	....	....	....	....	....	1.5865 264	9.7754 405	6.1615 36
8	1.5938 481	9.8974 679	6.2097 94	1.6047 064	10.078 441	6.2895 51	1.6103 243	10.172 072	6.3157 85
½	....	....	....	....	....	....	1.6344 792	10.574 653	6.4697 38
	....	....	....	1.6528 476	10.880 794	6.5830 59	1.6589 964	10.983 273	6.6204 32
	....	....	....	....	....	....	1.6838 813	11.398 022	6.7688 98
9	1.6894 790	11.491 316	6.8016 91	1.7024 331	11.707 218	6.8767 57	1.7091 395	11.818 992	6.9151 71
½	....	....	....	....	....	....	1.7347 767	12.246 278	7.0592 82
	....	....	....	1.7535 061	12.558 434	7.1619 00	1.7607 983	12.679 971	7.2012 63
	....	....	....	....	....	....	1.7872 101	13.120 168	7.3411 46
10	1.7908 477	13.180 795	7.3600 86	1.8061 112	13.435 187	7.4387 37	1.8140 184	13.566 973	7.4789 61
½	....	....	....	....	....	....	1.8412 287	14 020 478	7.6147 40
	....	....	....	1.8602 946	14.338 243	7.7075 12	1.8688 471	14.480 785	7.7485 12
	....	....	....	....	....	....	1.8968 798	14.947 997	7.8803 08
11	1.8982 986	14.971 643	7.8868 74	1.9161 034	15.268 390	7.9684 58	1.9253 330	15.422 217	8.0101 55
½	....	....	....	....	....	....	1.9542 130	15.903 550	8.1380 84
	....	....	....	1.9735 865	16.226 442	8.2218 04	1.9835 262	16.392 103	8.2641 22
	....	....	....	....	....	....	2.0132 791	16.887 985	8.3882 98
12	2.0121 965	16.869 941	8.3838 43	2.0327 941	17.213 235	8.4677 71	2.0434 783	17.391 305	8.5106 38
½	....	....	....	....	....	....	2.0741 305	17.902 174	8.6311 71
	....	....	....	2.0937 779	18.229 632	8.7065 74	2.1052 424	18.420 707	8.7499 22
	....	....	....	....	....	....	2.1368 211	18.947 018	8.8669 18
13	2.1329 283	18.882 138	8.8526 82	2.1565 913	19.276 521	8.9384 21	2.1688 734	19.481 223	8.9821 85
½	....	....	....	....	....	....	2.2014 065	20.023 441	9.0957 49
	....	....	....	2.2212 890	20.354 817	9.1635 16	2.2344 276	20.573 793	9.2076 35
	....	....	....	....	....	....	2.2679 440	21.132 400	9.3178 67
14	2.2609 040	21.015 066	9.2949 83	2.2879 277	21.465 461	9.3820 54	2.3019 631	21.699 385	9.4264 69
½	....	....	....	....	....	....	2.3364 926	22.274 877	9.5334 67
	....	....	....	2.3565 655	22.609 425	9.5942 27	2.3715 400	22.859 000	9.6388 84
	....	....	....	....	....	....	2.4071 131	23.451 885	9.7427 43
15	2.3965 582	23.275 970	9.7122 48	2.4272 625	23.787 708	9.8002 21	2.4432 198	24.053 663	9.8450 67
½	....	....	....	....	....	....	2.4798 681	24.664 468	9.9458 79
	....	....	....	2.5000 803	25.001 339	10.000 21	2 5170 661	25.284 435	10.045 20
	....	....	....	....	....	....	2.5548 221	25.913 701	10.143 06
16	2.5403 517	25.672 528	10.105 89	2.5750 827	26.251 379	10.194 38	2.5931 444	26.552 407	10.239 46
17	2.6927 728	28.212 880	10.477 26	2.7319 053	28.865 088	10.565 92	2.7522 690	29.204 483	10.611 06
18	2.8543 392	30.905 653	10.827 60	2.8982 783	31.637 972	10.916 13	2 9211 580	32.019 300	10.961 17
19	3.0255 995	33.759 992	11.158 12	3.0747 835	34.579 725	11.246 23	3.1004 106	35.006 843	11.291 03
20	3.2071 355	36.785 591	11.469 92	3.2620 378	37.700 630	11.557 39	3.2906 628	38.177 713	11.601 83
21	3.3995 636	39.992 727	11.764 08	3.4606 959	41.011 598	11.850 68	3.4925 895	41 543 159	11.894 66
22	3.6035 374	43.392 290	12.041 58	3.6714 523	44.524 204	12.127 14	3.7069 072	45.115 120	12.170 56
23	3.8197 497	46.995 828	12.303 38	3.8950 437	48.250 728	12.387 72	3.9343 762	48.906 270	12.430 50
24	4.0489 346	50.815 577	12.550 36	4.1322 519	52.204 198	12.633 35	4.1758 034	52.930 057	12.675 42
25	4.2918 707	54.864 512	12.783 36	4.3839 060	56.398 434	12.864 88	4.4320 456	57.200 761	12.906 18

Years.	RATIO of INTEREST: ANNUALLY, 0.06.			RATIO of INTEREST: HALF-YEARLY, 0.03.			RATIO of INTEREST: QUARTERLY, 0.015.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
½	....	....	....	....	....	....	0.9852 217	4.0000 000	4.0600 000
	....	....	....	0.9708 737	2.0000 000	2.0600 000	0.9706 618	1.9851 117	2.0451 117
1½	....	....	....	....	....	....	0.9563 170	1.3135 318	1.3735 318
	0.9433 962	1.0000 000	1.0600 000	0.9425 960	0.9852 217	1.0452 217	0.9421 841	0.9777 792	1.0377 792
2½	....	....	....	....	....	....	0.9282 603	0.7763 573	0.8363 573
	....	....	....	0.9151 417	0.6470 607	0.7070 607	0.9145 421	0.6421 008	0.7021 008
3½	....	....	....	....	....	....	0.9010 267	0.5462 247	0.6062 247
	0.8899 965	0.4854 369	0.5454 369	0.8884 871	0.4780 541	0.5380 541	0.8877 111	0.4743 361	0.5343 361
4½	....	....	....	....	....	....	0.8745 922	0.4184 393	0.4784 393
	....	....	....	0.8626 088	0.3767 092	0.4367 092	0.8616 672	0.3737 367	0.4337 367
5½	....	....	....	....	....	....	0.8489 332	0.3371 754	0.3971 754
	0.8396 193	0.3141 098	0.3741 098	0.8374 843	0.3091 950	0.3691 950	0.8363 874	0.3067 200	0.3667 200
6½	....	....	....	....	....	....	0.8240 270	0.2809 614	0.3409 614
	....	....	....	0.8130 915	0.2610 127	0.3210 127	0.8118 493	0.2588 933	0.3188 933
7½	....	....	....	....	....	....	0.7998 515	0.2397 774	0.2997 774
	0.7920 937	0.2285 915	0.2885 915	0.7894 093	0.2249 128	0.2849 128	0.7880 310	0.2230 603	0.2830 603
8½	....	....	....	....	....	....	0.7763 853	0.2083 186	0.2683 186
	....	....	....	0.7664 167	0.1968 677	0.2568 677	0.7649 116	0.1952 231	0.2552 231
9½	....	....	....	....	....	....	0.7536 074	0.1835 139	0.2435 139
	0.7472 582	0.1773 964	0.2373 964	0.7440 939	0.1744 610	0.2344 610	0.7424 704	0.1729 829	0.2329 829
10½	....	....	....	....	....	....	0.7314 979	0.1634 620	0.2234 620
	....	....	....	0.7224 213	0.1561 549	0.2161 549	0.7206 876	0.1548 133	0.2148 133
11½	....	....	....	....	....	....	0.7100 371	0.1469 230	0.2069 230
	0.7049 606	0.1433 626	0.2033 626	0.7013 798	0.1409 242	0.2009 242	0.6995 439	0.1396 964	0.1996 964
12½	....	....	....	....	....	....	0.6892 058	0.1330 578	0.1930 538
	....	....	....	0.6809 513	0.1280 591	0.1880 591	0.6790 205	0.1269 278	0.1869 278
13½	....	....	....	....	....	....	0.6689 857	0.1212 611	0.1812 611
	0.6650 571	0.1191 350	0.1791 350	0.6611 178	0.1170 527	0.1770 527	0.6590 993	0.1160 043	0.1760 043
14½	....	....	....	....	....	....	0.6493 589	0.1111 151	0.1711 151
	....	....	....	0.6418 620	0.1075 332	0.1675 332	0.6397 624	0.1065 568	0.1665 568
15½	....	....	....	....	....	....	0.6303 078	0.1022 972	0.1622 972
	0.6274 124	0.1010 359	0.1610 359	0.6231 669	0.0992 217	0.1592 217	0.6209 929	0.0983 084	0.1583 084
16½	....	....	....	....	....	....	0.6118 156	0.0945 658	0.1545 658
	....	....	....	0.6050 164	0.0919 051	0.1519 051	0.6027 741	0.0910 475	0.1510 475
17½	....	....	....	....	....	....	0.5938 661	0.0877 345	0.1477 345
	0.5918 975	0.0870 222	0.1470 222	0.5873 946	0.0854 174	0.1454 174	0.5850 897	0.0846 096	0.1446 096
18½	....	....	....	....	....	....	0.5764 431	0.0816 575	0.1416 575
	....	....	....	0.5702 860	0.0796 278	0.1396 278	0.5679 242	0.0788 645	0.1388 645
19½	....	....	....	....	....	....	0.5595 313	0.0762 185	0.1362 185
	0.5583 948	0.0758 680	0.1358 680	0.5536 758	0.0744 314	0.1344 314	0.5512 623	0.0737 084	0.1337 084
20½	....	....	....	....	....	....	0.5431 156	0.0713 242	0.1313 242
	....	....	....	0.5375 493	0.0697 435	0.1297 435	0.5350 893	0.0690 570	0.1290 570
21½	....	....	....	....	....	....	0.5271 815	0.0668 986	0.1268 986
	0.5267 875	0.0667 929	0.1267 929	0.5218 925	0.0654 948	0.1254 948	0.5193 907	0.0648 415	0.1248 415
22½	....	....	....	....	....	....	0.5117 149	0.0628 790	0.1228 790
	....	....	....	0.5066 918	0.0616 278	0.1216 278	0.5041 527	0.0610 050	0.1210 050
23½	....	....	....	....	....	....	0.4967 021	0.0592 137	0.1192 137
	0.4969 694	0.0592 770	0.1192 770	0.4919 338	0.0580 948	0.1180 948	0.4893 617	0.0575 000	0.1175 000
24½	....	....	....	....	....	....	0.4821 297	0.0558 591	0.1158 591
	....	....	....	0.4776 056	0.0548 557	0.1148 557	0.4750 047	0.0542 867	0.1142 867
25½	....	....	....	....	....	....	0.4679 849	0.0527 788	0.1127 788
	0.4688 390	0.0529 601	0.1129 601	0.4636 947	0.0518 766	0.1118 766	0.4610 689	0.0513 315	0.1113 315
26½	....	....	....	....	....	....	0.4542 550	0.0499 415	0.1099 415
	....	....	....	0.4501 891	0.0491 284	0.1091 284	0.4475 419	0.0486 055	0.1086 055
27½	....	....	....	....	....	....	0.4409 280	0.0473 207	0.1073 207
	0.4423 010	0.0475 849	0.1075 849	0.4370 768	0.0465 865	0.1065 865	0.4344 118	0.0460 843	0.1060 843
28½	....	....	....	....	....	....	0.4279 919	0.0448 936	0.1048 936
	....	....	....	0.4243 464	0.0442 293	0.1042 293	0.4216 669	0.0437 465	0.1037 465
29½	....	....	....	....	....	....	0.4154 354	0.0426 405	0.1026 405
	0.4172 650	0.0429 628	0.1029 628	0.4119 868	0.0420 385	0.1020 385	0.4092 960	0.0415 737	0.1015 737
30½	....	....	....	....	....	....	0.4032 473	0.0405 442	0.1005 442
	....	....	....	0.3999 871	0.0399 979	0.0999 979	0.3972 879	0.0395 500	0.0995 500
31½	....	....	....	....	....	....	0.3914 167	0.0385 896	0.0985 896
	0.3936 463	0.0389 521	0.0989 521	0.3883 370	0.0380 932	0.0980 932	0.3856 322	0.0376 614	0.0976 614
32½	0.3713 644	0.0354 448	0.0954 448	0.3660 449	0.0346 439	0.0946 439	0.3633 366	0.0342 413	0.0942 413
33½	0.3503 438	0.0323 565	0.0923 565	0.3450 324	0.0316 076	0.0916 076	0.3423 300	0.0312 312	0.0912 312
34½	0.3305 130	0.0296 209	0.0896 209	0.3252 262	0.0289 187	0.0889 187	0.3225 380	0.0285 658	0.0885 658
35½	0.3118 047	0.0271 846	0.0871 846	0.3065 568	0.0265 248	0.0865 248	0.3038 902	0.0261 933	0.0861 933
36½	0.2941 554	0.0250 045	0.0850 045	0.2889 592	0.0243 833	0.0843 833	0.2863 205	0.0240 714	0.0840 714
37½	0.2775 051	0.0230 456	0.0830 456	0.2723 718	0.0224 597	0.0824 597	0.2697 666	0.0221 655	0.0821 655
38½	0.2617 973	0.0212 785	0.0812 785	0.2567 365	0.0207 251	0.0807 251	0.2541 699	0.0204 473	0.0804 473
39½	0.2469 786	0.0196 790	0.0796 790	0.2419 988	0.0191 555	0.0791 555	0.2394 748	0.0188 929	0.0788 929
40½	0.2329 986	0.0182 267	0.0782 267	0.2281 071	0.0177 310	0.0777 310	0.2256 295	0.0174 823	0.0774 823

Years.	RATIO *of* INTEREST: *ANNUALLY*, 0.06.			RATIO *of* INTEREST: *HALF-YEARLY*, 0.03.			RATIO *of* INTEREST: *QUARTERLY*, 0.015.		
	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.	Improved Principal.	Cumulated Annuity.	Value of Annuity.
26	4.5493 830	59.156.383	13.003 17	4.6508 859	60.848 098	13.083 12	4.7040 116	61.733 527	13.123 59
27	4.8223 459	63.705 766	13.210 53	4.9341 248	65.568 746	13.288 83	4.9926 565	66.544 441	13.328 44
28	5.1116 867	68.528 112	13.406 16	5.2346 130	70.576 883	13.482 73	5.2990 342	71.650 570	13.521 44
29	5.4183 879	73.639 798	13.590 72	5 5534 010	75.890 016	13.665 50	5.6242 018	77.070 030	13.703 28
30	5.7434 912	79.058 186	13.764 83	5.8916 031	81.526 718	13.837 78	5.9693 228	82.822 047	13.874 61
31	6.0881 006	84.801 677	13.929 09	6.2504 017	87.506 695	14.000 17	6.3356 216	88.927 026	14.036 04
32	6.4533 867	90.889 778	14.084 05	6.6310 512	93.850 853	14.153 24	6.7243 978	95.406 630	14.188 13
33	6.8405 899	97.343 165	14.230 23	7.0348 822	100.58 137	14.297 52	7.1370 308	102.28 385	14.331 43
34	7.2510 253	104.18 375	14.368 14	7.4633 065	107.72 177	14.433 52	7.5749 843	109.58 307	14.466 44
35	7.6860 868	111.43 478	14.498 25	7.9178 219	115.29 703	14.561 71	8.0398 122	117.33 020	14.593 65
36	8.1472 520	119.12 087	14.620 99	8.4000 172	123.33 362	14.682 54	8.5331 637	125.55 273	14.713 50
37	8.6360 871	127.26 812	14.736 78	8.9115 783	131.85 964	14.796 44	9.0567 889	134.27 981	14.826 43
38	9.1542 523	135.90 421	14.846 02	9.4542 934	140.90 489	14.903 80	9.6125 456	143.54 243	14.932 82
39	9.7035 075	145.05 846	14.949 08	10.030 060	150.50 100	15.004 99	10.202 406	153.37 343	15.033 06
40	10.285 718	154.76 197	15.046 30	10.640 891	160.68 151	15.100 38	10.828 461	163.80 769	15.127 51
41	10.902 861	165.04 768	15.138 02	11.288 921	171.48 201	15.190 29	11.492 934	174.68 223	15.216 50
42	11.557 033	175.95 054	15.224 55	11.976 416	182.94 027	15.275 04	12.198 181	186.63 636	15.300 34
43	12.250 455	187.50 758	15.306 18	12.705 780	195.09 633	15.354 93	12.946 705	199.11 175	15.379 34
44	12.985 482	199.75 803	15.383 19	13.479 562	207.99 270	15.430 23	13.741 161	212.35 268	15.453 77
45	13.764 611	212.74 351	15.455 84	14.300 467	221.67 445	15.501 20	14.584 367	226.40 612	15.523 89
46	14.590 487	226.50 812	15.524 37	15.171 365	236.18 942	15.568 11	15.479 316	241.32 193	15.589 96
47	15.465 917	241.09 861	15.589 03	16.095 302	251.58 836	15.631 17	16.429 182	257.15 303	15.652 21
48	16.393 872	256.56 453	15.650 03	17.075 506	267.92 509	15.690 61	17.437 335	273.95 558	15.710 86
49	17.377 504	272.95 840	15.707 58	18.115 404	285.25 673	15.746 64	18.507 351	291.78 919	15.766 12
50	18.420 154	290.33 590	15.761 86	19.218 632	303.64 387	15.799 45	19.643 029	310.71 714	15.818 19
51	19.525 364	308.75 606	15.813 08	20.389 047	323.15 078	15.849 23	20.848 395	330 80 658	15.867 24
52	20.696 885	328.28 142	15.861 40	21.630 740	343.84 566	15.896 16	22.127 726	352 12 877	15.913 46
53	21.938 698	348.97 831	15.906 98	22.948 052	365.80 086	15.940 39	23.485 562	374.75 937	15.957 01
54	23.255 020	370.91 701	15.949 98	24.345 588	389.09 313	15.982 08	24.926 719	398.77 866	15.998 04
55	24.650 322	394.17 203	15.990 55	25.828 234	413.80 391	16.021 38	26.456 311	424.27 186	16.036 70
56	26.129 341	418.82 235	16.028 82	27.401 174	440.01 956	16.058 42	28.079 765	451.32 941	16 073 12
57	27.697 101	444.95 169	16.064 92	29.069 905	467.83 175	16 093 34	29.802 839	480.04 731	16.107 44
58	29.358 927	472.64 879	16.098 98	30.840 262	497.33 771	16.126 25	31.631 647	510.52 745	16.139 77
59	31.120 463	502.00 772	16.131 12	32.718 434	528.64 057	16.157 27	33.572 677	542.87 795	16.170 23
60	32.987 691	533.12 818	16.161 43	34.710 987	561.84 979	16.186 51	35.632 816	577.21 359	16.198 93
61	34.966 952	566.11 587	16.190 03	36.824 886	597.08 144	16.214 07	37.819 372	613.65 619	16.225 98
62	37.064 969	601.08 282	16.217 01	39.067 522	634.45 870	16.240 05	40.140 103	652.33 504	16.251 45
63	39.288 868	638.14 779	16.242 46	41.446 734	674.11 223	16.264 54	42.603 242	693.38 736	16.275 46
64	41.646 199	677.43 666	16.266 47	43.970 840	716.18 067	16.287 63	45.217 528	736.95 880	16.298 08
65	44.144 972	719.08 286	16.289 13	46.648 664	760.81 107	16.309 38	47.992 236	783.20 393	16.319 39
66	46.793 670	763.22 783	16.310 50	49.489 568	808.15 946	16.329 90	50.937 210	832.28 683	16.339 47
67	49.601 290	810.02 150	16.330 66	52.503 482	858.39 137	16.349 23	54.062 898	884.38 163	16.358 38
68	52.577 368	859.62 279	16.349 68	55.700 945	911.68 241	16.367 45	57.380 389	939.67 316	16.376 21
69	55.732 010	912.20 016	16.367 62	59.093 132	968.21 887	16.384 63	60.901 454	998.35 757	16.393 00
70	59.075 930	967.93 217	16.384 55	62.691 904	1028.1 984	16.400 82	64.638 583	1060.6 431	16.408 82
71	62.620 486	1027.0 081	16.400 52	66.509 841	1091.8 307	16.416 08	68.605 036	1126.7 506	16.423 78
72	66.377 715	1089.6 286	16.415 58	70.560 290	1159.3 382	16.430 46	72.814 885	1196.9 147	16.437 78
73	70.360 378	1156.0 053	16.429 79	74.857 412	1230.9 569	16.444 02	77.283 065	1271.3 844	16.451 01
74	74.582 001	1226.3 667	16.443 20	79.416 228	1306.9 371	16.456 80	82.025 428	1350.4 238	16.463 48
75	79.056 921	1300.9 487	16.455 85	84.252 676	1387.5 446	16.468 85	87.058 800	1434.3 133	16.475 22
76	83.800 336	1380.0 056	16.467 78	89.383 664	1473.0 611	16.480 20	92.401 037	1523.3 506	16.486 29
77	88.828 356	1463.8 059	16.479 04	94.827 130	1563.7 855	16.490 91	98.071 092	1617.8 515	16.496 72
78	94.158 058	1552.6 343	16.489 66	100.60 210	1660.0 350	16.501 00	104.08 908	1718.1 514	16.506 55
79	99.807 541	1646.7 924	16.499 68	106.72 877	1762.1 462	16.510 51	110.47 636	1824.6 060	16.515 81
80	105.79 599	1746.5 999	16.509 13	113.22 855	1870.4 759	16.519 47	117.25 558	1937.5 930	16.524 53
81	112 14 375	1852.3 959	16.518 05	120.12 417	1985.4 028	16.527 92	124.45 080	2057.5 133	16.532 74
82	118.87 238	1964.5 396	16.526 46	127.43 973	2107.3 289	16.535 89	132.08 754	2184.7 924	16.540 49
83	126.00 472	2083.4 120	16.534 40	135.20 081	2236.6 802	16.543 39	140.19 290	2319.8 817	16.547 78
84	133.56 500	2209.4 167	16.541 89	143.43 454	2373.9 090	16.550 47	148.79 564	2463.2 606	16.554 65
85	141.57 890	2342.9 817	16.548 95	152.16 971	2519.4 951	16.557 14	157.92 627	2615.4 378	16.561 13
86	150.07 364	2484.5 606	16.555 61	161.43 684	2673.9 473	16.563 43	167.61 718	2776.9 530	16.567 23
87	159.07 806	2634.6 343	16.561 90	171.26 834	2837.8 057	16.569 35	177.90 277	2948.3 794	16.572 98
88	168.62 274	2793.7 123	16.567 83	181.69 859	3011.6 431	16.574 93	188.81 951	3130.3 252	16.578 40
89	178.74 010	2962.3 351	16.573 42	192.76 403	3196.0 672	16.580 21	200.40 615	3323.4 358	16.583 50
90	189.46 451	3141.0 752	16.578 70	204.50 336	3391.7 227	16.585 17	212.70 378	3528.3 963	16.588 31
91	200.83 238	3330.5 397	16.583 68	216.95 761	3599.2 936	16.589 84	225.75 604	3745.9 340	16.592 84
92	212.88 232	3531.3 721	16.588 38	230.17 033	3819.5 055	16.594 26	239.60 923	3976.8 205	16.597 11
93	225.65 526	3744.2 544	16.592 81	244.18 771	4053.1 284	16.598 41	254.31 251	4221.8 751	16.601 13
94	239.19 458	3969.9 097	16.596 99	259.05 874	4300.9 790	16.602 33	269.91 802	4481.9 671	16.604 92
95	253.54 625	4209.1 042	16.600 94	274.83 541	4563.9 236	16.606 02	286.48 115	4758.0 192	16.608 49
96	268.75 903	4462.6 505	16.604 66	291.57 289	4842.8 815	16.609 51	304.06 065	5051.0 109	16.611 85
97	284.88 457	4731.4 095	16.608 17	309.32 968	5138.8 280	16.612 79	322.71 889	5361.9 816	16.615 02
98	301.97 765	5016.2 941	16.611 48	328.16 786	5452.7 976	16.615 88	342.52 207	5692.0 345	16.618 01
99	320.09 631	5318.2 718	16.614 60	348.15 328	5785.8 880	16.618 79	363.54 044	6042.3 407	16.620 82
100	339.30 208	5638.3 681	16.617 55	369.35 582	6139.2 636	16.621 54	385.84 857	6414.1 429	16.623 47
	Value of Perpetual Ann.		16.666 67	- - - - - - - - - -		16.666 67	- - - - - - - - - -		16.666 67

Years.	RATIO of INTEREST: ANNUALLY, 0.06.			RATIO of INTEREST: HALF-YEARLY, 0.03.			RATIO of INTEREST: QUARTERLY, 0.015.		
	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.	Discounted Principal.	Annuity for Cumulation	Ratio of Annuity.
26	0.2198 100	0.0169 043	0.0769 043	0.2150 128	0.0164 344	0.0764 344	0.2125 845	0.0161 987	0.0761 987
27	0.2073 680	0.0156 972	0.0756 972	0.2026 702	0.0152 512	0.0752 512	0.2002 938	0.0150 279	0.0750 279
28	0.1956 301	0.0145 926	0.0745 926	0.1910 361	0.0141 689	0.0741 689	0.1887 136	0.0139 566	0.0739 566
29	0.1845 527	0.0135 796	0.0735 796	0.1800 698	0.0131 770	0.0731 770	0.1778 030	0.0129 752	0.0729 752
30	0.1741 181	0.0126 489	0.0726 489	0.1697 331	0.0122 659	0.0722 659	0.1675 232	0.0120 741	0.0720 741
31	0.1642 548	0.0117 922	0.0717 922	0.1599 897	0.0114 277	0.0714 277	0.1578 377	0.0112 452	0.0712 452
32	0.1549 574	0.0110 023	0.0710 023	0.1508 057	0.0106 552	0.0706 552	0.1487 122	0.0104 814	0.0704 814
33	0.1461 862	0.0102 729	0.0702 729	0.1421 488	0.0099 422	0.0699 422	0.1401 143	0.0097 767	0.0697 767
34	0.1379 115	0.0095 984	0.0695 984	0.1339 889	0.0092 832	0.0692 832	0.1320 135	0.0091 255	0.0691 255
35	0.1301 052	0.0089 739	0.0689 739	0.1262 973	0.0086 733	0.0686 733	0.1243 810	0.0085 230	0.0685 230
36	0.1227 408	0.0083 948	0.0683 948	0.1190 474	0.0081 081	0.0681 081	0.1171 898	0.0079 648	0.0679 648
37	0.1157 932	0.0078 574	0.0678 574	0.1122 135	0.0075 838	0.0675 838	0.1104 144	0.0074 471	0.0674 471
38	0.1092 389	0.0073 581	0.0673 581	0.1057 720	0.0070 970	0.0670 970	0.1040 307	0.0069 666	0.0669 666
39	0.1030 555	0.0068 938	0.0668 938	0.0997 003	0.0066 445	0.0666 445	0.0980 161	0.0065 200	0.0665 200
40	0.0972 222	0.0064 617	0.0664 617	0.0939 771	0.0062 235	0.0662 235	0.0923 492	0.0061 047	0.0661 047
41	0.0917 190	0.0060 589	0.0660 589	0.0885 824	0.0058 315	0.0658 315	0.0870 100	0.0057 181	0.0657 181
42	0.0865 274	0.0056 834	0.0656 834	0.0834 974	0.0054 663	0.0654 663	0.0819 794	0.0053 580	0.0653 580
43	0.0816 296	0.0053 331	0.0653 331	0.0787 043	0.0051 257	0.0651 257	0.0772 397	0.0050 223	0.0650 223
44	0.0770 091	0.0050 061	0.0650 061	0.0741 864	0.0048 079	0.0648 079	0.0727 741	0.0047 091	0.0647 091
45	0.0726 501	0.0047 005	0.0647 005	0.0699 278	0.0045 111	0.0645 111	0.0685 666	0.0044 168	0.0644 168
46	0.0685 378	0.0044 149	0.0644 149	0.0659 136	0.0042 339	0.0642 339	0.0646 023	0.0041 438	0.0641 438
47	0.0646 583	0.0041 477	0.0641 477	0.0621 299	0.0039 747	0.0639 747	0.0608 673	0.0038 887	0.0638 887
48	0.0609 984	0.0038 977	0.0638 977	0.0585 634	0.0037 324	0.0637 324	0.0573 482	0.0036 502	0.0636 502
49	0.0575 457	0.0036 636	0.0636 636	0.0552 016	0.0035 056	0.0635 056	0.0540 326	0.0034 271	0.0634 271
50	0.0542 884	0.0034 443	0.0634 443	0.0520 328	0.0032 933	0.0632 933	0.0509 086	0.0032 184	0.0632 184
51	0.0512 154	0.0032 388	0.0632 388	0.0490 459	0.0030 945	0.0630 945	0.0479 653	0.0030 229	0.0630 229
52	0.0483 164	0.0030 462	0.0630 462	0.0462 305	0.0029 083	0.0629 083	0.0451 922	0.0028 399	0.0628 399
53	0.0455 816	0.0028 655	0.0628 655	0.0435 767	0.0027 337	0.0627 337	0.0425 793	0.0026 684	0.0626 684
54	0.0430 015	0.0026 960	0.0626 960	0.0410 752	0.0025 701	0.0625 701	0.0401 176	0.0025 077	0.0625 077
55	0.0405 674	0.0025 370	0.0625 370	0.0387 173	0.0024 166	0.0624 166	0.0377 982	0.0023 570	0.0623 570
56	0.0382 712	0.0023 876	0.0623 876	0.0364 948	0.0022 726	0.0622 726	0.0356 128	0.0022 157	0.0622 157
57	0.0361 049	0.0022 474	0.0622 474	0.0343 998	0.0021 375	0.0621 375	0.0335 538	0.0020 831	0.0620 831
58	0.0340 612	0.0021 157	0.0621 157	0.0324 251	0.0020 107	0.0620 107	0.0316 139	0.0019 588	0.0619 588
59	0.0321 332	0.0019 920	0.0619 920	0.0305 638	0.0018 916	0.0618 916	0.0297 861	0.0018 420	0.0618 420
60	0.0303 143	0.0018 757	0.0618 757	0.0288 093	0.0017 798	0.0617 798	0.0280 640	0.0017 325	0.0617 325
61	0.0285 984	0.0017 664	0.0617 664	0.0271 555	0.0016 748	0.0616 748	0.0264 415	0.0016 296	0.0616 296
62	0.0269 797	0.0016 637	0.0616 637	0.0255 967	0.0015 761	0.0615 761	0.0249 127	0.0015 330	0.0615 330
63	0.0254 524	0.0015 670	0.0615 670	0.0241 274	0.0014 834	0.0614 834	0.0234 724	0.0014 422	0.0614 422
64	0.0240 118	0.0014 762	0.0614 762	0.0227 423	0.0013 963	0.0613 963	0.0221 153	0.0013 569	0.0613 569
65	0.0226 526	0.0013 907	0.0613 907	0.0214 368	0.0013 144	0.0613 144	0.0208 367	0.0012 768	0.0612 768
66	0.0213 704	0.0013 102	0.0613 102	0.0202 063	0.0012 374	0.0612 374	0.0196 320	0.0012 015	0.0612 015
67	0.0201 608	0.0012 345	0.0612 345	0.0190 464	0.0011 650	0.0611 650	0.0184 970	0.0011 307	0.0611 307
68	0.0190 196	0.0011 633	0.0611 633	0.0179 530	0.0010 969	0.0610 969	0.0174 276	0.0010 642	0.0610 642
69	0.0179 430	0.0010 963	0.0610 963	0.0169 224	0.0010 328	0.0610 328	0.0164 200	0.0010 016	0.0610 016
70	0.0169 274	0.0010 331	0.0610 331	0.0159 510	0.0009 726	0.0609 726	0.0154 706	0.0009 428	0.0609 428
71	0.0159 692	0.0009 737	0.0609 737	0.0150 354	0.0009 159	0.0609 159	0.0145 762	0.0008 875	0.0608 875
72	0.0150 653	0.0009 177	0.0609 177	0.0141 723	0.0008 626	0.0608 626	0.0137 335	0.0008 355	0.0608 355
73	0.0142 125	0.0008 650	0.0608 650	0.0133 587	0.0008 124	0.0608 124	0.0129 394	0.0007 865	0.0607 865
74	0.0134 081	0.0008 154	0.0608 154	0.0125 919	0.0007 651	0.0607 651	0.0121 913	0.0007 405	0.0607 405
75	0.0126 491	0.0007 687	0.0607 687	0.0118 691	0.0007 207	0.0607 207	0.0114 865	0.0006 972	0.0606 972
76	0.0119 331	0.0007 246	0.0607 246	0.0111 877	0.0006 789	0.0606 789	0.0108 224	0.0006 564	0.0606 564
77	0.0112 577	0.0006 832	0.0606 832	0.0105 455	0.0006 395	0.0606 395	0.0101 967	0.0006 181	0.0606 181
78	0.0106 204	0.0006 441	0.0606 441	0.0099 401	0.0006 024	0.0606 024	0.0096 072	0.0005 820	0.0605 820
79	0.0100 193	0.0006 072	0.0606 072	0.0093 695	0.0005 675	0.0605 675	0.0090 517	0.0005 481	0.0605 481
80	0.0094 522	0.0005 725	0.0605 725	0.0088 317	0.0005 346	0.0605 346	0.0085 284	0.0005 161	0.0605 164
81	0.0089 171	0.0005 398	0.0605 398	0 0083 247	0.0005 037	0.0605 037	0.0080 353	0.0004 860	0.0604 860
82	0.0084 124	0.0005 090	0.0605 090	0.0078 468	0.0004 745	0.0604 745	0.0075 707	0 0004 577	0 0604 577
83	0.0079 362	0.0004 800	0.0604 800	0.0073 964	0.0004 471	0.0604 471	0.0071 330	0.0004 311	0.0604 311
84	0.0074 870	0.0004 526	0.0604 526	0.0069 718	0.0004 212	0.0604 212	0.0067 206	0.0004 060	0.0604 060
85	0.0070 632	0.0004 268	0.0604 268	0.0065 716	0.0003 969	0.0603 969	0.0063 321	0.0003 823	0.0603 823
86	0.0066 634	0.0004 025	0.0604 025	0.0061 944	0.0003 740	0.0603 740	0.0059 660	0.0003 601	0.0603 601
87	0.0062 862	0.0003 796	0.0603 796	0.0058 388	0 0003 524	0.0603 524	0.0056 210	0.0003 392	0.0603 392
88	0.0059 304	0.0003 579	0.0603 579	0.0055 036	0.0003 320	0.0603 320	0.0052 961	0.0003 195	0.0603 195
89	0.0055 947	0.0003 376	0.0603 376	0.0051 877	0.0003 129	0.0603 129	0.0049 899	0.0003 009	0.0603 009
90	0.0052 780	0.0003 184	0.0603 184	0.0048 899	0.0002 948	0.0602 948	0.0047 014	0.0002 834	0.0602 834
91	0.0049 793	0.0003 003	0.0603 003	0.0046 092	0.0002 778	0.0602 778	0.0044 296	0.0002 670	0.0602 670
92	0.0046 974	0.0002 832	0.0602 832	0.0043 446	0.0002 618	0.0602 618	0.0041 735	0.0002 515	0.0602 515
93	0.0044 315	0.0002 671	0.0602 671	0.0040 952	0.0002 467	0.0602 467	0.0039 322	0.0002 369	0.0602 369
94	0.0041 807	0.0002 519	0.0602 519	0.0038 601	0.0002 325	0.0602 325	0.0037 048	0.0002 231	0.0602 231
95	0.0039 441	0.0002 376	0.0602 376	0.0036 385	0.0002 191	0.0602 191	0.0034 906	0.0002 102	0.0602 102
96	0.0037 208	0.0002 241	0.0602 241	0.0034 297	0.0002 065	0.0602 065	0.0032 888	0 0001 980	0.0601 980
97	0.0035 102	0.0002 114	0.0602 114	0.0032 328	0.0001 946	0.0601 946	0.0030 987	0.0001 865	0.0601 865
98	0.0033 115	0.0001 994	0.0601 994	0.0030 472	0.0001 834	0.0601 834	0.0029 195	0.0001 757	0.0601 757
99	0.0031 241	0.0001 880	0.0601 880	0.0028 723	0.0001 728	0.0601 728	0.0027 507	0.0001 655	0.0601 655
100	0.0029 472	0.0001 774	0.0601 774	0.0027 074	0.0001 629	0.0601 629	0.0025 917	0.0001 559	0.0601 559
	Ratio of Perpetual Ann.		0.0600 000	- - - - - - - - -		0.0600 000	- - - - - - - - -		0.0600 000

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